Intensity Dependent Confidence Intervals on Microarray Measurements of Differentially Expressed Genes: A case study of the effect of MK5, FKRP and TAF4 on the transcriptome

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Abstract

To perform a quantitative analysis with gene-arrays, one must take into account inaccuracies (experimental variations, biological variations and other measurement errors) which are seldom known. In this paper we investigated amplification and noise propagation related errors by measuring intensity dependent variations. Based on a set of control samples, we create confidence intervals on up and down regulations. We validated our method through a qPCR experiment and compared it to standard analysis methods (including loess normalization and filtering methods based on genetic variability). The results reveal that experimental variability and amplification related errors are a major concern that should be accounted for.

Keywords: Microarray analysis, confidence intervals, measurement errors, gene-array, upregulation, downregulation, differential expression

Running Title: MK5, TAF4, FKRP on Microarrays.
1 Introduction

The transcriptome contains all the mRNA transcripts in a specific cell(type) under certain conditions. Depending on these conditions, the amount of individual mRNA may vary. Microarray studies allow the rapid identification of many transcripts in cells under controlled conditions and can be used to compare expression patterns of genes between cell systems under different circumstances. For example, one can monitor the transcripts in normal versus diseased cells, or control cells versus cells lacking a specific gene or overexpression of a particular protein or a mutated form of a protein.

Analysis of such differential expression experiments often involves normalization [SS03, CGS92], data filtering [DYCS00] and reporting measured changes. Subsequently, neural networks [SOM03], eigenvalue decomposition [SMRL05, ABB00] and various cluster algorithms [BL02, NGK01] can help to elucidate the results. Annotation of genes with their cellular location, function or gene-category/sequence then provides more insight into the effects of the altered gene expression.

In this paper we focus on the measurement processes involved in such experiments. Microarrays contain a number of error-sources [RCB+01], some of them physical (quenching [Kub94, RW97]), some chemical (hybridization), some related to the electronics (gating [SN06], dynamic range [dlNvHT06], saturation [LBS+04]). In most microarray experiments the measurement errors remain unknown, but they are widely believed to follow Lorentz distributions [PTVF03, BWWQ02]).

The general assumption with such experiments is that 'strong signals are better signals'. However, given the realization that cell systems might propagate/amplify noise throughout genetic pathways, we hypothesized that strong signals might be subject to greater measurement errors. Instead of having an absolute error one would then find a relative error as well. To study such errors we conducted a number of experiments that all included a control sample. That control sample would simultaneously account for experimental-, biological- and machine-related variations, after which we could assess the error distributions on an intensity specific basis. Based on the error model, our technique reports confidence intervals for up/down regulation.

This study is set in the context of three experiments. The first involves the mitogen-activated protein kinase-activated protein kinase-5 (MAPKAPK5 or MK5). This murine protein kinase belongs to the MAPK signaling pathway and at present, knowledge of its role in cellular processes remains limited [Gae06]. To examine a possible effect of MK5 on transcription, we constructed a doxycycline-inducible PC12 cell line that allowed inducible expression of a constitutive active form of MK5 (MK5L337A). RNA was purified from three independent samples of cells grown in the presence of doxycycline (no expression of activated MK5) and from three independent samples of cells in which the expression of MK5 was turned on by removal of doxycycline. Each microarray slide (KTH Rat 27k Oligo Microarray-Operon ver3.0) was loaded with one sample uninduced (Cy5) and one sample induced (Cy3) (for a reference on Cy5/Cy3 see [MEM+93]). We added a fourth slide containing two induced samples as a control for measurement errors.

The second experiment involves the TATA binding protein Associated Factor 4 (TAF4). The transcription factor TFIID is a multiprotein complex composed of the TATA box-binding protein (TBP) and multiple TBP-associated factors (TAFs). TFIID plays an essential role in mediating transcriptional activation by gene-specific activators. TAFs have been postulated to exert several important roles in transcription acting as core promoter specificity factors and co-activators. Genetic studies in vertebrate cells also point to an essential role of TAFs in cell cycle progression [TC06, NBT01, AT00, DKFM05]. Using siRNAs we measured the influence of TAF4 depletion on the transcriptome1. These experiments were performed in HeLa cells and SK-N-DZ cells. For each cell type we used 4 slides with scrambled siRNAs and 4 slides with TAF4-directed siRNA. The microarrays relied on DIG (digoxigenin) labeling.

The third experiment focuses on a putative glycosyltransferase. A number of congenital muscular dystrophies (CMD) are now known to be associated with mutations in genes encoding for proteins that are either putative or determined glycosyltransferases lending support to the idea that aberrant post-translational modifications of proteins may represent a new mechanism of pathogenesis in the muscular dystrophies. One of these genes, fukutin-related protein (FKRP), is thought to be coding for a putative glycosyltransferase, but its function has not yet been established [BBBF02]. To evaluate the possible effect of FKRP on transcription we transfected C2C12 cells with siRNA that targets FKRP. The results of the transfection were measured using microarray analysis using DIG labeling. Table 1 gives an overview of the different experiments.

1SiRNA will bind to the transcript and activate the destruction or prevent translation of the target sequence [Elb01].
Table 1: Overview of the different experiments.

<table>
<thead>
<tr>
<th>Experiment Labeling</th>
<th>Constitutive Active MK5</th>
<th>FKR RP Knockdown</th>
<th>TAF4 Knockdown</th>
</tr>
</thead>
<tbody>
<tr>
<td>Microarray</td>
<td>KTH Rat272 Oligo m.a.</td>
<td>Applied Biosystems Mouse Genome Survey m.a.V2.0</td>
<td>Applied Biosystems Human Geno me Survey m.a.V2.0</td>
</tr>
<tr>
<td></td>
<td>OperonV3.0 Tecan HS 4800</td>
<td>DIG Labeling</td>
<td>DIG Labeling</td>
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<tr>
<td></td>
<td>GenePix 4000B</td>
<td>Applied Biosystems 1700 scanner</td>
<td>Applied Biosystems 1700 scanner</td>
</tr>
<tr>
<td>Cells</td>
<td>Normal (Cy5)</td>
<td>sRNA 1</td>
<td>sRNA</td>
</tr>
<tr>
<td></td>
<td>MK5 Induced (Cy3)</td>
<td>sRNA #1</td>
<td>sRNA</td>
</tr>
<tr>
<td></td>
<td>Control (Both)</td>
<td>Scrambled</td>
<td>Scrambled</td>
</tr>
<tr>
<td>Amount</td>
<td>3</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>Requested Comparisons</td>
<td>C2C12</td>
<td>SK-N-DZ</td>
<td>HeLa</td>
</tr>
<tr>
<td>Blind analysis</td>
<td>Microarray facility Tronhein Quantile Normalization</td>
<td>UNIGEN (Tronheim)</td>
<td>UNIGEN (Tronheim)</td>
</tr>
<tr>
<td></td>
<td>27468 reported of which 4007 in agreement</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>Both Quantile &amp; no normalization</td>
<td>Applied Biosystems Inter-array normalization</td>
<td>Applied Biosystems Inter-array normalization</td>
</tr>
<tr>
<td>Intensity dependent analysis</td>
<td>1422</td>
<td>2977</td>
<td>576</td>
</tr>
<tr>
<td></td>
<td>2497 (22 validated through qPCR)</td>
<td>661</td>
<td>65</td>
</tr>
<tr>
<td>Overlap</td>
<td>311, with 10 wrong in the standard analysis</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

2 Analysis Method

The presented analysis method measures the variance of a control sample, then uses it to model an intensity dependent error distribution and based on that defines confidence intervals for each individual spot, or group of spots. Regulations are reported as terms within a confidence interval of 95%. Conversion to ratios can be performed as necessary.

2.1 Acquiring the Error Model

To acquire the error model, one can employ two techniques. The first supplies a number of identical pairs of biological samples and puts them on different slides. For instance, one slide can contain the TAF4 downregulated transcript, while another slide contains the normal transcript. One can then use the inter-slide variance to develop an error model. A second approach, and the one used for the MK5 experiment, acquires the error on the regulation difference. In this setup, one provides the same sample for red and green. Because red and green have the same content one expects both channels to be equal for all spots. In the discussion below we assume that red and green name two samples that ought to be compared. Whether they are using Cy5/Cy3 staining or DIG labeling is irrelevant for the discussion.

Figure 1 plots the red and green channel of such a control slide. We find that the variance around the expected values increases together with the spot intensity. This phenomenon indicates relative errors, and is the main reason why one relies on a log-transform. However, in the second half (with red or green intensities larger than 32768) the variance decreases with increasing spots intensity. A partial reason for this might lie in the number of saturated pixels.
Figure 1: Scatterplot of the control slides and the two measurements of the MK5 experiments. The red points are from slide 1. The green points are from slide 3. The blue points are from the control slide. Horizontally the red channel is set out, vertically the green. The bend is due to quenching [Kub94]. The variance of the control slide can be observed in the width of the blue area. It increases up to 32768 (indicated with gray dotted lines), after which it decreases again. In a perfect world, the control sample should have the same red as green value, and be a straight line.

The above observation on the error distribution prohibits us to use a maximum likelihood estimation of the absolute and relative errors [ITAL00, PTVF03]. Instead, we model a collection of error distributions: one for each intensity. A two-dimensional map will count the number of spots with a specific intensity and deviation. Spot intensity (set out horizontally) is calculated as the mean of the red and green channel. Spot deviation (set out vertically) is red subtracted from green. Afterward, the algorithm normalizes the two-dimensional histogram so that each intensity has: a) a proper cumulative probability distribution and b) relies on enough samples to have a good estimate of the modeled error. This process is detailed in section 7 and results in two functions $F$ and $G$. They produce respectively a probability distribution and cumulative probability distribution for each intensity ($x$).

$$G(x) (y) = P\left(r - g < y \text{ with } \frac{r + g}{2} = x\right)$$

For illustrative purposes, we added $x$ and $y$ labels to Figure 1. Figure 2 plots the error distribution of the MK5 experiment. When the error model is obtained from different slides then the probability distribution $F$ (and associated cumulative distribution $G$) is based on the error model of each slide and convolved accordingly.
Figure 2: Error Distribution of various up/down regulation experiments. Horizontally the spot intensity is set out. Vertically the measurement error is set out as a cumulative distribution function. The cumulative distribution expresses the probability that a specific difference will occur due to experimental, biological or measurement variations. The colors are more intense within the 95% confidence interval. With such a diagram one can to determine the limits in which a regulation is very likely to fall. The multiple diagrams are measurement errors obtained from different experiments and different machines. The MK5 sample was Cy5/Cy3 stained and scanned on a Tecan scanner. All other samples were DIG labeled and scanned on an Applied Biosystems 1700 microarray scanner. As an example how to read the diagrams: in the MK5 diagram (top right) we find that the biological variation is larger for spots with intensity 32768. If a measured spot has intensity 32768, then its 95% confidence interval on the difference between the two channels is around $[-9000, 9000]$ (marked with a white arrow).

2.2 Confidence Intervals on One Measurement

Assuming that the probability distribution $f$ expresses the error distribution of a specific spot, and that $r$ is the real (but unknown) regulation, then our measurement $m$ will report a value in the range $m = r + \epsilon$, in which $\epsilon$ satisfies $f$. In other words, instead of measuring the real regulation, we will always measure the real regulation with some extra unknown error. Since we know $m$ and have some understanding of $\epsilon$ (its distribution) we can state that $r = m - \epsilon$. Thus, by determining a confidence interval on $\epsilon$ we can report a confidence interval on $r$ as well.

A 95% confidence interval for spots with intensity $x$ is given as $[G^{-1}(x)(0.025) : G^{-1}(x)(0.975)]$. If a spot measures as $m$, then in 95% of the cases, the real regulation falls within

$$[m - G^{-1}(\langle m \rangle)(0.025) : m - G^{-1}(\langle m \rangle)(0.975)]$$
2.3 Reporting Regulations

A widely accepted method for quantitative measurement are log-ratios. Despite widely used, they have a number of important limitations. First, the log ratio cannot capture information such as the measurement error. For instance the ratio 2/1 has probably more errors involved than 2000/1000. The $\log_{10}$ ratio will report 0.3 regardless. Secondly, the log ratio has numerical problems near zero. An up- or downregulation from zero to 1416 might make biological sense but it seems inappropriate to express it as a (log-)ratio of $\infty$.

To approach these challenges, our method reports the measured regulation as the difference between two slides, thereby including the lowest and highest expected differences (Table 2). In many cases this leads to an up- or downregulation. Such non-sensical regulations ought to be filtered out since the possible error outweighs the actual measurement. Eg, a confidence interval of $[−1950 : 1950]$ for a spot with a regulation of $−500$ indicates that the real regulation-difference will range within $[−2450 : 1450]$. Figure 3A illustrates a set of points omitted due to such filtering.

<table>
<thead>
<tr>
<th>Gene #</th>
<th>Confidence Interval</th>
<th>Difference</th>
<th>Summed Values</th>
<th>Regulation Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>At least</td>
<td>At most</td>
<td>Green</td>
</tr>
<tr>
<td>1-6430.72:6840.32</td>
<td>-39267.7 -32837 -25996.7</td>
<td>39613 6776 2</td>
<td>down</td>
<td>4.84</td>
</tr>
<tr>
<td>2-2447.36:2242.56</td>
<td>-7807.36 -5360 -3117.44</td>
<td>6191 831 2</td>
<td>down</td>
<td>4.75</td>
</tr>
<tr>
<td>3-2355.22199.92</td>
<td>-5122.2 -2767 -637.08</td>
<td>3807 1040 2</td>
<td>down</td>
<td>1.61</td>
</tr>
<tr>
<td>4-2775.04:2754.56</td>
<td>1531.96 4307 7061.56</td>
<td>2531 6838 6</td>
<td>up</td>
<td>1.61</td>
</tr>
<tr>
<td>5-2437.12:2447.36</td>
<td>-5919.12 -3482 -1034.64</td>
<td>5215 1733 4</td>
<td>down</td>
<td>1.6</td>
</tr>
<tr>
<td>6-2037.76:2457.6</td>
<td>472.24 2510 4967.6</td>
<td>809 3319 2</td>
<td>up</td>
<td>1.58</td>
</tr>
<tr>
<td>7-3532.8:3430.4</td>
<td>2701.2 6234 9664.4</td>
<td>4818 11052 4</td>
<td>up</td>
<td>1.56</td>
</tr>
<tr>
<td>8-1812.48:1536</td>
<td>-3697.48 -1885 -339</td>
<td>2514 629 2</td>
<td>down</td>
<td>1.55</td>
</tr>
<tr>
<td>9-2590.72:2621.44</td>
<td>-6302.72 -3712 -1090.56</td>
<td>5684 1972 6</td>
<td>down</td>
<td>1.55</td>
</tr>
<tr>
<td>10-2170.88:2314.23</td>
<td>969.12 3140 5454.24</td>
<td>1854 4996 4</td>
<td>up</td>
<td>1.52</td>
</tr>
<tr>
<td>11-3461.12:3686.4</td>
<td>2038.88 5500 9186.4</td>
<td>3982 9482 2</td>
<td>up</td>
<td>1.51</td>
</tr>
<tr>
<td>12-2283.52:2048</td>
<td>-5168.52 -2885 -837</td>
<td>4528 1643 2</td>
<td>down</td>
<td>1.51</td>
</tr>
<tr>
<td>13-8448/8704</td>
<td>10789 19237 27941</td>
<td>21540 40777 2</td>
<td>up</td>
<td>1.5</td>
</tr>
<tr>
<td>14-2754.56:3368.96</td>
<td>765.44 3520 6888.96</td>
<td>1555 5075 2</td>
<td>up</td>
<td>1.49</td>
</tr>
<tr>
<td>15-1771.52:1986.56</td>
<td>438.48 2210 4196.56</td>
<td>914 3124 2</td>
<td>up</td>
<td>1.48</td>
</tr>
<tr>
<td>16-6082.56:5898.94</td>
<td>5740.44 11823 17721.2</td>
<td>12046 23689 2</td>
<td>up</td>
<td>1.48</td>
</tr>
<tr>
<td>17-2078.72:2211.84</td>
<td>-4762.72 -2684 -472.16</td>
<td>3708 1024 2</td>
<td>down</td>
<td>1.46</td>
</tr>
<tr>
<td>18-2119.68:2037.76</td>
<td>-4797.68 -2668 -630.24</td>
<td>4444 1376 2</td>
<td>up</td>
<td>1.46</td>
</tr>
<tr>
<td>19-1781.76:1792</td>
<td>334.24 2096 3888</td>
<td>688 2784 2</td>
<td>up</td>
<td>1.46</td>
</tr>
<tr>
<td>20-3932.16:4259.84</td>
<td>2675.84 6608 10867.8</td>
<td>5984 12592 2</td>
<td>up</td>
<td>1.45</td>
</tr>
<tr>
<td>21-10455:10915.8</td>
<td>-36683 -26228 -15312.2</td>
<td>85832 59604 2</td>
<td>down</td>
<td>1.26</td>
</tr>
<tr>
<td>22-7700.48:7782.4</td>
<td>5041.52 12742 20524.4</td>
<td>20556 33298 2</td>
<td>up</td>
<td>1.25</td>
</tr>
<tr>
<td>23-2140.16:2273.28</td>
<td>320.84 2461 4734.28</td>
<td>1321 3782 2</td>
<td>up</td>
<td>1.24</td>
</tr>
<tr>
<td>24-2621.44:2979.84</td>
<td>-6161.44 -3540 -560.16</td>
<td>5883 2343 2</td>
<td>down</td>
<td>1.24</td>
</tr>
<tr>
<td>25-3450.88:3952.64</td>
<td>-8665.88 -5215 -1262.36</td>
<td>10529 5314 2</td>
<td>down</td>
<td>1.24</td>
</tr>
<tr>
<td>26-2232.32:2600.96</td>
<td>-5150.32 -2918 -317.04</td>
<td>4264 1346 4</td>
<td>down</td>
<td>1.24</td>
</tr>
<tr>
<td>27-2181.2:2099.2</td>
<td>202.88 2384 4483.2</td>
<td>867 3251 2</td>
<td>up</td>
<td>1.23</td>
</tr>
<tr>
<td>28-3758.08:3768.32</td>
<td>1212.92 4971 8739.32</td>
<td>5296 10267 2</td>
<td>up</td>
<td>1.23</td>
</tr>
<tr>
<td>29-4925.44:5857.28</td>
<td>2662.56 7608 13465.3</td>
<td>11941 19549 2</td>
<td>up</td>
<td>1.22</td>
</tr>
<tr>
<td>30-4246.88:2887.68</td>
<td>418.12 2845 5732.68</td>
<td>1909 4754 2</td>
<td>up</td>
<td>1.22</td>
</tr>
<tr>
<td>31-5980.16:5867.52</td>
<td>-14564.2 -8584 -2716.48</td>
<td>20997 12413 2</td>
<td>down</td>
<td>1.22</td>
</tr>
<tr>
<td>32-4423.68:4966.4</td>
<td>-11228.7 -6805 -1838.6</td>
<td>15221 8416 4</td>
<td>down</td>
<td>1.22</td>
</tr>
<tr>
<td>33-1771.52:1484.84</td>
<td>-3399.52 -1628 -143.2</td>
<td>2307 679 2</td>
<td>down</td>
<td>1.21</td>
</tr>
<tr>
<td>34-3491.84:3481.6</td>
<td>331.16 3823 7304.6</td>
<td>5513 9336 4</td>
<td>up</td>
<td>1.06</td>
</tr>
</tbody>
</table>

Table 2: Gene regulation induced by MK5 activation. Each regulation is listed as a term with a confidence interval covering 95% of the real values. Gene regulation is calculated as the mean of all the measured oligosequences/probes. The reported confidence interval is the result of a convolution of the respective error distributions. The yellow row is explained in detail in the text.

When a consensus on the regulation exists (lowest boundary and highest boundary have the same sign), we can calculate the regulation ratios by assuming that either red or green could have been fully
responsible for the measurement error. In such extreme cases the highest ratio can have a value of $\infty$.

2.4 Confidence Intervals on Multiple Measurements

When multiple measurements are available, we can make the final confidence intervals smaller by convolving their respective probability functions. Section 7.4 covers the details. Table 2 illustrates the combination of oligosequences belonging to the same gene and consequently reports smaller confidence intervals.

As an illustrative example of the advantage of combining the different probability distributions we investigate gene \#34 (Table 2). The microarray measures this gene using two distinct probes, labeled Rn30006190 and Rn30021393. On slide 1, Rn30006190 has an upregulation in the range $[-455 : 2504]$ (measured as 999). On slide 2, it has an upregulation in the range $[-256, 675]$ (measured as 184). On slide 1, Rn30021393 has an upregulation in the range $[-815 : 3106]$ (measured as 1017). On slide 2, it has an upregulation in the range $[-1080 : 4131]$ (measured as 1623). None of these individual measurements can tell us something about the gene regulation since they all could have been downregulated as well. However, by combining their error distributions we are able to report that the overall gene is upregulated with at least a 6% increase and at most a 4.6 times increase (last row of Table 2).

3 Validation

We validated our method by means of qPCR and by comparing it to standard analysis protocols. For MK5 this analysis was performed at the Microarray facility in Tromsø. For the FKRP and TAF4 experiments, this analysis was performed by UNIGEN (Trondheim).

3.1 Quantitative PCR

To validate the regulations we found in the TAF4 experiment, we selected 22 genes and monitored their transcript levels by quantitative PCR (qPCR). Such qPCR results should be treated with caution. First, it is an inherent different measurement technique and thus it is unexpected that the results will completely fall within the reported confidence intervals. Secondly, the quantitative PCR experiment is often based on a new batch of cells, which means that the transfection efficiency can be different, and thus the actual results as produced in the qPCR can be a ratio higher or lower. A new batch was used for the TAF4 HeLa cells. The SK-N-DZ cells were based on the same batch. To account for the transfection efficiency, we performed a least square fit of the qPCR results to the microarray results. Thirdly, the primer sequences can be slightly different leading to different measurement efficiencies. Fourth, the housekeeping gene used in the qPCR experiment can be indirectly linked with the genes we measure, leading to a gene specific bias. And as a last remark, since we do not have an error model of the qPCR measurements, the dynamic range of the housekeeping gene might put a limitation on the qPCR accuracy. Notwithstanding these considerations, we performed 22 qPCR experiments, which confirmed that our technique is a valuable analysis method. Table 3 summarizes the results.
Table 3: Quantitative PCR analysis to verify differentially expressed genes. A number of the genes that were reported to be expressed differentially by the microarray analysis were measured using quantitative PCR.

From the 22 measurements, 3 were not used because we could doubt both the PCR and microarray results. In particular, a number of qPCR measurements could be considered up or downregulated depending on the analysis process followed (e.g., mean of ratios versus ratio of means). From the 19 remaining genes, 12 were fully correct, that is, the qPCR results fell within the reported confidence interval. For 2 genes, the predicted upperbound was too low. For 3 genes, the microarray reported strong regulations, however the qPCR measurement was unable to measure the exact value because the CP values were too large. For these genes it is very likely that the microarray reported correct. One gene did not match between both experiments. And for 1 gene the microarray experiments reported a confidence interval that was substantially larger than the qPCR value.

In the strictest sense (upperbounds and lowerbounds match), our method was able to match 79% of the qPCR results. If one is satisfied with proper lower bounds, then 89% of the results were reported accurately.

3.2 FKRP and TAF4

Next to the qPCR validation, we compared our method to a blind analysis by other groups. The blind analysis for the FKRP and TAF4 experiments followed the guidelines of [ACPS06]. The PCA analysis revealed no outlier for any of the slides. The analysts attempted to gage the genetic variations (abbreviated: genvar) between the different slides and then report those that changed significantly. For the TAF4 HeLa cells experiment, the genvar error model reduced the dataset to 70 significant genes, while the intensity dependent analysis (abbreviated: indep) retained 2497 genes\(^2\). Five genes were only reported in the genvar set. Those 5 were all below the average gene intensity and the mismatch may be due to the normalization differences (quantile vs Applied Biosystems) or microarray outliers. We would liked to

\(^2\)The TAF4 SK-N-DZ was not sent for analysis, but to be complete, we found 661 to be significant.
have validated those 5 mismatches through qPCR, but no probe sequences, nor gene annotations were available, so we could not verify them. The previous 22 qPCR measurements did however include 3 genes that were reported in the genvar analysis. Two of these produced qPCR values with large CP values (thus with a high error rate), thereby offering little extra information. For the FKRP experiment there were no significant alterations which was, according to the report, due to the few samples we provided (4 replicas vs 3 replicas). The indep analysis reported 2977 regulations for the siRNA#1 group and 576 regulations for the siRNA#2 group.

Compared to a standard analysis, our method reported more genes. In the TAF4 experiment, we found 35x more genes than the standard analysis. Most of these genes could be validated with qPCR, leading to the conclusion that standard analysis methods may be too stringent.

3.3 MK5

The standard microarray analysis, based on loess normalization [CGS92, SS03], contained 27648 spots for each slide, of which 4007 pairs in agreement (both slides reporting the same qualitative regulation, being up or down). Based on both slides, our method only reported 1422 spots. Three hundred and eleven spots occurred in both methods, 1111 spots were unique to our analysis and 3696 spots were unique to the standard analysis.

Figure 3: Plots illustrating the difference between standard filtered results (based on loess normalization and a consensus for both slides) and the filtering based on the confidence intervals for the MK5 experiment. A) the red spots are reported by the standard method but no longer by the confidence interval method. The green spots are the control slide, illustrating the large variance of the measurement. All spots omitted in the confidence interval method were too close to the measurement error to be useful. B) The red spots are those reported in the confidence interval method but not in the standard analysis. The green spots again represent the control slide.

To better understand the differences in reported genes, it is helpful to include a picture (Figure 3) that illustrates both the variance on the measurements and the samples we removed/retained.

The first consideration regards spots that occurs in the loess set but not in our analysis. Is there a good reason why we should not take those particular data points into account? Figure 3A illustrates the spots that only occurred in the loess set (red) as well as the variance of the experiment (green). Clearly, the omitted spots were too close within the expected variance to be useful.

The second concern regards those spots that only occurred in our analysis. These are pictured in Figure 3B. The main reason why our method was more sensitive and could report them lies in the convolution of the error distributions of similar spots. This information was unavailable to the loess method since there we were forced to stick to a more rigid approach that both slides agreed qualitatively.

The last concern regards overlapping spots. All of them should report at least the same qualitative regulation. From the 311 spots, 10 failed to do so. Looking at the non-normalized data (Table 4) we find that all spots were correctly reported by the confidence interval method. The reason why the loess method failed, probably lies in the model fitting that will inevitable position certain spots at the wrong side of the zero-line (a ratio of 2 is after all closely located to zero when expressed as a \log_{10} ratio).
Table 4: Wrongly reported datapoints in the loess normalized data. We compared the regulations of our method to a standard loess normalization and found 10 spots for which the two methods disagreed qualitatively. Each case contains the data as found on the non-normalized microarray (reported in the two first green/red columns). The reported log ratio after loess normalization is given in the second row of each case. The reported confidence interval is presented in the first row of each case.

4 Discussion
Our method was validated using qPCR and we found that it reports useful confidence intervals (79% correct, 89% when omitting the upper limit). We also found that the method surpasses standard methods in the number of genes it reports (x35 in our case).

4.1 Difference between machines, cell lines and experiments
The sampling of the error distribution is specific to the gain of the acquisition hardware, the biological sample, the slide quality, slide facturer, supplier of the microarray hardware, temperature, sample handling and probably many more influences. Therefore, the error model must be developed for each specific experiment. This is illustrated in Figure 2, which visualizes the difference between a number of these variables.

1. We illustrated the technique on a knockdown of a gene as well as on a constitutive active gene. Figures 2A & B are the constitutive active MK5. Figures 2C, D, E & F are those with a knockdown of a gene. These figures also illustrate the technique on two different scanners. Figures 2A & B are made on a Tecan scanner with Cy5/Cy3 labeling. All others are made with DIG labeled slides scanned on an Applied Biosystems 1700 scanner.

2. Figures 2G, H & I versus Figures 2C, D, E & F illustrate the differences between scrambled siRNA and specific siRNA. The results show that scrambled siRNA introduces more variability in the cell system than previously anticipated. This might suggest that a scrambled siRNA alone as a negative control might not be sufficient, or will in a sense, reduce the number of useful results that can be obtained from this type of experiment.

3. We illustrated the technique on the same experiment, but with different cell types. Figures 2C, G are performed in HeLa cells, while Figure 2E, I plots the data from SK-N-DZ cells. Compared to the FKRP experiments, they reach their maximum variability point at lower intensities. Between the two different cell types we find that the SK-N-DZ cells reached their maximum variability point also at lower intensities.
4. Figure 2D plots siRNA#1 while Figure 2F plots the siRNA#2, which target slightly different FKRP mRNA. The small variations in Figure 2F might suggest that we would obtain more data from this experiment. This however is incorrect. For siRNA#2 we only obtained 576 valuable genes, while the siRNA#1 group produced 2977 genes. This probably happened due to either a bad transfection efficiency (leading to low variations, but also to little useful data) or a low siRNA#2 impact in general. This illustrates that the size of the error as such does not provide much information, it must always be related to the impact of the cell alteration itself.

5. Figures 2D, F, H are mouse survey gene arrays, while Figures 2C, E, G, I are human genome survey arrays. We find little overall impact of the type of array in the shape of the error plots.

6. Figure 2A is made using Cy5/Cy3 labeling without normalization. Figure 2B is the same figure but relying on quantile normalization. Figure 2C-I are based on the applied biosystem inter array normalization algorithm. The differences in confidence intervals between Figure 2A and Figure 2B illustrates how our algorithm can model the inter-filter effect [Kub94]. Instead of having a flat ‘eye-shaped’ error model (Figure 2B), one finds back a banana-shaped error model. This means that the model is independent from a particular normalization to account for light reabsorption. Using confidence intervals, there is no particular need to perform separate dye specific normalizations.

Looking at these observations, we see that the machine fabricant and normalization algorithm have a major impact on the shape of the error plots. The type of cell perturbation, in our case, is a second major factor (scrambled siRNA vs specific siRNA). The specific cell lines (HeLa vs SK-N-DZ), actual genes (TAF4 vs FKRP) and type of microarray (mouse versus human) have a lesser impact on the overall shape of the error plot.

4.2 Optimal areas of measurement

Looking at the results (Figure 2 and 3B), our observations do not support the general believe that 'bright spots are good spots'. Actually, we find that intense spots are subject too much larger errors. Therefore we might wonder whether there are measurement areas that produce the most information. In our MK5 error model we find that the bright spots are the ones that should be removed from the data set since they are too close to the expected error, while the darker spots often fall outside the measurement error (see Figure 3A). Figure 3B illustrates this further: contrary to what one would expect we find the largest collection of useful spots at the edges around the origin.

4.3 Amplification errors seem to outweigh genetic variability

Given the considerations these days on genetic pathways and genetic variability, we now discuss how these two factors influence our analysis method. The first concern is that certain genes have a larger natural variability (unstable expressed genes) than other, more stably expressed, genes. Since our method does not assess genetic variability, it might omit significant changes in stable expressed genes if they are too close to each other. It might also report highly unstable expressed genes as significantly altered while, in reality, they might just have fallen outside the confidence interval by chance. While there may be such genes, our initial observations does not seem to be influenced by it. Our PCR results confirm our confidence intervals, which seems to indicate that the impact of genetic variability is much lower than anticipated. Instead we find that the experimental variability, cell perturbation and consequent amplification/propagation cascades outweighs natural genetic variability.

The second concern addresses genetic pathways: the gene expression pattern in a cell is the result of a cascade event, where products of primary gene transcripts can affect the expression of other genes. Of course, when measuring the same samples, one still expects to find the same values (eg. in Figure 1, regardless of the gene linking, the control should be a straight line). However, if an error or a variability occurs in the initial perturbation, then it is not unexpected that this error will propagate along the same pathways. This effectively leads to a cascade of expression patterns, in which every step can reduce or increase the net output effect. In other words, the amount of transcribed gene can be dependent on the amount of transcripts of linked genes, but multiplied with an unknown factor. Very seldom will we find that one expression pattern produces a new expression pattern with exactly the same amount of transcripts. So, by pooling together a random set of transcripts based on their intensity, we substantially limit the impact of genetic pathways. In the worst case scenario, if there were a significant collection of dependent transcripts, all with the same expression levels, then they would be placed in the same intensity-slice, thereby sharpening the probability distribution on that slice. This would in turn lead to
a list of genes that could contain non-significantly altered gene expressions. In our work, we did not find much evidence that our intensity-based pooling is inadequate and/or overly sensitive to genetic pathways. The entire collection of probability distributions was in all our experiments smooth without outliers.

4.4 Lorentz distributions

We believe that the presented method makes a fair trade off between a full understanding the gene linkages/variations (which is something we cannot measure with 3 or 4 slides) and error models that do not take such possibility into account at all. Standard microarray error models are often based on the log-scale of the two channels (red/green or slide1/slide2) [BWWQ02, HvHV04]. The resulting distributions appear as a Lorentz distribution [PTVF03, BWWQ02]. However, such distributions cannot capture relative errors in the experimental process. This leads to standard error models that are too wide for low intensity spots and too small for high intensity spots.

4.5 Gating

Aside from the advantages listed above we also found an interesting side observations, which was a form of gating on the Tecan scanner. Figure 4 plots the one dimensional distribution of all intensities, and one would expect either a Lorentz distribution [PTVF03] or a normal distribution, instead we find something in between that has a plateau around zero (marked with a red circle).

![Figure 4: Univariate probability distribution of the spot values on the Tecan scanned slides (MK5). Red is the first slide, green is the second slide and blue is the control slide. The plateau around 0 is currently unexplained. It might be due to a form of gating in the electronics of the acquisition hardware. It might also be related to a chemical critical mass.](image)

We marked the plateau with a red circle (See Figure). At this point, we have merely been speculating about an explanation for this local uniformity

1. The plateau is not related to an error in the background subtraction because that would widen the entire probability distribution.
2. A hybridization problem might have occurred. This will place many dots around 0. This however is not consistent with the scatterplot, which does not hint at such a large non-hybridization rate. Since all microarrays had a similar distribution, this becomes very unlikely.

3. The microarray age might be an explanation, but this should not have occurred since we bought them just before the experiment.

4. The electronics of the microarray scanner might be subject to a form of gating [SN06]. This will produce random results for a signal until the signal is strong enough to be picked up properly. Because we did not see the same plateau at low intensities, this might hold some ground.

5. Highly speculative is a chemical critical mass of sorts that will randomly fluctuate unless there is enough material to produce a stronger signal.

6. A systematic production error on the microarray slides, but this is difficult to verify without close cooperation with the slide fabricator.

7. It might be a specific feature of the MK5 cell system, with a large collection of genes only marginally expressed.

Deconvolution of error distributions  Regarding future work, we might improve the method through deconvolution of the DIG labeled error distributions. When acquiring the error model based on the differences between replica slides, one actually measures the auto-convolved error distribution. As such, it will be slightly larger than the real error distribution. This can be improved through deconvolution techniques such as adaptations to the Richardson-Lucy algorithm [RLAA93], but in general seems unnecessary.

5  Conclusion

We presented a method to analyze differences between groups of microarrays, such as often found in differential gene expression experiments. Instead of reporting one single number for each regulation, we report the regulation including its confidence interval. The confidence interval is obtained from an error model that must be measured within the experiment itself.

We compared our method to a standard analysis method and illustrated its capability to filter out spots that are too close to the error to be useful. For indicative purposes we compared the reported results to standard analysis methods. We also performed a limited qPCR experiment. Although a relative small number of samples have been investigated, they support the credibility of our analysis method.

6  Material and Methods

Manufacturers instruction are used unless stated otherwise.

6.1  Constitutive active MK5 cell-line

To clone the cDNA sequence of MK5, we introduced two mutations in the pcDNA-HA-MK5WT plasmid [SJH+02]. Both used the Stratagene mutagenesis kit. The first mutation assured compatibility with the pTRE2 plasmid and used a forward primer 5'-CCC-AAG-CTT-GAC-GCG-TCC-ATG-TAT-GAT-G-3' with complementary reversed primer. The second mutation turned the wt MK5 into a constitutive active MK5L337A mutant. The resulting MK5 cDNA sequences were excised by MluI/NotI digestion and cloned into the corresponding sites of pTRE2. We verified the plasmid by sequencing. Two 6-well plates with 5.10^5 PC12 TetOff cells (BD Biosciences) were transfected with 14 µg of pTRE2-MK5L337A and 2 µg pTKHyg per well using lipofectamine 2000 (Invitrogen) [PBB+02]. After 3.5h, the medium was changed and supplemented with 10ng/ml Doxycycline (Sigma). 24h after transfection, cells were transferred to 10 cm dishes with fresh medium and Doxycycline. 48h after transfection, 100 µg/ml of Geneticin (Gibco) and 200 µg/ml Hygromycin B (Invitrogen) was supplied additionally to the medium. The cells were grown until visible colonies of resistant cells could be detected. From each plate two colonies were transferred in threefold dilution to a 96 well plate. For positive clones, we confirmed the transgene expression though reverse transcriptase-PCR and western blot. Cells were maintained in DMEM supplied with 10% horse serum and 5% fetal bovine serum, 2mM L-glutamine, penicillin (110 units/ml) and streptomycin (100µg/ml). Additionally, 50µg/ml of Geneticin, 100µg/ml Hygromycin B were supplied to
maintain selection. To suppress HA-MK5_{L.337A} expression during ordinary cell culture, we added 10ng/ml Doxycycline.

6.2 TAF4/FKRP knock-down using siRNAs

SiRNAs introduced into the cells lead to degradation of mRNA having the complementary sequence, thereby silencing/depressing gene expression. SiRNAs were pre-designed and ordered from Qiagen (http://www.qiagen.com/). For the FKRP experiment, the siRNAs sequences targeted AACCTCC-TAGTCTTCTTCTAT; AACCCAAAGACTGGAGCAACT. For the TAF4 experiments, the siRNA targeted AAGGCCTGTGGATACTCTTAA. Cells were plated at 10^6 cells/ml into a 6-well dish. Because of different growth-rates, HeLa and C2C12 cells were transfected after 24 hours, while SK-N-DZ cells were transfected after more than 48 hours. Two different transfection mixes were made. Both included 90 vol% D-MEM(SBS). The first transfection mix contained 10 vol% TAF4 siRNA (30nM siRNA/well). The second transfection mix contained 10 vol% scrambled siRNA. The different mixes were vortexed, 7.5 µl RNAiFect was added and then incubated for 15 minutes (room temperature). D-MEM was aspirated from the wells. Subsequently, 100µl of the transfection mixture was added to each well in addition to 1.9 ml fresh D-MEM (10% FBS + antibiotics). We produced each transfection mix in triplicate. Twenty-four hours after transfection, RNA was to be extracted for further analysis. The same procedure was followed in the FKRP knockdown experiments.

6.3 RNA extraction and cDNA Synthesis

C2C12 (FKRP), HeLa (TAF4) and SK-N-DZ (TAF4) cells were plated at 2.10^5 cells per well in a 6 well dish; MK5 stable cells at 5.10^5 cells per 6 well dish. For the TAF4 and FKRP experiment, cells were lysed by incubation in lysis buffer containing chaotropic salt and Proteinase K, after which RNA was isolated with the MagNA Pure Compact RNA system (Roche-Applied-Science). For the MK5 experiment, we used the Nucleospin II RNA isolation kit (Machery-Nigel). The Nanodrop ND-1000 (Nanodrop technologies Inc.) verified RNA concentrations and purity. One µg of RNA was reverse transcribed to cDNA using the iScript cDNA synthesis kit (Biorad) (MK5) and SuperScript™II from Invitrogen™ (remaining experiments).

6.4 Quantitative Realtime PCR TAF4 related genes

We made 4 cDNA dilutions: 1:2, 1:5, 1:10 and 1:50. All were supplemented with mastermix, primers, probe and water. Relative expression for each target gene was normalized to GAPDH using the 2^-dC_T method [LS01]. The expression differences between scrambled and normal siRNA were calculated by dividing the averages of each cell type. The qPCR experiments were performed on LightCycler 480 (Roche), with accompanying software version 1.2.0.0625.

6.5 Microarray

The number of slides and their layout is provided in Table 1. For the MK5 experiment, we made 3 slides, each containing an induced (Cy3) and uninduced sample (Cy5). The 4th slide contained two induced samples. Samples were labeled with the 3DNA 350S HS labeling kit (Genisphere). Hybridized slides were scanned using the Genepix 4000B (Molecular Devices) with a constant gain of 950/800. We obtained more than 70% hybridization (measured as #spots > median + 1SD). Spots with too large an intensity (> 90% of the maximum) or too large a regulation (> x10) were removed. For standard analysis, we relied upon a blind analysis of the microarray facility in Tromso, which used loess normalization [CGS92]. Our own analysis used quantile normalization [DYCS00]. For the FKR & TAF4 experiments, we used an Applied Biosystems 1700 scanner, with AB. v2.0 slides surveying respectively the mouse genome and human genome. UNIGEN in Trondheim performed a blind data analysis following the guidelines of [ACPS06]. This included quantile normalization on the raw machine output. Our analysis was based on the already normalized output of the Applied Biosystems scanner.
7 Detailed Analysis Method

7.1 Notation

We denote every slide with a number which is placed top-right. The control slide is marked with a $c$. In the bottom-right we refer to either the red or green channel. Eg $d_i^r$ refers to the red channel of spot $d$ in slide $i$. Each channel must be measured, with or without quantile normalization, but always without taking the logarithm. The maximum measurable value is expressed as $C$, which typically is 65535 (this is the maximum value that can be expressed using 16 bits). The dataset is preferably already filtered for false positives. The norm of a spot $d$ is written as $|d| := \frac{d_r + d_g}{2}$.

The difference between the two channels is subscried with a $\delta$ subscript. Eg $d_\delta = d_r - d_g$.

7.2 Creating Histograms

We model the error distributions as a collection of histograms in function of spot intensity. We rely upon $s_x$ bins, each in which we store a histogram. We denote $h_x$ the histogram for bin $x$. It will cover all the spots within intensity range $[\frac{x C}{s_x}, \frac{x+1 C}{s_x}]$. The histogram $h_x$ counts the occurrences of a specific intensity. Using $2 s_y$ bins, $h_{x,y}$ will cover all the spots for which the difference lies within $[\frac{y C}{s_y}, \frac{y+1 C}{s_y}]$. The creation of these histograms obviously starts with each $h_{x,y} = 0$. The algorithm below calculates the 2 dimensional histogram.

```plaintext
foreach spot $d$
  $x := \lfloor |d| s_x \rfloor$
  $y := \lfloor d_\delta s_y \rfloor$
  $h_{x,y} := h_{x,y} + 1$
```

7.3 Smoothing

After performing this process we smoothen out the distribution along the intensity axis. This ensures that each histogram contains a minimum amount of measurement-error measurements. The smoothing is performed adaptively by widening a window around each intensity until enough points are gathered. If we call $s_p$ the minimum mass of each histogram, then the algorithm below will create a smoothed collection of probability distributions and store it in $g$.

```plaintext
foreach intensity $X$
  $w := 0$
  do
    $g_X := \sum_{x=X-w}^{X+w} h_x$
    $w := w + 1$
  while $\sum g_X < s_p$
  $g_X := \frac{g_X}{s_p}$
```

In the above, the total mass of a histogram is written as $\sum h$. The addition of histograms is the same as the addition of the counts in each bin. If $a$ and $b$ are two histograms then $c = a + b$ $\iff$ $c_i = a_i + b_i$. We use similar notation for division.

7.4 Multiple Measurements

Assume that we have a set of spots $M$, all measuring the same process (eg the same oligosequence, or the same gene), then we can define the overall measurement $m$ as $m_r = \sum_{d \in M} d_r$ and $m_g = \sum_{d \in M} d_g$. Then we also have that $m_\delta = \sum_{d \in M} d_\delta$.

The error distribution associated with a specific spot is written as $\tilde{d}$.
For each value of $d$, we have an associated error distribution. The overall error distribution for $m$ will consequently be the convolution of the underlying error distributions (written as $\ast$).

$$\tilde{m} = \ast \tilde{d}$$

### 7.5 Confidence Intervals

The confidence interval of $\kappa$ associated with $m$, given the error distribution $\tilde{m}$ is given by

$$\left[ \text{CDF}^{-1}_{\tilde{m}}\left(1 - \frac{\kappa}{2}\right), \text{CDF}^{-1}_{\tilde{m}}\left(\frac{\kappa + 1}{2}\right) \right]$$

$m_l$ and $m_h$ are the lowest and highest boundaries for measurement $m$.

### 7.6 Regulation Factors

Converting absolute regulation differences to regulation ratios requires that we assume that either $m_r$ or $m_g$ could have been fully responsible for the measurement error. This leads to the following possible regulation ratios:

$$f_1 = \text{if } m_g - m_l < 0 \text{ then } \infty \text{ else } \frac{m_g - m_l}{m_g}$$

$$f_2 = \text{if } m_g - m_h < 0 \text{ then } \infty \text{ else } \frac{m_g - m_h}{m_g}$$

$$f_3 = \text{if } m_r + m_l < 0 \text{ then } \infty \text{ else } m_r + m_l$$

$$f_4 = \text{if } m_r + m_h < 0 \text{ then } \infty \text{ else } m_r + m_h$$

$\min\{f_1, f_2, f_3, f_4\}$ reports the lowest possible regulation ratio. $\max\{f_1, f_2, f_3, f_4\}$ reports the highest possible regulation ratio.

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### 9 Authors Contributions

Werner Van Belle invented and implemented the presented technique and wrote the manuscript. Nancy Gerits created the constitutive active MK5 cell line, designed and performed the MK5 experiments and helped writing the manuscript. Kirsti Jakobsen performed the TAF4 experiments, performed the qPCR experiments and provided substantial input in the manuscript. Vigdis Brox performed the FKRP experiments. Marijke Van Ghelu designed the TAF4 and FKRP study and helped writing the manuscript. Ugo Moens designed the MK5 experiment, helped designing the TAF4 experiment and helped writing the manuscript.
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