Master of Science

Re-design of a multipurpose snowmobile sled for Norwegian volunteer (SAR organizations).

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Abstract
This master thesis is written for the Norwegian volunteer organization “Hjelpekorpset” that is a search and rescue organization. The organization performs different kinds of activities in addition to rescue missions. During wintertime, they transport materials, furniture and other cargo to local huts to raise funds. This is the basis for the thesis, where the aim was to redesign a multipurpose snowmobile sled for both rescue missions and transportations jobs. Problem areas have been the towbar and the general design in terms of securing both stretchers and cargo.

The towbar have been reinforced by simplifying the design using fewer components and installing hingejoints in the transmission to the sled. Material selection was executed for the towbar rods and the top plate. This resulted in Aluminium alloy Al 6061 on the towbar, that was applied on the supporting bod structure and the railings as well. On the top plate, Plywood was determined to be the best choice of material. After conducting Finite Element Analysis on the system, the attachment ring is performed in a different, stronger material than the rest of the towbar; Titanium Alloy Ti-6Al-2Sn-2Zr-2Mo-2Cr.

The design of the railings were altered so that they covers the two longitudinal sides, making it more convenient to secure a stretcher on the sled. A frame was designed that can be attached when needed to make it easier to transport cargo on the sled.

Objectives have been to strengthen the towbar and keeping the mass below 50 kg. This have been achieved with a thorough design process ending up on a final weight of the sled of 41.85 kg. Aesthetics of the design was examined by 3D printing a miniature prototype of the sled.

The final design of the snowmobile sled. Model drawn in SolidWorks
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1 Introduction
The aim of the project is to optimize the design for a multipurpose snowmobile sled that should be used both for transporting cargo and for rescue missions in difficult terrain. A preliminary project is performed which studied the existing snowmobile sleds on the market, and transformed the problem from the customer to specifications for the product. This lays the basis for the project where the design will be developed for an improved snowmobile sled.

The thesis is the final part of the Master of Science and will provide 30 student points and a diploma in Engineering Design. The formal date for delivery of the thesis is 6th of June 2017.

1.1 Background
In Norway, the need for volunteer organizations are different from countries where there is war or natural disasters. The organizations exists here as well, but their chores are drug-related, integrating new citizens, helping lonely souls or rescue operations in mountains when someone is lost or injured. In order for rescue operations in the mountains to be successful, it is crucial that the volunteers have the proper equipment. One of the main challenges they face is search and rescue in arctic environments. This includes winter climate when the mountains are covered in snow, ice and cold. Most of rescue operations during these conditions are proceeded by using snowmobiles with sleds that can reach almost anywhere.

The Norwegian Search and Rescue organizations (SAR) are mainly based on volunteer work (Hjelpekorpset is one of them). Some financing comes from the government but most of the financing the local SAR groups need to raise by them self. One way of raising funds is by doing transportation work by snowmobiles. Thus, there is a need for multipurpose sleds that can be used for all of the different operations/ work Hjelpekorpset do during the winter.

1.2 Problem Description
The sleds that exist today often have very specified area of application, there is a need for a sled that can be used for all operations/ transport missions that the Norwegian volunteer SAR organizations carries out. The sled must be reliable and easy to maneuver in difficult terrain. Area of application for the sled:
- Transport of various equipment for use during SAR-operation
- Transport of patients.
- General transportation of; firewood, gas, gasoline, furniture etc. (the volunteer SAR organizations in Norway often do transportation work to private huts etc.)

Hjelpekorpset are well experienced with snowmobile sleds used for rescue missions as well as transportation purposes. The specified problem-area is the transmission from the towbar to the sled itself, where there are weaknesses in the rods and bolts that need to be addressed. The complete problem description is presented in Appendix A.

1.3 Method
The design itself will be a product of the method described by Nigel Cross in his text course book “Engineering Design Methods” that have been frequently used in courses during the master program. This method consists of eight steps and is a guide to assure that the designer do not loose sight of the original demand during the process. For the material selections of the design, the method presented by Michael F. Ashby in his book “Materials Selection in Mechanical Design” and the program CES EduPack 2016 is used to ensure that the selection is as precise as possible.

When the design and materials are chosen, analyses will be performed on the object to make sure it will meet the demands and requirements set in the beginning of the project. If the design object do not pass this stage, it might be necessary to reconsider the design before prototyping it and performing numerical analysis.

The design will be divided into separate parts to make a systematic progress. System boundaries are set only around the sled itself, and no surrounding factors or organisms will affect it. The different parts are illustrated Figure 1-1 and the part of the report regarding the design will be divided into:
1. Railings
2. Top plate
3. Towbar
4. Skis
5. Supporting body structure

Figure 1-1: Sled divided into several parts for a systematic design process. Drawn in INKSCAPE 0.91.

2 The Design Process
As stated, the design process consists of eight steps from an idea or demand arises to a finished product. In order to design a product that is safe, reliable and satisfactory otherwise it is necessary to examine the demands for the design. This is performed regarding both physical conditions and what demands or wishes Hjelpekorpset have to determine the specifications.

2.1 Objectives
To clarify the objectives the information from the customer is crucial. Since the sled is intended for transportation of equipment and patients, it have to be able to fit large capacities in an effective way. It have to carry weight while driving in difficult and bumpy terrain where especially the attachment system from the snowmobile to the sled is an area of problems. The sled has to be stable and comfortable for injured patients in all kinds of snow and terrains. Both equipment and patients have to be easy to attach and release in a secure and simple matter. In order to organize the information given by the customer, Cross’ objective tree method is utilized, as shown in Figure 2-1.
### 2.2 Physical Requirements

A snowmobile sled is intended for outdoor use, and will be exposed to climate and weather changes. The sled is used during wintertime in low temperatures, on snow. During spring, summer and fall it is usually stored in a storage. The materials the sled is constructed of therefore have to be able to withstand both low temperatures during winter and higher temperatures during summer storage. The climatic requirements are:

- Winter, temperatures down to -50°C
- Summer storage, temperatures up to 40°C
- Ice, rain, sun

The sled is to be used both in Narvik and in the surrounding areas and are therefore often transported by car or train to the mountains. In order to manage this the persons handling the sled have to drag or carry the sled onto the transportation. The weight of the sled cannot exceed a weight that an average grown person can lift up. Based on an assumption that the persons involved in the rescue missions or other transport missions are in good physical health the limit for the total mass of the sled is set to 50 kg.

Since this is a sled for rescue operations and transportation of cargo, the design have to take into consideration the mass of load it will be carrying. In a rescue situation the sled have to withstand the mass of two or three persons including the patient and rescue team, assuming there is no more than one person in need of rescuing. The average weight of men of military age in Norway in 2010 were 76 kg (1). In addition to the persons, they might carry some equipment or heavy backpacks that have to be transported as well. Based on this the sled have to be designed to withstand a load of at least 200 kg, and not dimensioned for more than 300 kg.

Additionally, the sled have to be long enough to transport a grown man without any problems. The average length of Norwegian men of military age in 2012 were about 1800 mm (2). If the cargo is longer than the sled this might cause problems in maneuvering the sled and the risk of the cargo falling off is greater. During a rescue operation, the patient will be attached to a stretcher that is stiff, and thus have support beyond the boundaries of the sled.
In Table 2-1, the physical requirements for the sled are summed up given a range on most values where the final decision depends on the final design attributes and how the sled will work.

<table>
<thead>
<tr>
<th>Requirement</th>
<th>Minimum</th>
<th>Maximum</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weight of sled</td>
<td>-</td>
<td>50 kg</td>
</tr>
<tr>
<td>Load weight</td>
<td>200 kg</td>
<td>300 kg</td>
</tr>
<tr>
<td>Length (top plate)</td>
<td>1600 mm</td>
<td>2200 mm</td>
</tr>
<tr>
<td>Load length</td>
<td>-</td>
<td>15-30% of final Design length</td>
</tr>
<tr>
<td>Width</td>
<td>900 mm</td>
<td>1000 mm</td>
</tr>
<tr>
<td>Temperature</td>
<td>-50°C</td>
<td>40°C</td>
</tr>
</tbody>
</table>

### 2.3 Determining Characteristics

To determine the importance of the engineering characteristics of the product it is necessary to get overview of the relations between the customers’ demands and the specifications of the product. This is obtained by using the “Quality Function Deployment Analysis” (QFDA) (Cross, 2008). The method results in a “House of Quality” (HOQ) where the specifications are rated after the relevance to the demands for the product, and the characteristics are determined.

In Figure 2-2, HOQ is presented and shows that the strength of the towbar and the size of the top plate are the key characteristics for the sled. In the mid table, the customer objectives are related to the engineering characteristics and rated from 1-3 on the relationship between them, where 3 is the strongest relationship. The customer objectives are weighted based on the importance where 0 is worst and 10 is most important. In the summation the rank and the weight are multiplied and summed up.

On the top of the table the engineering characteristics are compared to each other, and marked with a black dot if they are related. To the left of the table two existing products are compared to the customer objectives and ranked with values from 1-3 where three is the highest score.

By comparing existing products to the objectives, it is possible to exploit the strong attributes on the models in order to gain inspiration for the design process. The two models scores the same, but have different strengths and weaknesses. Model 1 is in this case the cargo sled J830 by Montana Trailers that is similar to the one that Hjelpekorpset uses today (3). This model scores high on sustaining loads and is easy to operate, which are two of the most important objectives for the design. Model 2 is a sled from Altapulken that is intended for rescue missions. This model is specialized in comfort for patients with a door made for entering stretchers, and heater to keep the sled warm (4). It scores high on comfort and passenger safety.
Figure 2-2: House of Quality. Roof: Engineering characteristics are compared and a black dot symbolizes that the one characteristic is dependent on the other. Middle: Customer objectives relative to engineering characteristics are rated from 1-3 where 3 is best, multiplied with the weight of the objectives and summed up. Right: Two competing snowmobile sleds are compared to each other. Drawn in INKSCAPE 0.91.

2.4 Alternatives

In order to generate the best suitable alternative designs for the design, “the morphological chart method” by Nigel cross is used. “The aim of the morphological chart method is to generate the complete range of alternative design solutions for a product, and hence to widen the search for potential new solutions” (5)

The railings surrounding the sled is not satisfactory as they appear today. When placing a stretcher on the sled, the railings is a hurdle in the top and rear end of the sled. However, the railings can not be removed completely since there is a need for some kind of railings to secure cargo, stretchers, equipment and persons. Additionally, the sled should have some extra security for cargo, preferably as a frame that is removable and easy to attach to the sled when needed.

The towbar is the part of the sled that “Hjelpekorpset” have experienced the most problems with, and need to be improved. The new design needs to make a sustainable solution that requires minimum maintenance and is less likely to fail than the sled in use today. To obtain this it is natural to have as few components as possible in a strong, solid construction. The profile of the components as well as how they are fastened to the sled will be essential.

Additionally, the mass have to be considered as the whole system can not exceed 50 kg. The alternatives for the features and suggested solutions are presented in Table 2-2. The solutions are expressed in paths of different colors.
Table 2-2: Generated alternatives and solutions for railing, frame and towbar on top plate. Illustrations drawn in INKSCAPE 0.91 if references not are given.

<table>
<thead>
<tr>
<th>Features</th>
<th>Alternative 1</th>
<th>Alternative 2</th>
<th>Alternative 3</th>
<th>Alternative 4</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>RAILING</strong></td>
<td>Only on longitudinal sides</td>
<td>On longitudinal sides and top</td>
<td>Detachable in top and rear end</td>
<td>Detachable in rear end</td>
</tr>
<tr>
<td><strong>Lock</strong></td>
<td>None</td>
<td>Manual lock</td>
<td>Click lock</td>
<td></td>
</tr>
<tr>
<td><strong>Attachment</strong></td>
<td>None</td>
<td>Reattach completely</td>
<td>Hang loose at ends of sled</td>
<td>Stops at 90°</td>
</tr>
<tr>
<td><strong>FRAME</strong></td>
<td>Open loop of 4 foldable plates</td>
<td>Closed loop of 4 foldable plates</td>
<td>Frame attached to sled, foldable</td>
<td></td>
</tr>
<tr>
<td><strong>Attachment</strong></td>
<td>Free, supported by railings</td>
<td>Locked onto railing</td>
<td>“Clicked” into railing (railing and frame design to fit)</td>
<td>Tied onto railing</td>
</tr>
<tr>
<td><strong>TOWBAR</strong></td>
<td>Simple rod attached to body structure</td>
<td>Triangular attached to body structure</td>
<td>Triangular attached to body structure and ski</td>
<td>Simple ring to directly attach to snowmobile</td>
</tr>
<tr>
<td><strong>Attachment</strong></td>
<td>Welded</td>
<td>Screwed</td>
<td>Joint</td>
<td></td>
</tr>
</tbody>
</table>
## 2.5 Evaluation
The different solutions (colored lines) in Table 2-2 got different qualities. To make sure the best solution for the problem is selected, “The Weighted Objectives Method” by Nigel Cross is used. This method uses the objectives of the product to measure the different solutions. By giving each of the solutions a weighted number, it is easier to make a scientific approach for comparing the solutions rather than guessing and assuming.

### Design Objectives
In Chapter 2.3 HOQ was presented and the objectives for the whole sled listed. Some of these objectives applies directly to the railings, frame, and towbar, but there are also some objectives that are not listed in the HOQ. The total objectives are listed below with an assigned letter:

A. Light weight
B. Reliability
C. Passenger safety
D. Easy to operate with gloves
E. Easy maintenance
F. Small number of components
G. Optimal design for transport of stretcher
H. Optimal design for transport of cargo
I. Good maneuverability

In order to set weights for the objectives, they have to be compared to each other. In Table 2-3, this is done by setting the objectives as both rows and columns, and comparing them to each other. If for instance A and B are being compared, and B is the more important of the two, B will be assigned 1 and A assigned 0. All results then are summed up for each objective and assigned weights accordingly equation 2-1 and ranked.

\[
\text{Relative weight} = \frac{\text{Resulting sum for objective}}{\text{Total resulting sums for all objectives}}
\]

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
<th>G</th>
<th>H</th>
<th>I</th>
<th>Result</th>
<th>Weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>-</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>5</td>
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<tr>
<td>1</td>
<td>-</td>
<td>1</td>
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<td>0</td>
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<td>1</td>
<td>5</td>
<td>0.14</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>-</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>4</td>
<td>0.11</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>1</td>
<td>-</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>3</td>
<td>0.08</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>-</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>4</td>
<td>0.11</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>-</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>3</td>
<td>0.08</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td>1</td>
<td>0</td>
<td>6</td>
<td>0.17</td>
</tr>
<tr>
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<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>-</td>
<td>0</td>
<td>3</td>
<td>0.08</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>-</td>
<td>3</td>
<td>0.08</td>
</tr>
</tbody>
</table>

Sum 36 1.00

### Evaluation
In order to find a rational and feasible solution, the different suggested solutions have to be compared using the found objectives. In Table 2-4 the solutions are compared according to a five-step scale:

0. Inadequate
1. Weak
2. Satisfactory
3. Good
4. Excellent

To find the best solution the results are multiplied with the relative weights of the objectives and the blue solution from Table 2-2 stands out as the optimal solution.
Table 2-4: Evaluation of solutions for railings and frame

<table>
<thead>
<tr>
<th></th>
<th>Blue</th>
<th>Red</th>
<th>Green</th>
<th>Orange</th>
</tr>
</thead>
<tbody>
<tr>
<td>Light weight (0.14)</td>
<td>3</td>
<td>3</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>Reliability (0.14)</td>
<td>3</td>
<td>2</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>Passenger safety (0.14)</td>
<td>2</td>
<td>2</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Easy to operate with gloves (0.11)</td>
<td>3</td>
<td>2</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>Easy maintenance (0.11)</td>
<td>2</td>
<td>2</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Small number of components (0.07)</td>
<td>2</td>
<td>2</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Transport of stretcher (0.18)</td>
<td>4</td>
<td>2</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>Transport of cargo (0.11)</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Good maneuverability (0.08)</td>
<td>3</td>
<td>0</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>SUM</td>
<td>2.86</td>
<td>2.06</td>
<td>2.47</td>
<td>1.81</td>
</tr>
</tbody>
</table>

2.6 Details

2.6.1 Railings

The railings have to be a simple, supporting structure for passengers to hold on to, or to fasten cargo, the frame or stretchers to. It will be welded onto the body structure to ensure stability. The design should be as simple as possible to ensure minimum mass but at the same time strong enough to be secure. Since it will be railings only on the two longitudinal sides of the sled, they lose some of the support they have today from being a closed loop. Hence, some measure have to be done to ensure the stability of the structure. A simple solution is to have the railing curve around the corners of the top plate, but not cover the short sides. The suggested rail design is shown in Figure 2-3.

2.6.2 Top plate

The function of the top plate is simply to support cargo and persons. It needs to withstand the load and impacts while driving in difficult terrain. Since the total mass of the sled is set to 50 kg, it is important to regard the mass of the plate as well.

The size of the top plate affects the mass, which should be kept to a minimum. The length and width therefor will be set to the minimum measures in Table 2-1, respectively 1600 mm x 900 mm. Additionally, the material, which will be decided later on in the process, and structure of the top plate will be essential for the total mass.

2.6.3 Towbar

Since the towbar is the feature on the sled that is the most troubled today, it is subject for different evaluation than the rest of the features. The mass is important, but the most important requirement is that it needs to be strong, reliable, and contribute to the sled being easy to maneuver and stable. The blue solution in Table 2-2 suggests that a triangular construction with attachment in the body structure of the sled itself, as illustrated in Figure 2-4. This will be one of the heaviest solutions, but it will fill the
requirements the best. To try to get the mass down the profile of the rods used in the towbar have to be subject for investigation.

To try to get the mass down the profile of the rods used in the towbar have to be subject for investigation.

2.6.3.1 Features
In the blue solution in Table 2-2, the attachment method to the sled is welding. A welded joint will cause the resulting forces that occurs when the snowmobile breaks, accelerates or turns to propagate to the rest of the system and could cause weaknesses in the design. It is not desirable to have moment or axial forces spreading throughout the structure and in order to avoid this situation it is necessary to explore the other attachment options.

The best option to avoid the case of propagating forces are to have a joint that is rotational in one or more directions like the alternatives illustrated in Figure 2-5. As the figure illustrates, the balljoint is rotational in all three directions while the hingejoint is rotational only in one direction. While riding the sled, the towbar will move in all directions relevant to the attachment to the snowmobile, and some rotational freedom in all directions will be preferred and could spare the rest of the system from damage. Installing a balljoint on the sled, however, is an intricate process. A hingejoint with bearing can be, if not rotational, tolerant to movements in all directions and damp impacts. The bearing is easy to replace if wore down, as well as other parts in a hingejoint rather than a balljoint. This is a standard component that many production companies are producing today, and will be outsourced to an established company rather than produced.

For the comfort, as well as preventing damage to the towbar and ease the attaching and detaching of the sled to the snowmobile it is desirable with a rotational attachmentring. This could be solved by installing a hallow rod connecting the triangle structure with the attachmentring in the end, as illustrated in Figure 2-6.
2.6.3.2 Analyses and Dimensioning

In order to set the dimensions of the structure, the worst-case scenario of forces acting on the sled are considered. The possible situations where forces are acting on the sled are when the snowmobile accelerates, brakes, turns, accelerates & turns simultaneously or brakes & turns simultaneously. In order to determine which are the worst case scenario, the situation in Figure 2-7 is studied where the force F is the behavior of the snowmobile.

\[
\sum F_x = 0 \rightarrow F - A_x + B_x = 0 \rightarrow F \cos \alpha - A_x + B_x = 0
\]
\[
\sum F_y = 0 \rightarrow F_y - A_y - B_y = 0 \rightarrow F \sin \alpha - A_y - B_y = 0
\]

This shows that the resulting force in x direction in A will become largest and will increase as \( F \cos \alpha \) increases which gives \( |\alpha| = 0, \pi, 2\pi, 3\pi \ldots \). The results shows that the situation will have the same magnitude in the opposite direction if the snowmobile are breaking instead of accelerating.

In order to determine the angle between AC and BC the rods are isolated and a diagram of the free bodies evaluated. Each of the rods are affected by two forces, and will seek equilibrium which will lead to the forces being equally big but opposite directed as illustrated in Figure 2-8 (8).
The figure illustrates the case when the link in C is in equilibrium and the forces acting on AC are tension forces \(F_t\), while the forces acting on BC are compressive forces \(F_c\), and the diagram of the free bodies becomes as in the upper corner of Figure 2-8. By comparing the sums of the forces for this case, it is possible to find the angle \(\theta\).

\[
\begin{align*}
\sum F_x &= 0 \rightarrow T\cos\theta - S\cos\theta + F_x = 0 \rightarrow F_x + \cos\theta(T - S) = 0 \\
\sum F_y &= 0 \rightarrow -T\sin\theta - S\sin\theta = 0 \rightarrow \sin\theta(T + S) = 0 \\
\Rightarrow T &= -\frac{F_x}{2\cos\theta}, \quad S = \frac{F_x}{2\cos\theta}, \quad 0 < \theta < \frac{\pi}{2}
\end{align*}
\]

This proves that \(F_t\) and \(F_c\) are larger the more \(\theta\) grows. It suggests that the angle between AC and BC, which increases with decreasing \(\theta\), should be as big as possible, hence the distance between A and B should be as wide as the sled itself. The length of the rods should be as small as possible for minimum resulting forces passing on to the sled, but still long enough to ensure stability and best possible maneuverability. Stability and maneuverability cannot be calculated since it is human experienced properties, and the rods are set to be half the length of the top plate, which gives a length of 900 mm.

### 2.6.4 Skis

The function of the skis are to make the sled slide on snow and support the sled so it stays above ground. Skidesign are important for the maneuverability and safety in difficult terrain or different kinds of snow and ice. A wider ski will make the sled more stable and better afloat in deep snow, and a thinner ski assures that less energy is required to steer the sled in snow and can make it more stable on hard, icy snow. The mass of the skis should be considered as well to maintain as low total mass as possible.

#### 2.6.4.1 Alternatives and evaluation

The skis will be outsourced to a manufacturing company that already produces skis. In Table 2-5, three types of skis have been described, compared and evaluated. The skis are chosen since they all have cross section profiles that offers qualities to make them stable and avoid darting. Alternative 3 from KIMPEx seems like the best choice based on this information since it is the lightest option, seems to have good maneuverability and comes with mount kit included in the price.
### Manufacturer

<table>
<thead>
<tr>
<th>Manufacturer</th>
<th>C&amp;A PRO (9)</th>
<th>Ultimate Snowmobile Skis &amp; Parts (USI) (10)</th>
<th>KIMPEX (11)</th>
</tr>
</thead>
</table>

| Illustration                        | ![Image]                          | ![Image]                                    | ![Image]         |

| Weight (pair)                       | 6.24 kg                           | 6.8 kg                                      | 3.62 kg         |
| Width                               | 184.15 mm                         | 304.8 mm                                    | 127 mm          |
| Mount kit included                  | No                                | No                                          | Yes             |
| Price                               | 2147 NOK                          | 3723 NOK                                    | 2463 NOK        |
| Maneuverability                     | Plastic Keel                      | Metal Keel                                  | Metal Keel      |
|                                     | Pebbled sides                     | Pebbled sides                              | Raised rear portion |
|                                     | Pebbled underneath                | Side edge underneath                       | Side edge underneath |

#### 2.6.4.2 Details

To improve the stability, a possibility is to install two skis per side of the sled. This will add considerable mass to the system with a total of 4 ski-systems (skis, suspensions and shock absorbers). The estimated mass for one ski-system is 5 kg.

With two skis on each side, the sled will have a large contact area with the substrate and will acquire more energy for the snowmobile to turn around, and cause less maneuverability. The arguments of mass and maneuverability are higher prioritized in this situation, thus there will be only one ski-system on each side of the sled.

The suspensions are designed as a simple, triangular construction where the shock absorbers will be installed as well. In the technical drawings, the shock absorbers are not included, and a simplified model of the skis are attached only for the illustrative purposes.

#### 2.6.5 Supporting body structure

The supporting body structure have only one function: to keep the sled together. It needs to connect all other features in a satisfying matter, which makes it a simple, rectangular structure where the top plate rests, the towbar joints and the railings and ski-systems are welded onto. Since the maximum mass of the sled is set to 50 kg, it is important that the body structure is as simple as possible with a material and profile that is both strong and light.

#### 2.6.6 Detachable Frame

For the frame to be as easy and practical as possible, the chosen design is an open loop. In Table 2-2 the suggested design consists of four sides. In order to make the frame foldable and easier to handle since the sled not is squared but rectangular, the design is changed to five sides connected through hinges as illustrated in Figure 2-9. As before, the mass are to be kept to a minimum and the frame have to be easy to attach or detach to the railing. The structure have to be strong enough to secure the cargo and resist weather changes, equal to the top plate, and the material for the two will be the same in the drawings. The walls need to be high enough to keep cargo from falling out of the sled, and are set to 500 mm. Length and width are the same as for the sled itself so it can fit directly into the sled and the design should be as simple as possible.
Outdoor during winter time, especially in the mountains, the temperatures drops real low, and it is a big advantage to be able to handle all aspects of the sled with gloves on, the frame as well. Locks of various kinds, or tying ropes will be difficult under such conditions. A alternative solution for locking the loop is to have a click- solution, that requires minimum operations as illustrated in Figure 2-10.

Detailed drawings of the frame are presented in Appendix B.

Figure 2-9: The frame structure open, closed and folded. Illustration created in SolidWorks.

Figure 2-10: Click-lock solution for frame-loop. Drawn in INKSCAPE 0.91.

3 Material Selection
The method for the material selection is the method presented in the book “Material selection in mechanical design” by Michael F. Ashby. This method systematically goes through the stages from idea to finished design via three stages.

The concept phase and parts of the Embodiment phase in Figure 3-1 is conducted previously in the design process. One of the main physical properties that have to be prioritized for both the towbar and the top plate is the total mass of the sled as well as the performance in different weather conditions and temperatures and the ability to resist applied forces. For the material selection itself, material indexes are calculated and applied to material charts using the software CES EduPack 2016.
3.1 Towbar

It is decided that the towbar it should be a triangular construction that is attached to the sled through a hinge joint, and to the snowmobile through a rotational ring.

3.1.1 Material indexes

As stated in chapter 2.6.3, details of the towbar design; even though the weight of the sled is important, the most important thing for the towbar is that it needs to be strong, reliable, and contribute to the sled being easy to maneuver and stable. The length of the rods are set to 900 mm, and the width should be as long as the width of the sled. The profile of the rods should be as thin as possible but at the same time be strong enough to withstand the forces acting on the system. The design requirements for the light beam are presented in Table 3-1.

Table 3-1: Requirements towbar beam for material selection

<table>
<thead>
<tr>
<th>Function:</th>
<th>Towbar beam</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constraints:</td>
<td>a) Length= 900 mm</td>
</tr>
<tr>
<td></td>
<td>b) Support bending load F without failing by yield or fracture</td>
</tr>
<tr>
<td>Objective:</td>
<td>Minimize mass</td>
</tr>
<tr>
<td>Free variable:</td>
<td>a) Cross-section area</td>
</tr>
<tr>
<td></td>
<td>b) Choice of material</td>
</tr>
</tbody>
</table>

This gives the objective function

\[ m = AL\rho \quad (3-1) \]

Where \( m \) is mass, \( A \) is cross-section area, \( L \) is length and \( \rho \) is the density of the material.

In Figure 3-2 the situation when accelerating is illustrated on a small part of one rod as a beam with length \( L \) and applied tensile force \( F \) and elongation, \( \varepsilon \).
Both F and L are fixed, and the cross-section area have to be sufficient to support the tensile load. The failure strength of a material can be expressed as in equation 3-2, and rewritten to make sure the cross-section is large enough for the applied force.

\[
\sigma_f = \frac{F}{A}
\]

\[
A \geq \frac{F}{\sigma_f}
\]  

Combined with equation 3-1 this gives

\[
m = AL\rho \geq \left( \frac{F}{\sigma_f} \right) L\rho \implies m \geq FL \left( \frac{\rho}{\sigma_f} \right)
\]

Where the last bracket containing the density and the failure strength is the one related to the material properties. This gives the material index in equation 3-3 that is inserted in the material chart presented in Figure 3-3.

\[
M_1 = \frac{\sigma_f}{\rho}
\]

In addition to the tensile strength, the compressive strength of the beam is important in the case of the snowmobile breaking and the towbar have to be strong enough to withstand the weight of the sled being pressed towards the snowmobile. Euler’s buckling describes how a beam behaves when applied a compressive force (13). In equation 3-4, it is the case when both ends are pinned.

\[
F = \frac{\pi^2 EI}{L^2}
\]

Where E is the modulus of elasticity of the material and I is are moment of inertia of the cross section. I in the case of the beam is expressed in equation 3-5.

\[
I = \frac{b^4}{12}
\]

Combined with equation 3-1 this gives

\[
b^2 = \left( \frac{12FL^2}{\pi^2E} \right)^\frac{1}{2} \Rightarrow m = (12F)^\frac{1}{2} \left( \frac{L^2}{\pi} \right) \left( \frac{\rho}{E^2} \right)
\]

Resulting in the second material index expressed in equation 3-6 and inserted in Figure 3-4.
After these selections, it still remains too many materials to choose from that are relevant candidates. In order to narrow the selection down further, the price per kg of the materials are compared in Figure 3-5 and a limit is set on 50 NOK/kg.

Figure 3-3: Material chart Yield strength/Density for the material selection of the towbar. The chart is created in CES EduPack 2016.

Figure 3-4: Material chart Young’s modulus/Density for the material selection of the towbar. The chart is created in CES EduPack 2016.
3.1.2 Evaluation

These three stages leave five relevant materials in the metals and alloys family that is listed in Table 3-2. In order to compare the materials the different properties have been given a value from 1-5 where 1 is best relative to the other materials. The values are summed up in Table 3-3, and the material that scores the best are age-hardening wrought Al-alloys. Further investigations in the data sheet in Appendix C shows that the Aluminium 6000 series are typically used in general engineering and automotive such as connecting rods.

The railings and body structure of the sled will be designed as rods as well, and have to withstand impacts and imposed forces. Aluminium 6000 series are common to use for such purposes, and are considered as a good fit for these parts as well.

Table 3-2: Material properties of the remaining five materials for the towbar (14) (15) (16) (17) (18)

<table>
<thead>
<tr>
<th>Material</th>
<th>Density $[10^3 \text{ kg/m}^3]$</th>
<th>Young's modulus [GPa]</th>
<th>Yield strength [MPa]</th>
<th>Price [NOK/kg]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wrought magnesium alloys</td>
<td>1.5-1.95</td>
<td>42-47</td>
<td>115-410</td>
<td>26.9-28.2</td>
</tr>
<tr>
<td>Cast magnesium alloys</td>
<td>1.75-1.87</td>
<td>42-47</td>
<td>70-215</td>
<td>26.9-28.1</td>
</tr>
<tr>
<td>Cast Al-alloys</td>
<td>2.5-2.9</td>
<td>72-89</td>
<td>50-330</td>
<td>20.3-23.3</td>
</tr>
<tr>
<td>Non age-hardening wrought Al-alloys</td>
<td>2.5-2.9</td>
<td>68-72</td>
<td>30-286</td>
<td>19.7-22.4</td>
</tr>
<tr>
<td>Age-hardening wrought Al-alloys</td>
<td>2.5-2.9</td>
<td>68-80</td>
<td>95-610</td>
<td>19.6-22.4</td>
</tr>
</tbody>
</table>

Table 3-3: Material properties of the remaining materials for the towbar in values relative to each other where 1 is best and 5 is worst

<table>
<thead>
<tr>
<th>Material</th>
<th>Density</th>
<th>Young's modulus</th>
<th>Yield strength</th>
<th>Price</th>
<th>Sum</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wrought magnesium alloys</td>
<td>1</td>
<td>4</td>
<td>2</td>
<td>5</td>
<td>12</td>
</tr>
<tr>
<td>Cast magnesium alloys</td>
<td>2</td>
<td>4</td>
<td>5</td>
<td>4</td>
<td>15</td>
</tr>
<tr>
<td>Cast Al-alloys</td>
<td>3</td>
<td>1</td>
<td>3</td>
<td>3</td>
<td>10</td>
</tr>
<tr>
<td>Non age-hardening wrought Al-alloys</td>
<td>3</td>
<td>3</td>
<td>4</td>
<td>2</td>
<td>12</td>
</tr>
<tr>
<td>Age-hardening wrought Al-alloys</td>
<td>3</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>7</td>
</tr>
</tbody>
</table>
3.1.3 Dimensioning
Knowing the material properties, the cross-section area and width of the rod is calculated in Appendix D. In the calculations, it is assumed that the material have the highest density and lowest young’s modulus (worst-case scenario) for age-hardening wrought al- alloys presented in Table 3-2. The force applied to the system are calculated from assumption of acceleration of 0-100 km/t on 1.5 s and total a weight of the system of 1000 kg. This cross section area will give a side width of only 23 mm, and in order to make it more robust but not adding weight, the profile of the towbar rods is hollow. The calculated area will be the same, but the width of the sides will differ. The inner widths are set to 15 mm and make the outer widths 27.3 mm. this gives a mass of 1.34 kg per rod using Al alloy of the 6000 series, which have a density of 2700 kg/m³. Such a low mass allows for larger dimensions to ensure that the construction will be strong for even worse cases than the one calculated.

3.2 Top Plate and detachable frame
The dimensions of the top plate are set to 1600 mm x 900 mm and it have to sustain the maximum mass of 300 kg. The supporting body structure will relieve some of the impact, but the plate have to be strong enough not to brake or crack under the force of the impact that may occur in bumps or when loading the sled.

The detachable frame will have the same requirements as the top plate for the material choice to withstand some impacts with the cargo, and both the top plate and the frame have to be as light as possible. The dimensions for the sides of the frame are 900 mm x 500 mm and 1800 mm x 500 mm, while the thickness for both the frame and the top plate are free variables.

The design requirements for the top plate are presented in Table 3-4. Requirements for the frame would be the same as for the top plate.

<table>
<thead>
<tr>
<th>Table 3-4: Requirements Top plate for material selection</th>
</tr>
</thead>
<tbody>
<tr>
<td>Function: Top plate</td>
</tr>
<tr>
<td>Constraints: a) Length= 1600 mm</td>
</tr>
<tr>
<td>b) Width= 900 mm</td>
</tr>
<tr>
<td>c) Support impact with cargo load F without failing by yield or fracture</td>
</tr>
<tr>
<td>Objective: Minimize mass</td>
</tr>
<tr>
<td>Free variable: a) Cross- section area</td>
</tr>
<tr>
<td>b) Choice of material</td>
</tr>
</tbody>
</table>

This gives the objective function that is presented in equation 3-1.

The Young’s modulus, $E$ is a measure of the elasticity or impact strength of the material, and are directly related to the stress, $\sigma$ and strain, $\varepsilon$ in a material as shown in equation 3-7.

$$E = \frac{\sigma}{\varepsilon}$$  \hspace{1cm} (3-7)

By combining equations 3-1, 3-2 and 3-7, knowing that $V= At$ for a plate where $t$ is the thickness, this gives:

$$\frac{m}{\rho \cdot t} = \frac{F}{E \cdot \varepsilon}$$

Since the thickness is a free variable in this case, the expression is rewritten and gives a material index as follows:

$$t = \frac{m \cdot \varepsilon}{F} \frac{(E)}{\rho}$$

$$M = \frac{\rho}{E}$$

The material index is inserted in Figure 3-6, where it becomes clear that several material groups are relevant based on this. However, since the total mass of the sled is important, the limit for the density is set to 1500 kg/m³.
Since the sled is going to be used as passenger or patient transport in low temperatures, it is important that the top plate does not get too cold; hence, the thermal conductivity is investigated in Figure 3-7. A limit at 1 W/m°C is set to narrow down the selection.

The cost is always a subject of interest in the design processes, and in Figure 3-8 the price per kg material is compared with the density of the material. This leaves the natural materials as the best choice for this purpose, and plywood fits the requirements and area of use for the top plate which can be read about in Appendix E; datasheet of plywood.

![Material chart Young's modulus/ density for the material choice of the top plate inserted with material index ρ/E and limit for the density at 1500 kg/m^3. The chart is created with CES EduPack 2016.](image1)

![Material chart Thermal conductivity for the material choice of the top plate inserted a limit at 1 W/m°C. The chart is created with CES EduPack 2016.](image2)
Figure 3-8: Material chart Price/ density for the material choice of the top plate. The chart is created with CES EduPack 2016.

4 Production methods

Age-hardening wrought Al-alloys are created by heating the material to a temperature where it is still solid, but makes the alloying elements dissolve, and then cooled down rapidly. After this the material is heated once more, but not to temperatures as high as in the dissolving phase, for several hours so that it ages and obtain its mechanical properties of high strength and corrosion resistance. This process leaves a low weight material but with constrains in the processability properties (19). The best methods of processing are, accordingly the datasheet in Appendix C, casting and machining.

Casting is a production method where the material is shaped in liquid state. The material is poured into a mold and cooled down to solid phase temperature. Centrifugal casting is used for casting of cylindrical shaped metals and includes die casting, investment casting, permanent mold, sand casting and shell mold casting (20).

When machining a material the component is shaped by material removal such as turning, drilling, boring and mashing (20).

For this case, CES EduPack 2016 is used to help choose the production method. Figure 4-1 shows that investment casting are among the best methods for non-ferrous metals such as aluminium alloy Al6061 and are economically attractive for small batches. Figure 4-2 shows that this method offers a low limit for the tolerance of the dimensions as well, which is useful for the accuracy of the design. To create the figures, limits were set for the relative equipment costs at medium and relative tooling cost at low. The datasheet of the investments casting are presented in Appendix F where it states that this production method can be used for both solid parts, and hollow components.
Figure 4-1: Process chart of economic batch size/ non-ferrous metals. The chart is created with CES EduPack 2016.

Figure 4-2: Process chart of tolerance [mm]. Limits are set for the relative equipment cost and the relative tooling cost at medium and low, respectively. The chart is created with CES EduPack 2016.

5 Finite element analysis
Finite element analysis (FEA) are mainly used in engineering problems regarding strength or temperature tolerances in a structure or material exposed to loads, pressure or extreme temperatures. Such analysis are done by Partial differential equations (PDE) that usually are too complicated for analytical analysis. To perform such analysis, numerical approximations are performed, such as FEA. Today several software facilitates the process for the engineer (21).

5.1 Strength analysis
A snowmobile sled will be subjected to forces applied by the snowmobile itself while driving as well as the cargo on the sled and possible uneven terrain. The largest force will occur when the snowmobile is accelerating while turning 90° and cause the largest amount of stress on the towbar. Even though the towbar rods are dimensioned for these stresses, other components or the rods could give in under extreme conditions and need to be tested.

When the snowmobile turns, this will give both compressive and tension forces that could lead to the material giving in and be permanently deformed. A measure of the elasticity of the material is the
yield strength that gives a measure of the tolerance of the material until deformation occurs. Von Mises stress are stresses that occurs in the material and are considered a safe measure for engineering problems. If the von Mises stress exceeds the yield strength, the material will have plastic deformation and are more likely to fail. Hence, the aim is that all parts of the towbar should experience a lower von Mises stress than the given yield strength (22).

If the structure is not dimensioned for the applied forces, it might be deformed into a state where the structure can no longer be used for the purpose it is intended for. In addition to von Mises stress, the strain that occurs in the material can be a good indicator of whether the design is acceptable or not. The strain and deformation are directly linked together as shown in equation Feil! Fant ikke referansekilden, where $\varepsilon$ is the engineering strain, $\Delta L$ is the change in length when exposed to forces, and $l_0$ is the initial length. This connection makes it important to keep the strain to a minimum (23).

$$\varepsilon = \frac{\Delta L}{l_0} \quad (5-1)$$

5.2 SolidWorks

The towbar, with hingejoints, rods and attachment ring were subject for the linear structural analysis in SolidWorks simulation add- in. This add-in allows the 3D CAD drawing to be analyzed directly.

In the original design, all parts except for the plastic sides and the rubber tubes of the hingejoints were done in Aluminium alloy Al6061. The attachment ring were set to a profile of 10 mm, and were a free variable. In chapter 2.6.3 it became clear the ring should be rotational to ease handling. The dimensioning of the hingejoints were set according to the bodystructure of the sled as well as the calculated dimensions of the towbar- rods.

High quality, fine mesh was applied to the model, and a force of 20 kN simulating maximum acceleration while turning 90° were applied to the attachmentring. Since the analysis is worst-case scenario, the hingejoints were fastened as if the sled were stuck while the snowmobile is accelerating. The meshing, forces, materials etc. are described in detail in the report in Appendix G produced after the final analysis.

The analysis showed that the dimensioning of the attachment ring needed redesigning due to large displacement and high Von Mises stress. The first analysis showed that it was the attachmentring that was the weak point at the structure and the main focus of the further analysis. The displacement were much larger than what is acceptable, and the ring were deformed due to the applied force thus the ring were subject for redesigning. The redesigning of the attachment ring and the rods were done in several iterations, as presented in table 5-1.

After altering the profile of the ring and the rods, the design of the ring, how it was attached to the towbar as well as the material of the ring; the stress, strain and displacement became satisfactory. Figure 5-1 shows the deflection of the towbar, and illustrates how the attachment ring is the weakest link. The rods themselves seems to handle the forces well, and that the calculated profiles from the analysis in Chapter 3.1 are sufficient for this case.
Table 5-1: Iterations of analysis of the towbar in Solid Works with changes in design done in each iteration and resulting Von Mises stress, displacement and strain.

<table>
<thead>
<tr>
<th>Iteration</th>
<th>Changes in design</th>
<th>Von Mises [pa]</th>
<th>Displacement [mm]</th>
<th>Strain</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>N/A</td>
<td>4.24529 \times 10^9</td>
<td>27.9361</td>
<td>0.252238</td>
</tr>
<tr>
<td>2</td>
<td>Dimensions for the profile of the attachment ring enlarged by 5 mm. Profile of the rods altered so that they are solid bodies, and not hallow.</td>
<td>7.55718 \times 10^9</td>
<td>10.3241</td>
<td>0.048519</td>
</tr>
<tr>
<td>3</td>
<td>Rod on the attachment ring were shortened down to 15 mm. Cross section of the main rods were enlarged from 35x35 mm to 35x40 mm, keeping the same cross section area.</td>
<td>2.4318 \times 10^9</td>
<td>8.2837</td>
<td>0.0377143</td>
</tr>
<tr>
<td>4</td>
<td>Material of attachment ring changed from 6061 Aluminium alloy to 201 Annealed stainless steal</td>
<td>2.58224 \times 10^9</td>
<td>4.68902</td>
<td>0.0127025</td>
</tr>
<tr>
<td>5</td>
<td>Length of ring changed from 15 mm to 12 mm</td>
<td>1.19966 \times 10^9</td>
<td>4.09967</td>
<td>0.0117419</td>
</tr>
<tr>
<td>6</td>
<td>Changed the profile of the rod on the ring from 14.5 mm to 15 mm wide Material of attachment ring changed to Titanium alloy Ti-6Al-2Sn-2Zr-2Mo-2Cr-0.25Si (SS) that got high yield strength.</td>
<td>1.142 \times 10^9</td>
<td>4.666</td>
<td>0.01494</td>
</tr>
<tr>
<td>7</td>
<td>The design of the ring altered so that the ring is welded directly onto the towbar, and the attachment ring rod that made it rotational was deleted.</td>
<td>3.7023 \times 10^8</td>
<td>3.44939</td>
<td>0.00503221</td>
</tr>
</tbody>
</table>
Figure 5-1: Deflection of the towbar after performing FEA analysis. Maximum displacement 3.44939 mm.

6 Prototyping
A design process requires several steps, and iterations. This leaves the designer with a clear idea of how the product should look and feel like; however, this might not be consistent with the real case. In order to get a clearer idea of how the dimensions of the different components are relative to each other an alternative is to print a downscaled model of the design in a 3D printer.

The printer that were used is a Cubepro duo by 3D systems, which prints in PLA (Polylactid acid), ABS (Acrylonitrile Butadiene Styrene) and dissolvable natural PLA using Layer manufacturing technology (LMT) (24). This technique is divides a 3D model into 2D layers, and prints the model layer by layer to a complete 3D model as can be studied in Figure 6-1 that is a close-up photograph of the skis and shows the layers (25).

Figure 6-1: Close-up of the ski in the 3D printed model. Lines on the rods and ski shows the effect of LMT.
Photo: Kari W. Johansen
The model were downscaled to approximately 8% of the original size, making the total length 213 mm in ABS. To make the model robust, it was necessary to enlarge some of the rod dimensions and simplify the design:

- Profiles of railings were increased to 50 mm diameter.
- Profile of body structure frame were increased to 60x60 mm.
- Hingejoint were cut since there are some weak connections that are complicated to enlarge.
- The profiles of the rods of the towbar were done rigid and increased to 50x50 mm.
- Railings and skis were printed separately and glued onto the model of the sled.

In Appendix H technical drawings of the 3D printed model are presented.

Since the sled not is printed in the calculated dimensions or materials, it is not suitable for testing of forces or environmental challenges; the area of application is aesthetics. In Figure 6-2 a photograph of the model is presented.

![Figure 6-2: photo of 3D printed model of the sled. Photo: Kari W. Johansen](image)

### 7 Final Design

From using design methods by Nigel Cross and material selection methods by Michael F. Ashby, the sled have been redesigned to better meet the requirements set in Chapter 2. In Appendix I detailed drawings of the sled is presented, in table 7-1 a summary of components with material and weight are listed and in Figure 7-1 the final design is illustrated.

The design deals with resulting forces that spreads throughout the sled by installing hingejoints with bearings in the transmission from the towbar to the sled. This way the sled will last longer and require less maintenance than today. The hingejoints are easy to change parts in, and if they are ordered from a known manufacturer, the costs would not be large in replacing parts.

To lower the maintenance, the objective have been to have a simple design with few parts. The towbar have been the focus, and designed to consist of two hallow rods attached to a ring for towing. The structure have been subject for finite element analysis and over several iterations, the design was adjusted to resist the applied force. This resulted in a ring that is welded directly onto the towbar structure, and different material on the ring than the rest of the structure.

Sleds used today have railings surrounding the top plate. The design of the railings have been altered to better fit the area of use with railings only on the longitudinal sides of sled, making the sled suitable for both stretchers with patients and transporting cargo.

As for the hingejoints, the skis are outsourced as described in chapter 2.6.4.
Table 7-1: Components of the final design with material and weight

<table>
<thead>
<tr>
<th>Component</th>
<th>Material</th>
<th>Weight [g]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Railings x2</td>
<td>Al6061 alloy</td>
<td>2277.04</td>
</tr>
<tr>
<td>Towring</td>
<td>Ti-6Al-2Sn-2Zr-2Mo-2Cr</td>
<td>188.92</td>
</tr>
<tr>
<td>Top plate</td>
<td>Plywood</td>
<td>10048.18</td>
</tr>
<tr>
<td>Towbar</td>
<td>Al6061 alloy</td>
<td>1828.31</td>
</tr>
<tr>
<td>Supporting body structure</td>
<td>Al6061 alloy</td>
<td>14760.27</td>
</tr>
<tr>
<td>Hingejoint x2</td>
<td>N/A</td>
<td>234.42</td>
</tr>
<tr>
<td>Skisystem x2</td>
<td>N/A</td>
<td>5000</td>
</tr>
<tr>
<td>TOTAL</td>
<td></td>
<td>41848.6</td>
</tr>
</tbody>
</table>

It was desired by the customer to have some additional frame for protection of cargo that can be attached when needed. The detachable frame are set to be produced in plywood as the top plate in Chapter 3.2. The dimensions are set according to the sled itself. In Appendix B detailed 2D drawings of the frame with dimensions are presented.

Figure 7-1: The final design of the snowmobile sled. Model drawn in SolidWorks

7.1 Design restrictions

Even though the design have been subject for analysis, there are components and parameters that are not tested which could affect the performance of the product under extreme conditions. The analysis are executed using computer software and approximates how the system would behave in a real situation based on assumptions and calculations. Approximations can not predict the behavior of the system with certainty and are not to be considered a guarantee for the design.

The material choices are done using the software CES EduPack. This version of the software have a limited database of materials to choose from, and other materials could have changed the resulting design.

7.2 Further work

There are still work to be executed until the sled is ready to be produced:

- A 1:1 prototype in the chosen materials and profiles should be tested in the situations the sled is intended for. Tests like these should look into the strength of the whole system, the comfort and security for passengers and patients.
- As the front of the skis are not attached to the sled or towbar in any way, the stability of the skis are uncertain since they haven’t been tested and should undergo 1:1 tests in different terrains and snow types.
- The detachable frame have not been subject for any analysis, and the whole system should be analyzed for the worst-case scenarios that can occur while using it before producing them. Since the frame have a weight of 17 kg, the material choice and profiles should be analyzed as well to minimize the mass and weight.
- Analysis of the profiles of the railings need to be executed before producing since they have not undergone any strength analysis, and it is not certain they will sustain the applied forces.
- The profile of the top plate should be analyzed before producing to test for applied forces that will occur when being loaded with cargo and patients while driving in different terrains. The plate should be subject for analysis regarding the mass as well.
- Even though the towbar system as a whole have been analyzed, the hinge joints have not been looked into specifically. The ring and rods are dimensioned to withstand the worst-case scenario for the structure, however, the hinge joints should undergo analysis to determine if they can withstand repeating forces from the sides.
- In case the sled loosens from the snowmobile while driving, there are not installed any safety measures such as a safety line in the design as it occurs today. This should be installed for security means.
- Cost analysis of the production, shipping and mounting of the system.
Acknowledgements
The master thesis marks the end of five years at UiT, campus Narvik. It is the competence of the university as well as the student community in Narvik that have made these years as wonderful as they have been, and the management of the school deserves a big thank you!

Further, my supervisors Guy Mauseth and Andreas Seger have been a great support during these months and always ready to help or guide if there was a struggle. Together with the rest of the team on the engineering design department, they have created a learning environment and passed their knowledge on. Thanks to the whole team of lecturers, and a special thanks to my supervisors.

At last, I want to thank my classmates of 5ID that have been helpful, understanding and caring. We have pulled through these two years together.
Appendices
The following documents are attached to the report:

A. Problem Description
B. Technical 2D drawing with measures detachable frame
C.Datasheet age-hardening wrought al- alloys
D. Calculations of towbar profile
E. Datasheet plywood
F. Datasheet investment casting
G. Report Finite Element Analysis in SolidWorks
H. Technical 2D drawing with measures 3D model of the sled
I. Technical 2D drawing with measures final design of the snowmobile sled

External files:

J. STEP file of the CAD file of the sled

Software
Developing the product different software were used, that are listed below.

SolidWorks
SolidWorks is a 3D CAD software and is developed by Dassault Systèmes SA. It is used to produce 3D-models, technical drawings, FEM-analysis, illustrations, simulations, animations etc.

CES
CES is developed by Granta Design and CES EduPack is a teaching resource that contains a large database of materials and production methods as well as material software for material selection.

Inkscape
InkScape 0.91 is open-source vector graphics editor that allows making 2D illustrations in scalable vector graphics.
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24. 3D systems. CubePro. 3D Systems. [Internett] [Sittert: 01 06 2017.] https://www.3dsystems.com/shop/cubepro/techspecs.

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Appendix A: Problem Description

Re-design of a multipurpose snowmobile sled for Norwegian volunteer (SAR organizations).

Kari Wilhelmsen Johansen
Master thesis in Engineering Design ... Spring 2017
Background

The “Hjelpekorps” emergency response extends well beyond patrolling the mountains at Easter. Every year “Hjelpekorps” help over 1000 people who get lost or injured during outdoor activities. One of the main challenges the Hjelpekorps have is search and rescue in arctic environment.

The Norwegian Search and Rescue organizations (SAR) are mainly based on volunteer work (Hjelpekorpset is one of them), some financing comes from the government but most of the financing the SAR groups need to raise by them self. One way of raising funds is by doing transportation work by snowmobiles. Thus, there is a need for multipurpose sleds that can be used for all of the different operations/ work Hjelpekorpset do during the winter.

Problem description

Short about the problem: The sleds that exist today have often very specified area of application, there is a need for a sled that can be used for all operation/transport mission that the Norwegian volunteer SAR organizations carries out. The sled must be reliable, easy to maneuver in difficult terrain.  Area of application for the sled:

- Transport of various equipment for use during SAR-operation
- Transport of patients.
- General transportation of; firewood, gas, gasoline, furniture etc. (The volunteer SAR organizations in Norway often do transportation work to private huts etc.)

The work shall include:

1. **A literature study** both in terms of finding state-of –the art for these types of products, existing equipment on the market and potential competitors, as well as other literature that is necessary with a view to solving the problem (regulations, standards for materials, patents etc.). Existing equipment described with respect to behaviour, structure, performance, weight, and size.
2. **Develop a specification** for the product based on demands for performance under the given physical conditions, requirements for stiffness, strength, weight, reliability, comfort, regulations and other requirements and demands of the customer.
3. **Conduct a systematic design** ending up with a final proposal to the technical solution for the product/system.
4. **Analysis of the product/system** shall be made in order to determine which aspects/ parts of the system/ product should undergo numerical and analytical calculations.
5. **Modelling of the system** in a 3D parametric CAD system and simulation/visualization of for instance movements. A set of 2D drawings should be generated. These drawings should include assembled drawings of the system in open and closed position and complete part production drawings with tolerances.
6. **Modelling and numerical analysis** of the product/ system will (also) be carried out using an appropriate numerical calculation tool (such as Ansys) and should be compared with the analytical calculations of the product / system.
7. **Construction/making** a (physical) prototype or a model of the product/system/structure.
8. **Suggestions** for future work and description of remaining work
The solution of the task should be based on typical engineering design methods and areas of study for the Master Program Engineering Design at UiT – campus Narvik.

General information

This master thesis should include:
- Preliminary work/literature study related to actual topic
  - A state-of-the-art investigation
  - An analysis of requirement specifications, definitions, design requirements, given standards or norms, guidelines and practical experience etc.
  - Description concerning limitations and size of the task/project
  - Estimated time schedule for the project/thesis
- Selection & investigation of actual materials
- Development (creating a model or model concept)
- Experimental work (planned in the preliminary work/literature study part)
- Suggestion for future work/development

Limitations of the task/project
Eventual ownership of product and documentation, restrictions and closure to be filled up here.

Preliminary work/literature study

After the task description has been distributed to the candidate a preliminary study should be completed within 4 weeks. It should include bullet points 1 and 2 in “The work shall include”, and a plan of the progress. The preliminary study may be submitted as a separate report or “natural” incorporated in the main thesis report. A plan of progress and a deviation report (gap report) can be added as an appendix to the thesis.

In any case the preliminary study report/part must be accepted by the supervisor before the student can continue with the rest of the master thesis. In the evaluation of this thesis emphasis will be placed on the thorough documentation of the work performed.

Reporting requirements

The thesis should be submitted as a research report and should include the following parts; Abstract, Introduction, Material & Methods, Results & Discussion, Conclusions, Acknowledgements, Bibliography, References and Appendices. Choices should be well documented with evidence, references, or logical arguments.

The candidate should in this thesis strive to make the report survey-able, testable, accessible, well written, and documented.

Materials which are developed during the project (thesis) such as software/codes or physical equipment are considered to be a part of this paper (thesis). Documentation for correct use of such information should be added, as far as possible, to this paper (thesis).

The text for this task should be added as an appendix to the report (thesis).
Appendix A

The report (Abstract, Introduction, Material & Methods, Results & Discussion, Conclusions, Acknowledgements, Bibliography, References) should not exceed 50 pages. Any additional material should be included in the appendix.

General project requirements
If the tasks or the problems are performed in close cooperation with an external company, the candidate should following the guidelines or other directives given by the management of the company.

The candidate does not have the authority to enter or access external companies’ information system, production equipment or likewise. If such should be necessary for solving the task in a satisfactory way a detailed permission should be given by the management in the company before any action are made.

Any travel cost, printing and phone cost must be covered by the candidate themselves, if and only if, this is not covered by an agreement between the candidate and the management in the enterprises.

If the candidate enters some unexpected problems or challenges during the work with the tasks and these will cause changes to the work plan, it should be addressed to the supervisor at the UiT Campus Narvik or the person which is responsible, without any delay in time.

Submission requirements
This thesis should result in a final report with an electronic copy (i.e. CD/DVD, memory stick) of the report included appendices and necessary software codes, simulations and calculations. The final report with its appendices will be the basis for the evaluation and grading of the thesis. The report with all materials should be delivered in one signed loose-leaf copy, together with three bound. If there is an external company that needs a copy of the thesis, the candidate must arrange this. A standard front page, which can be found on the UiT Campus Narvik internet site, should be used. Otherwise, refer to the “General guidelines for thesis” and the subject description for master thesis.

The final report with its appendices should be submitted no later than the decided final date. The final report should be delivered to the adviser at the office of the Department of Computer Science and Computational Engineering.

Date of distributing the task: 6.6.2017
Date for submission (deadline): 6.6.2017

Contact information
Supervisor at the UiT Campus Narvik: Guy Mauseth
Phone: e-mail: guy.b.mauseth@uit.no
Supervisor at the UiT Campus Narvik
Andreas Seger
Phone:
e-mail:

Candidate contact information
Kari Wilhelmsen Johansen
Phone:
e-mail: kjo141@post.uit.no
## Appendix B

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<th>ITEM NO.</th>
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<th>Weight [g]</th>
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<td>Plywood</td>
<td>5473.94</td>
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**DATE:** 30.3.2017  
**TITLE:** Detachable Frame  
**DRAWN BY:** Kari Wilhelmsen Johansen  
**APPROVED BY:** Kari Wilhelmsen Johansen  
**WEIGHT:** 16997.82  
**SCALE:** 1:100  
**DWG NO.:** A4  
**MATERIAL:** N/A
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1: Longside

SOLIDWORKS Student Edition, For Academic Use Only.

MATERIAL: Plywood
SCALE: 1:10
Dwg No. A4

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2: Hinge

UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

2: Hinge

SOLIDWORKS Student Edition.
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FRAME
3: Short side

UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

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Kari Wilhelmsen Johansen
30.3.2017

Kari Wilhelmsen Johansen
6.6.2017

2951.44 g

FRAME

MATERIAL: Plywood
SCALE: 1:5
SHEET 5 OF 9
UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

FRAME

5: Formed Hexscrew

MATERIAL: Aluminium Al 6061
SCALE: 5:1
SHEET 7 OF 9

NAME: SolidWorks Design Library Toolbox ANSI Metric

NAME: Kari Wilhelmsen Johansen

DATE: 6.6.2017

WEIGHT: 0.9105

DRAWN: SolidWorks Design Library Toolbox ANSI Metric

APPV'D: Kari Wilhelmsen Johansen

UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS
UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

6: AM A M2X25-N Pin

FRAME

SOLIDWORKS Student Edition.
For Academic Use Only.

DRAWN: SolidWorks Design Library Toolbox ANSI Metric
APPVD: Kari Wilhelmsen Johansen

DATE: 6.6.2017

0.24 g

MATERIAL: Aluminium Al 6061
SCALE: 5:1

Sheet 8 of 9
UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

SOLIDWORKS Student Edition.
For Academic Use Only.

NAME: Kari Wilhelmsen Johansen
DATE: 30.3.2017

NAME: Kari Wilhelmsen Johansen
DATE: 6.6.2017

FRAME

MATERIAL: Aluminium Al 6061
SCALE: 2:1

7: Click lock

3.91 g
Age-hardening wrought Al-alloys

Description

Figure 1: 1. A close-up of building cladding made from wrought aluminum alloy. © John Fernandez 2. Chassis of a personal computer. © Chris Lefteri 3. The 2000 and 7000 series age-hardening aluminum alloys are the backbone of the aerospace industry.

The material
The high-strength aluminum alloys rely on age-hardening: a sequence of heat treatment steps that causes the precipitation of a nano-scale dispersion of intermetallics that impede dislocation motion and impart strength. This can be as high as 700 MPa giving them a strength-to-weight ratio exceeding even that of the strongest steels. This record describes for the series of wrought Al alloys that rely on age-hardening requiring a solution heat treatment followed by quenching and ageing. This is recorded by adding TX to the series number, where X is a number between 0 and 8 that records the state of heat treatment. They are listed below using the IADS designations (see Technical notes for details).

- **2000 series**: Al + 2 to 6% Cu -- the oldest and most widely used aerospace series.
- **6000 series**: Al + up to 1.2% Mg and 1.3% Si -- medium strength extrusions and forgings.
- **7000 series**: Al with up to 8% Zn and 3% Mg -- the Hercules of aluminum alloys, used for high strength aircraft structures, forgings and sheet. Certain special alloys also contain silver. So this record, like that for the non-age hardening alloys, is broad, encompassing all of these.

Compositional summary
- **2000 series**: Al + 2 to 6% Cu + Fe, Mn, Zn and sometimes Zr
- **6000 series**: Al + up to 1.2%Mg + 0.25% Zn + Si, Fe and Mn
- **7000 series**: Al + 4 to 9 % Zn + 1 to 3% Mg + Si, Fe, Cu and occasionally Zr and Ag

General properties

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Mechanical properties

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<td>Bulk modulus</td>
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Poisson’s ratio 0.32 - 0.36
Yield strength (elastic limit) 95 - 610 MPa
Tensile strength 180 - 620 MPa
Compressive strength 95 - 610 MPa
Elongation 1 - 20 % strain
Hardness - Vickers 60 - 160 HV
Fatigue strength at 10^7 cycles 57 - 210 MPa
Fracture toughness 21 - 35 MPa.m^0.5
Mechanical loss coefficient (tan delta) 1e-4 - 0.001

**Thermal properties**
Melting point 495 - 640 °C
Maximum service temperature 120 - 200 °C
Minimum service temperature -273 °C
Thermal conductor or insulator? Good conductor
Thermal conductivity 118 - 174 W/m.°C
Specific heat capacity 890 - 1,02e3 J/kg.°C
Thermal expansion coefficient 22 - 24 µstrain/°C

**Electrical properties**
Electrical conductor or insulator? Good conductor
Electrical resistivity 3.8 - 6 µohm.cm

**Optical properties**
Transparency Opaque

**Processability**
Castability 4 - 5
Formability 3 - 4
Machinability 4 - 5
Weldability 3 - 4
Solder/brazability 2 - 3

**Eco properties**
Embodied energy, primary production * 198 - 219 MJ/kg
CO2 footprint, primary production * 12.2 - 13.4 kg/kg
Recycle False

**Supporting information**

**Design guidelines**
The age-hardening alloys have exceptional strength at low weight, but the origin of the strength -- age hardening -- imposes certain design constraints. At its simplest, age-hardening involves a three step heat treatment.

Step 1: the wrought alloy, as sheet, extrusion or forging, is solution heat treated -- held for about 2 hours at around 550 C (it depends on the alloys) to make the alloying elements (Cu, Zn, Mg, Si etc) dissolve.

Step 2: the material is quenched from the solution-treatment temperature, typically by dunking or spraying it with cold water. This traps the alloying elements in solution. Quenching is a savage treatment that can cause distortion and create internal stresses that may require correction, usually by rolling.
Step 3: the material is aged, meaning that it is heated to between 120 and 190 °C for about 8 hours during which the alloying elements condense into nano-scale dispersions of intermetallics (CuAl, CuAl2, Mg2Si and the like). It is this dispersion that gives the strength.

The result is a material that, for its weight, has remarkably high strength and corrosion resistance. But if it is heated above the solution treatment temperature -- by welding, for example -- the strength is lost. This means that assembly requires fasteners such as rivets, usual in airframe construction, or adhesives. Some 6000 series alloys can be welded, but they are of medium rather than high strength.

**Technical notes**

Until 1970, designations of wrought aluminum alloys were a mess; in many countries, they were simply numbered in the order of their development. The International Alloy Designation System (IADS), now widely accepted, gives each wrought alloy a 4-digit number. The first digit indicates the major alloying element or elements. Thus the series 1xxx describe unalloyed aluminum; the 2xxx series contain copper as the major alloying element, and so forth. The third and fourth digits are significant in the 1xxx series but not in the others; in 1xxx series they describe the minimum purity of the aluminum; thus 1145 has a minimum purity of 99.45%; 1200 has a minimum purity of 99.00%. In all other series, the third and fourth digits are simply serial numbers; thus 5082 and 5083 are two distinct aluminum-magnesium alloys. The second digit has a curious function: it indicates a close relationship: thus 5352 is closely related to 5052 and 5252; and 7075 and 7475 differ only slightly in composition. To these serial numbers are added a suffix indicating the state of hardening or heat treatment. The suffix F means 'as fabricated'. Suffix O means 'annealed wrought products'. The suffix H means that the material is 'cold worked'. The suffix T means that it has been 'heat treated'. More information on designations and equivalent grades can be found on the Granta Design website at www.grantadesign.com/designations
Phase diagram

Figure 2: The 2000 series of wrought aluminum alloys are based on aluminum (Al) with 2.5 - 6% copper (Cu). This is the relevant part of the phase diagram.

Typical uses
2000 and 7000 series: aerospace structures, pressure vessels, ultralight land-based transport systems; sports equipment such as golf clubs and bicycles.
6000 series: cladding and roofing; medium strength extrusions, forgings and welded structures for general engineering and automotive such as connecting rods.

Values marked * are estimates.
No warranty is given for the accuracy of this data

Reference
CES EduPack 2016, datasheet Age-hardening wrought Al-alloys
Force (F) 18518.51852 N
Length (L) 0.9 m
Density (ρ) 2900 kg/m³
Youngs (E) 68000000000 Mpa

\[ m = \left(12F\right)^{\frac{1}{2}} \left(\frac{L}{\pi}\right) \left(\frac{1}{E}\right) \]

Mass 1,351675465 kg

\[ b^2 = \left(\frac{12FL^2}{\pi^2E}\right)^{\frac{1}{3}} \]

width 0.02275705 m
22,7570499 mm
Area 0.000517883 m²

First iteration after material selection; Setting b1, finding b2
b1 0.015 m
A1 0.000225 m²
b2 0.027255886 m
A2 0.000742883 m²

After FEA analysis; setting b2, finding b1, different sidelengths in y and x directions
b2x 0.04 m
b2y 0.035 m
a2 0.0014 m²
relationship y and x 0.875
a1 0.000882117 m²
b1 0.029700449 m
b1x 0.03394337 m
b1y 0.025987893 m

Acceleration
Speed 100 km/h
27,77778 m/s
Time 1.5 s
Plywood

Description

The material

Plywood is laminated wood, the layers glued together such that the grain in successive layers are at right angles, giving stiffness and strength in both directions. The number of layers varies, but is always odd (3, 5, 7…) to give symmetry about the core ply - if it is asymmetric it warps when wet or hot. Those with few plies (3,5) are significantly stronger and stiffer in the direction of the outermost layers; with increasing number of plies the properties become more uniform. High quality plywood is bonded with synthetic resin. The data listed below describe the in-plane properties of a typical 5-ply.

Compositional summary

Cellulose/Hemicellulose/Lignin/12%H2O/Adhesive

General properties

<table>
<thead>
<tr>
<th>Property</th>
<th>Range</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density</td>
<td>700 - 800</td>
<td>kg/m^3</td>
</tr>
<tr>
<td>Price</td>
<td>* 4.87 - 5.4</td>
<td>NOK/kg</td>
</tr>
<tr>
<td>Date first used</td>
<td>1907</td>
<td></td>
</tr>
</tbody>
</table>

Mechanical properties

<table>
<thead>
<tr>
<th>Property</th>
<th>Range</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Young's modulus</td>
<td>6.9 - 13</td>
<td>GPa</td>
</tr>
<tr>
<td>Shear modulus</td>
<td>* 0.5 - 2</td>
<td>GPa</td>
</tr>
<tr>
<td>Bulk modulus</td>
<td>* 1.6 - 2.5</td>
<td>GPa</td>
</tr>
<tr>
<td>Poisson's ratio</td>
<td>0.22 - 0.3</td>
<td></td>
</tr>
<tr>
<td>Yield strength (elastic limit)</td>
<td>* 9 - 30</td>
<td>MPa</td>
</tr>
<tr>
<td>Tensile strength</td>
<td>10 - 44</td>
<td>MPa</td>
</tr>
<tr>
<td>Compressive strength</td>
<td>8 - 25</td>
<td>MPa</td>
</tr>
<tr>
<td>Elongation</td>
<td>2.4 - 3</td>
<td>% strain</td>
</tr>
<tr>
<td>Hardness - Vickers</td>
<td>3 - 9</td>
<td>HV</td>
</tr>
<tr>
<td>Fatigue strength at 10^7 cycles</td>
<td>* 7 - 16</td>
<td>MPa</td>
</tr>
<tr>
<td>Fracture toughness</td>
<td>* 1 - 1.8</td>
<td>MPa.m^0.5</td>
</tr>
<tr>
<td>Mechanical loss coefficient (tan delta)</td>
<td>* 0.008 - 0.11</td>
<td></td>
</tr>
</tbody>
</table>
**Thermal properties**

- **Glass temperature**: 120 - 140 °C
- **Maximum service temperature**: *100 - 130 °C
- **Minimum service temperature**: *-100 - -70 °C
- **Thermal conductor or insulator?**: Good insulator
- **Thermal conductivity**: 0,3 - 0,5 W/m.°C
- **Specific heat capacity**: 1,66e3 - 1,71e3 J/kg.°C
- **Thermal expansion coefficient**: 6 - 8 μstrain/°C

**Electrical properties**

- **Electrical conductor or insulator?**: Poor insulator
- **Electrical resistivity**: 6e13 - 2e14 μohm.cm
- **Dielectric constant (relative permittivity)**: 6 - 8
- **Dissipation factor (dielectric loss tangent)**: *0,05 - 0,09
- **Dielectric strength (dielectric breakdown)**: *0,4 - 0,6 1000000 V/m

**Optical properties**

- **Transparency**: Opaque

**Processability**

- **Moldability**: 3 - 4
- **Machinability**: 5

**Eco properties**

- **Embodied energy, primary production**: *13,8 - 15,2 MJ/kg
- **CO2 footprint, primary production**: *0,786 - 0,869 kg/kg
- **Recycle**: Recycle

**Supporting information**

**Design guidelines**

Plywoods offers high strength at low weight. Those for general construction are made from softwood plys, but the way in which plywood is made allows for great flexibility. For aesthetic purposes, hardwoods can be used for the outermost plys, giving "paneling plywoods" faced with walnut, mahogany or other expensive woods on a core of softwood. Those for ultra-light design have hardwood outer plys on a core of balsa. Metal-faced plywoods can be riveted. Curved moldings for furniture such as chairs are made by laying-up the unbonded plys in a shaped mold and curing the adhesive under pressure using an airbag or matching mold. Singly curved shapes are straightforward; double curvatures should be minimized or avoided.

**Technical notes**

Low cost plywoods are bonded with starch or animal glues and are not water resistant -- they are used for boxes and internal construction. Waterproof and marine plywoods are bonded with synthetic resin -- they are used for external paneling and general construction.

**Typical uses**

Furniture, building and construction, marine and boat building, packaging, transport and vehicles, musical instruments, aircraft, modeling.
Values marked * are estimates.
No warranty is given for the accuracy of this data

**Reference**

CES EduPack 2016 Datasheet Plywood
Investment casting

Description

The process
If you have gold fillings (or more elaborate metal work) in your mouth, be thankful for this process - it was used to make them. The lost wax process - the old name for INVESTMENT CASTING - has been practiced for at least three thousand years; sophisticated jewelry, ornaments and icon were being made in Egypt and Greece well before 1500BC. In investment casting, wax patterns are made and assembled (if small) into a tree with feeding and gating systems. The assembled pattern is dipped into refractory slurry, then covered in refractory stucco and allowed to dry. The procedure is repeated a number of times until about 8 layers have built up, creating a ceramic investment shell. The wax is then melted out and the ceramic shell fired before the molten metal is cast. Gravity die casting is adequate for simple shapes, but air pressure, vacuum or centrifugal pressure is needed to give complete filling of the mold when complex, thin sections are involved. The mold is broken up to remove the castings. The process is suitable for most metals of melting temperatures below 2200 C. Because the wax pattern is melted out, the shape can be very complex, with contours, undercuts, bosses, and recesses. For making hollow shapes, this process is very sophisticated: all large bronze statues are hollow, and they are made by an elaboration of this process.

Tradenames
Lost wax casting

Material compatibility
Metals - ferrous False
Metals - non-ferrous False
Shape
Circular prismatic True
Non-circular prismatic False
Solid 3-D False
Hollow 3-D False

Economic compatibility
Relative tooling cost low
Relative equipment cost medium
Labor intensity high
Economic batch size (units) 1 - 1e4

Physical and quality attributes
Mass range 0.01 - 20 kg
Range of section thickness 1 - 75 mm
Tolerance 0.05 - 0.25 mm
Roughness 0.5 - 3.2 µm
Surface roughness (A=v. smooth) A

Process characteristics
Primary shaping processes False
Discrete False
Prototyping False

Cost model and defaults
Relative cost index (per unit) * 922 - 4,48e3

Parameters: Material Cost = 70.9NOK/kg, Component Mass = 1kg, Batch Size = 1e3, Overhead Rate = 1,33e3NOK/hr, Discount Rate = 5%, Capital Write-off Time = 5yrs, Load Factor = 0.5

Capital cost 2,91e3 - 1,45e4 NOK
Material utilization fraction 0.8 - 0.85
Production rate (units) 1 - 200 /hr
Tooling cost  
* 726  -  7,26e3  NOK  
Tool life (units)  
* 1  -  5

Supporting information

Design guidelines
The process is extremely versatile, allowing great freedom of form. It offers excellent reproduction of detail in small 3D components.

Technical notes
Investment casting is one of the few processes that can be used to cast metals with high melting temperatures to give complex shapes; it can also be used for low melting metals. The traditional uses of investment casting were for the shaping of silver, copper, gold, bronze, pewter and lead. Today the most significant engineering applications are those for nickel, cobalt and iron-based alloys.

Typical uses
Jewelry, dental implants, statuary, metal sculpture and decorative objects, blades for high temperature gas turbines and similar equipment.

The economics
Investment casting lends itself both to small and large batch sizes. For small batch sizes the process is manual, with low capital and tooling costs, but significant labor costs. When automated, the capital costs are high, but quality control and speed are greater. The production rate is increased by the use of multiple molds.

The environment
There are the usual hazards associated with casting molten metal, but procedures for dealing with these are routine. The mold materials cannot, at present, be recycled.

Values marked * are estimates.
No warranty is given for the accuracy of this data

Reference
CES EduPack Datasheet Investment Casting
Appendix G: Simulation of TOWBAR

Date: 29. may 2017
Designer: Kari Wilhelmsen Johansen
Study name: Towbar Static
Analysis type: Static

Table of Contents
Description ........................................... 1
Design improvements ................................ 2
Model Information .................................... 3
Study Properties ..................................... 6
Units ..................................................... 6
Material Properties .................................. 7
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Contact Information ............................... 9
Mesh information ................................. 9
Resultant Forces ................................... 11
Study Results ........................................ 11
Conclusion ........................................... 14
Table of figures ...................................... 15

Description
Static analysis of the towbar with applied forces from the sled itself and the snowmobile accelerating and turning simultaneously. The analysis is performed in the simulation tool in SolidWorks Educational edition for the academic year 2015-2016.

Changes done in the design after the first analysis: Profile of the attachment ring increased by 5 mm and the design is fitted to welding. The material of the ring changed to titanium alloy Ti-6Al-2Sn-2Zr-2Mo-2Cr-0.25Si (SS), and the profile of the rods are increased from 35x35 mm to 35x40 mm solid profiles.

These changes resulted in large improvement of von Mises stress, displacement and strain.
Design improvements

After the first analysis, it became clear that the profiles of the towbar and the design of the ring needed some alterations. The following changes were done in the design:

- The profile of the attachment ring were increased by 5 mm, the design were changed from a simple ring with a rod to a weldable fit to the towbar. The material of the ring were changed from 6061 Aluminium alloy to 201 Annealed stainless steal, which gave a increase in Young’s modulus of 33,33%.
- The rod that attaches the ring to the rest of the structure were at first shortened so that the length fits the rest of the structure, but ultimately had to be deleted from the design in order to attempt to reduce the Von Mises stress.
- Profile of the towbar rods were increased from 35x35 mm to 35x40 mm with inner side lengths 25x33 mm.

Regarding the applied forces, the calculated forces acting on the system in both directions were somewhat altered as well:

- In the first analysis, a small force of 500 N were applied on the hinge joints. Further studies of the situation showed this was unnecessary. The force were too small to have a large impact on the results and the result is therefore included.
- The force acting on the attachment ring, acting as the snowmobile accelerating and turning simultaneously, where decreased by 5500 N due to calculation errors.

Additionally, the meshing of the towbar have been refined.
### Model Information

**Model name:** TOWBAR  
**Current Configuration:** Default

<table>
<thead>
<tr>
<th>Solid Bodies</th>
<th>Treated As</th>
<th>Volumetric Properties</th>
<th>Date Modified</th>
</tr>
</thead>
</table>
| Hingejoint hinge/ 2 | Solid Body | Mass: 0.125547 kg  
Volume: 4.64987e-005 m^3  
Density: 2700 kg/m^3  
Weight: 1.23036 N | May 16 15:36:49 2017 |
| Hingejoint plate/ 2 | Solid Body | Mass: 0.0845562 kg  
Volume: 3.13171e-005 m^3  
Density: 2700 kg/m^3  
Weight: 0.828651 N | May 16 15:39:03 2017 |
<table>
<thead>
<tr>
<th>Component</th>
<th>Mass</th>
<th>Volume</th>
<th>Density</th>
<th>Weight</th>
<th>Date</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hingejoint Rubber tube / 2</td>
<td>0.00424115 kg</td>
<td>4.41786e-006 m³</td>
<td>960 kg/m³</td>
<td>0.0415633 N</td>
<td>May 16 15:40:02 2017</td>
</tr>
<tr>
<td>Hingejoint side / 4</td>
<td>0.0100374 kg</td>
<td>7.06858e-006 m³</td>
<td>1420 kg/m³</td>
<td>0.0983664 N</td>
<td>May 16 15:43:53 2017</td>
</tr>
<tr>
<td>Attachment ring / 1</td>
<td>0.17751 kg</td>
<td>3.81742e-005 m³</td>
<td>4650 kg/m³</td>
<td>1.7396 N</td>
<td>May 29 11:07:07 2017</td>
</tr>
<tr>
<td>Hingejoint Hex Screw / 2</td>
<td>0.0155823 kg</td>
<td>5.71222e-006 m³</td>
<td>2700 kg/m³</td>
<td>0.152707 N</td>
<td>May 29 11:40:48 2017</td>
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<td>Hingejoint Hex Nut Style 11 / 2</td>
<td>0.00353385 kg</td>
<td>1.30883e-006 m³</td>
<td>2700 kg/m³</td>
<td>0.0346317 N</td>
<td>May 29 11:41:18 2017</td>
</tr>
<tr>
<td>Connection rods 1 and 2 / 1</td>
<td>0.155311 kg</td>
<td>5.75225e-005 m³</td>
<td>2700 kg/m³</td>
<td>1.52205 N</td>
<td>May 28 17:20:14 2017</td>
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</table>
| Rod 1 / 2 | Solid Body | Mass: 0.836496 kg  
Volume: 0.000309813 m^3  
Density: 2700 kg/m^3  
Weight: 8.19766 N | May 29 10:19:53 2017 |
|-----------|------------|-------------------------------------------------|
| Rod 2 / 1 | Solid Body | Mass: 0.836496 kg  
Volume: 0.000309813 m^3  
Density: 2700 kg/m^3  
Weight: 8.19766 N | May 29 10:19:53 2017 |
### Study Properties

<table>
<thead>
<tr>
<th>Study name</th>
<th>Towbar Static</th>
</tr>
</thead>
<tbody>
<tr>
<td>Analysis type</td>
<td>Static</td>
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<td>Mesh type</td>
<td>Solid Mesh</td>
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<td>Thermal Effect</td>
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<td>Thermal option</td>
<td>Include temperature loads</td>
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<td>Include fluid pressure effects from SOLIDWORKS Flow Simulation</td>
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<td>Inplane Effect</td>
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<td>Soft Spring</td>
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<td>Inertial Relief</td>
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<td>Incompatible bonding options</td>
<td>Automatic</td>
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<td>Large displacement</td>
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<tr>
<td>Compute free body forces</td>
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<tr>
<td>Friction</td>
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<tr>
<td>Use Adaptive Method</td>
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### Units

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<th>SI (MKS)</th>
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<tr>
<td>Length/Displacement</td>
<td>mm</td>
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<tr>
<td>Temperature</td>
<td>Kelvin</td>
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<tr>
<td>Angular velocity</td>
<td>Rad/sec</td>
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<tr>
<td>Pressure/Stress</td>
<td>N/m^2</td>
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# Material Properties

<table>
<thead>
<tr>
<th>Model Reference</th>
<th>Properties</th>
<th>Components</th>
</tr>
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<tbody>
<tr>
<td><img src="image1.jpg" alt="Image" /></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Name:</strong> 6061 Alloy</td>
<td><strong>Model type:</strong> Linear Elastic Isotropic</td>
<td><strong>HINGEJOINT-1 hengsel-1,</strong> <strong>HINGEJOINT-1 plate-1,</strong> <strong>HINGEJOINT-2 hengsel-1,</strong> <strong>HINGEJOINT-2 plate-1,</strong> <strong>TOWBAR connection rods 1 and 2-1,</strong> <strong>TOWBAR rod-1,</strong> <strong>TOWBAR rod-2,</strong> <strong>formed hex screw_am2-1,</strong> <strong>formed hex screw_am2-2,</strong> <strong>hex nut style 11_am-1,</strong> <strong>hex nut style 11_am-2</strong></td>
</tr>
<tr>
<td><strong>Model type:</strong> Linear Elastic Isotropic</td>
<td><strong>Default failure criterion:</strong> Unknown</td>
<td></td>
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<tr>
<td><strong>Yield strength:</strong> 5.51485e+007 N/m^2</td>
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<td></td>
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<tr>
<td><strong>Tensile strength:</strong> 1.24084e+008 N/m^2</td>
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<td></td>
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<tr>
<td><strong>Elastic modulus:</strong> 6.9e+010 N/m^2</td>
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<tr>
<td><strong>Poisson’s ratio:</strong> 0.33</td>
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<tr>
<td><strong>Mass density:</strong> 2700 kg/m^3</td>
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</tr>
<tr>
<td><strong>Shear modulus:</strong> 2.6e+010 N/m^2</td>
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<tr>
<td><strong>Thermal expansion coefficient:</strong> 2.4e-005 /Kelvin</td>
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<tr>
<td><img src="image2.jpg" alt="Image" /></td>
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<tr>
<td><strong>Name:</strong> Natural Rubber</td>
<td><strong>Model type:</strong> Linear Elastic Isotropic</td>
<td><strong>HINGEJOINT-1 rubber tube-1,</strong> <strong>HINGEJOINT-2 rubber tube-1</strong></td>
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<tr>
<td><strong>Default failure criterion:</strong> Unknown</td>
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<tr>
<td><strong>Tensile strength:</strong> 2e+007 N/m^2</td>
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<td><strong>Elastic modulus:</strong> 10000 N/m^2</td>
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<td><strong>Poisson’s ratio:</strong> 0.45</td>
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<tr>
<td><strong>Mass density:</strong> 960 kg/m^3</td>
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<tr>
<td><img src="image3.jpg" alt="Image" /></td>
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<tr>
<td><strong>Name:</strong> PET</td>
<td><strong>Model type:</strong> Linear Elastic Isotropic</td>
<td><strong>HINGEJOINT-1 sides-1,</strong> <strong>HINGEJOINT-1 sides-2,</strong> <strong>HINGEJOINT-2 sides-1,</strong> <strong>HINGEJOINT-2 sides-2</strong></td>
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<tr>
<td><strong>Default failure criterion:</strong> Unknown</td>
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<tr>
<td><strong>Tensile strength:</strong> 5.73e+007 N/m^2</td>
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<td><strong>Compressive strength:</strong> 9.29e+007 N/m^2</td>
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<tr>
<td><strong>Elastic modulus:</strong> 2.96e+009 N/m^2</td>
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<td><strong>Poisson’s ratio:</strong> 0.37</td>
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<tr>
<td><img src="image4.jpg" alt="Image" /></td>
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<tr>
<td><strong>Name:</strong> Ti-6Al-2Sn-2Zr-2Mo-2Cr-0.25Si (SS)</td>
<td><strong>Model type:</strong> Linear Elastic Isotropic</td>
<td><strong>TOWBAR attachment ring-1</strong></td>
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<tr>
<td><strong>Default failure criterion:</strong> Unknown</td>
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<tr>
<td><strong>Yield strength:</strong> 1.07e+009 N/m^2</td>
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<tr>
<td><strong>Tensile strength:</strong> 1.16e+009 N/m^2</td>
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<td><strong>Compressive strength:</strong> 1.23e+011 N/m^2</td>
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<tr>
<td><strong>Elastic modulus:</strong> 1.17e+009 N/m^2</td>
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<td><strong>Poisson’s ratio:</strong> 0.33</td>
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<tr>
<td><strong>Mass density:</strong> 4650 kg/m^3</td>
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<tr>
<td><strong>Shear modulus:</strong> 4.6e+010 N/m^2</td>
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<tr>
<td><strong>Thermal expansion coefficient:</strong> 9e-006 /Kelvin</td>
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## Loads and Fixtures

<table>
<thead>
<tr>
<th>Fixture name</th>
<th>Fixture Image</th>
<th>Fixture Details</th>
</tr>
</thead>
</table>
| Fixed Hinge-1   | ![Fixed Hinge-1](image) | **Entities:** 4 face(s)  
Type: Fixed Hinge |

### Resultant Forces

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<th>Components</th>
<th>X</th>
<th>Y</th>
<th>Z</th>
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<td>Reaction force(N)</td>
<td>0.000610352</td>
<td>-420.555</td>
<td>19995.6</td>
<td>20000</td>
</tr>
<tr>
<td>Reaction Moment(N.m)</td>
<td>0</td>
<td>0</td>
<td>0</td>
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### Load Details

<table>
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<tr>
<th>Load name</th>
<th>Load Image</th>
<th>Load Details</th>
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| Gravity-1 | ![Gravity-1](image) | **Reference:** Face < 1 >  
Values: 0 0 -9.81  
Units: SI |
| Force-1   | ![Force-1](image) | **Entities:** 1 face(s)  
Reference: Edge < 1 >  
Type: Apply force  
Values: ---, ---, 20000 N |
## Contact Information

<table>
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<th>Contact Image</th>
<th>Contact Properties</th>
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</thead>
</table>
|                | ![Contact Set-53](image) | Type: No Penetration contact pair  
Entites: 3 face(s)  
Advanced: Node to surface |

<table>
<thead>
<tr>
<th>Global Contact</th>
<th>Contact Image</th>
<th>Contact Properties</th>
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</table>
|                | ![Global Contact](image) | Type: Bonded  
Components: 1 component(s)  
Options: Incompatible mesh |

### Mesh information

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<th>Solid Mesh</th>
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<td>Standard mesh</td>
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<td>Automatic Transition:</td>
<td>Off</td>
</tr>
<tr>
<td>Include Mesh Auto Loops:</td>
<td>Off</td>
</tr>
<tr>
<td>Jacobian points</td>
<td>4 Points</td>
</tr>
<tr>
<td>Element Size</td>
<td>7.70942 mm</td>
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<tr>
<td>Tolerance</td>
<td>0.385471 mm</td>
</tr>
<tr>
<td>Mesh Quality</td>
<td>Draft Quality Mesh</td>
</tr>
<tr>
<td>Remesh failed parts with incompatible mesh</td>
<td>On</td>
</tr>
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</table>
### Mesh information - Details

<p>| | |</p>
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<td><strong>Total Nodes</strong></td>
<td>13126</td>
</tr>
<tr>
<td><strong>Total Elements</strong></td>
<td>40031</td>
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<tr>
<td><strong>Maximum Aspect Ratio</strong></td>
<td>81.555</td>
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<tr>
<td>% of elements with Aspect Ratio &lt; 3</td>
<td>68.4</td>
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<td>% of elements with Aspect Ratio &gt; 10</td>
<td>0.102</td>
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<tr>
<td>Time to complete mesh(hh:mm:ss):</td>
<td>00:00:16</td>
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<tr>
<td>Computer name:</td>
<td>NAR-E1570-08</td>
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**Figure 1**: Model of the towbar, drawn in SolidWorks with applied meshing.
### Resultant Forces

#### Reaction forces

<table>
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<tr>
<th>Selection set</th>
<th>Units</th>
<th>Sum X</th>
<th>Sum Y</th>
<th>Sum Z</th>
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<tr>
<td>Entire Model</td>
<td>N</td>
<td>0.000610352</td>
<td>-420.555</td>
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#### Reaction Moments

<table>
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<th>Units</th>
<th>Sum X</th>
<th>Sum Y</th>
<th>Sum Z</th>
<th>Resultant</th>
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<td>Entire Model</td>
<td>N.m</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
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### Study Results

#### Von Mises stress

<table>
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<tr>
<th>Name</th>
<th>Type</th>
<th>Min</th>
<th>Max</th>
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<tbody>
<tr>
<td>Stress1</td>
<td>VON: von Mises Stress</td>
<td>3.40517 N/m²</td>
<td>3.7023e+008 N/m²</td>
</tr>
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</table>
  
  
  
  Node: 1553
  
  Node: 1801

---

*Figure 2: Improved model of the towbar, drawn in SolidWorks with resulting von Mises stresses*
Figure 3: Close-up on towbar with maximum Von Mises stress
### Displacement

<table>
<thead>
<tr>
<th>Name</th>
<th>Type</th>
<th>Min</th>
<th>Max</th>
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<tr>
<td>Displacement1</td>
<td>URES: Resultant Displacement</td>
<td>0.000269449 mm</td>
<td>3.44939 mm</td>
</tr>
<tr>
<td>Node: 69</td>
<td>Node: 1874</td>
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Figure 4: Improved model of the towbar, drawn in SolidWorks with resulting deformation
Strain

<table>
<thead>
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<th>Name</th>
<th>Type</th>
<th>Min</th>
<th>Max</th>
</tr>
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<tbody>
<tr>
<td>Strain1</td>
<td>ESTRN: Equivalent Strain</td>
<td>1.65926e-010</td>
<td>0.00503221</td>
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</table>

Figure 5: Model of the towbar, drawn in SolidWorks with resulting strain and deformation

Conclusion

The Von Mises stress, deformation and the strain are all within acceptable limits and the design are satisfying.
### Table of figures

<table>
<thead>
<tr>
<th>Figure</th>
<th>Description</th>
<th>Page</th>
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<tr>
<td>1</td>
<td>Model of the towbar, drawn in SolidWorks with applied meshing</td>
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<td>2</td>
<td>Improved model of the towbar, drawn in SolidWorks with resulting von Mises stresses</td>
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<tr>
<td>3</td>
<td>Close-up on towbar with maximum Von Mises stress</td>
<td>12</td>
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<tr>
<td>4</td>
<td>Improved model of the towbar, drawn in SolidWorks with resulting deformation</td>
<td>13</td>
</tr>
<tr>
<td>5</td>
<td>Model of the towbar, drawn in SolidWorks with resulting strain and deformation</td>
<td>14</td>
</tr>
<tr>
<td>ITEM NO.</td>
<td>PART NUMBER</td>
<td>QTY.</td>
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<td>1</td>
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<tr>
<td>2</td>
<td>3D print Top plate</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>3D print TOWBAR rod 2</td>
<td>2</td>
</tr>
<tr>
<td>4</td>
<td>3D print TOWBAR connection rods 1 and 2</td>
<td>1</td>
</tr>
<tr>
<td>5</td>
<td>TOWBAR attachment ring</td>
<td>1</td>
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<tr>
<td>6</td>
<td>3D print SKI</td>
<td>2</td>
</tr>
<tr>
<td>7</td>
<td>3D print Railing handtakssøyle2</td>
<td>2</td>
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</table>

UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

NAME: Kari Wilhelmsen Johansen
DATE: 30.5.2017

3D print Sled

SOLIDWORKS Student Edition.
For Academic Use Only.

WEIGHT:
85963.93 g
UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

1: Bodystructure frame

3D print SLED

9229.28 g

NAME DATE TITLE:
Kari Wilhelmsen Johansen 30.5.2017 1: Bodystructure frame

SOLIDWORKS Student Edition.
For Academic Use Only.

MATERIAL: Aluminium Al6061

SCALE 1:10

WEIGHT: 9229.28 g

SHEET 3 OF 9
UNLESS OTHERWISE SPECIFIED:
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2: Top plate

3D print SLED

Kari Wilhelmsen Johansen 30.5.2017

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MATERIAL: Plywood
WEIGHT: 27130.08 g

Kari Wilhelmsen Johansen 30.5.2017

SOLIDWORKS Student Edition.
For Academic Use Only.

MATERIAL: Plywood
WEIGHT: 27130.08 g
3: Towbar rod

3D print SLED

SOLIDWORKS Student Edition.
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Material: Aluminium Al 6061

Weight: 5646.44 g

Scale: 1:5

SHEET 5 OF 9
4: Towbar connection rods 1 and 2

3D print SLED
5: Towbar attachment ring

3D print SLED

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UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS

7: Railing

3D print SLED

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SLED 2D drawings

Title: Snowmobile Sled

Designer: Kari Wilhelmsen Johansen
Date: 31.5.2017

SOLIDWORKS Student Edition.
For Academic Use Only.
<table>
<thead>
<tr>
<th>ITEM NO.</th>
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<th>QTY.</th>
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<tr>
<td>1</td>
<td>Ski</td>
<td>For illustrative purposes only</td>
<td>5000</td>
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<tr>
<td>2</td>
<td>Top plate</td>
<td>Plywood</td>
<td>10048.18</td>
<td>1</td>
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<td>4</td>
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<td>Aluminium AL6061 alloy</td>
<td>7483.58</td>
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<td>Aluminium AL6061 alloy</td>
<td>3638.35</td>
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<td>6</td>
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<td>Specified in sheet 2</td>
<td>2524.29</td>
<td>1</td>
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</table>

**Snowmobile sled**

**SOLIDWORKS Student Edition. For Academic Use Only.**

**DATE:** 29.5.2017

**APPV'D DATE:** 31.5.2017

**WEIGHT:** 41856.66 g

**DRAWN:** Kari Wilhelmsen Johansen

**NAME:** Kari Wilhelmsen Johansen

**DRAWN:** Kari Wilhelmsen Johansen

**NAME:** Kari Wilhelmsen Johansen

**TITLE:** Snowmobile sled

**SCALE:** 1:20

**SHEET:** 2 OF 17

**DWG NO.:** A4
### Appendix I

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<td>Titanium alloy (SS)</td>
<td>188.92</td>
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<td>8</td>
<td>Connection rods 1 and 2</td>
<td>Aluminium AL6061 alloy</td>
<td>155.31</td>
<td>1</td>
</tr>
<tr>
<td>9</td>
<td>Rod</td>
<td>Aluminium AL6061 alloy</td>
<td>836.5</td>
<td>2</td>
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<tr>
<td>10</td>
<td>HINGEJOINT plate</td>
<td>Aluminium AL6061 alloy</td>
<td>84.56</td>
<td>2</td>
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<td>HINGEJOINT hengsel</td>
<td>Aluminium AL6061 alloy</td>
<td>125.55</td>
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<td>12</td>
<td>HINGEJOINT rubber tube</td>
<td>Natural rubber</td>
<td>4.24</td>
<td>2</td>
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<td>13</td>
<td>HINGEJOINT sides</td>
<td>PET</td>
<td>10.04</td>
<td>4</td>
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<td>14</td>
<td>formed hex screw_am</td>
<td>Aluminium AL6061 alloy</td>
<td>15.58</td>
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<td>15</td>
<td>hex nut style_am</td>
<td>Aluminium AL6061 alloy</td>
<td>3.53</td>
<td>2</td>
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**SLED 2D drawings**

**SOLIDWORKS Student Edition.**

**For Academic Use Only.**

**TOWBAR**

**DRAWN:** Kari Wilhelmsen Johansen  
**DATE:** 29.5.2017  
**TITLE:**

**APPV'D:** Kari Wilhelmsen Johansen  
**DATE:** 31.5.2017  
**WEIGHT:** 2524.29  
**DWG NO.:** A42524.29  
**SCALE:** 1:10  
**SHEET:** 3 OF 17
2: Top-plate

SOLIDWORKS Student Edition.
For Academic Use Only.

Kari Wilhelmsen Johansen
15.4.2017

Kari Wilhelmsen Johansen
31.5.2017

Material: Plywood
Weight: 10048.18 g

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3: Railing 2

SLED 2D drawings

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4: Body structure frame

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SLED 2D drawings
5: Body structure support beam

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5: Body structure support beam

SLED 2D drawings

UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

<table>
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<th>NAME</th>
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<td></td>
<td>Kari wilhelmsen Johansen</td>
<td>29.5.2017</td>
<td>5: Body structure support beam</td>
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<th>APPV'D</th>
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<td>A4</td>
<td>3638.35 g</td>
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MATERIAL: Aluminium AL6061 alloy
SCALE: 1:5

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6: Towbar

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2524.29 g
UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

7: Attachment ring

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Kari wilhelmsen Johansen
31.5.2017

Titanium alloy (SS)
188.92 g

1:1 SHEET 9 OF 17

SLED 2D drawings

DRAWN
Kari wilhelmsen Johansen
31.5.2017

APPV'D
Kari wilhelmsen Johansen
31.5.2017

WEIGHT:
188.92 g

DATENAME
Kari wilhelmsen Johansen
31.5.2017
8: Connection rods 1 and 2

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9: Towbar rod

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<td>A4</td>
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</table>

MATERIAL: Aluminium AL6061 alloy
WEIGHT: 836.5 g

SLED 2D drawings

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Appendix I

10: Hingejoint plate

SLED 2D drawings

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Kari wilhelmsen Johansen
31.5.2017

Kari wilhelmsen Johansen
31.5.2017

Aluminium AL6061 alloy
84.56 g

UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

DIMENSIONS ARE IN MILLIMETERS
11: Hingejoint hinge

SLED 2D drawings
For Academic Use Only.

MATERIAL: Aluminium AL6061 alloy
WEIGHT: 125.55 g
SCALE: 1:1

NAME: Kari wilhelmsen Johansen
DATE: 31.5.2017

UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS
12: Hingejoint rubber tube

SOLIDWORKS Student Edition.
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Material: Natural rubber
Weight: 4.24 g

Dimensions are in millimeters.
<table>
<thead>
<tr>
<th>NAME</th>
<th>DATE</th>
<th>TITLE</th>
<th>DWG NO.</th>
<th>SCALE</th>
<th>SHEET</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kari wilhelmsen Johansen</td>
<td>31.5.2017</td>
<td>13: Hingejoint sides</td>
<td>A4</td>
<td>2:1</td>
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</table>

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**UNLESS OTHERWISE SPECIFIED:**
**DIMENSIONS ARE IN MILLIMETERS**

- **NAME**: Kari wilhelmsen Johansen
- **DATE**: 31.5.2017
- **TITLE**: 13: Hingejoint sides
- **DWG NO.**: A4
- **SCALE**: 2:1
- **MATERIAL**: PET
- **WEIGHT**: 10.04 g

**DRAWN**: Kari wilhelmsen Johansen
**APPPD**: Kari wilhelmsen Johansen

SLED 2D drawings

**APPV'D**: UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS

**NAME**: Kari wilhelmsen Johansen
**DATE**: 31.5.2017

**SOLIDWORKS Student Edition.**
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**APPV'D**: UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS

**NAME**: Kari wilhelmsen Johansen
**DATE**: 31.5.2017

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14: Hingejoint
Formed Hex Screw

SLED 2D drawings

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15.58 g

Kari wilhelmsen Johansen
31.5.2017
15: Hinge joint Hex Nut

UNLESS OTHERWISE SPECIFIED:
DIMENSIONS ARE IN MILLIMETERS

NAME DATE
SolidWorks Design Library Toolbox ANSI Metric Kari wilhelmsen Johansen 31.5.2017

SOLIDWORKS Student Edition. For Academic Use Only.

MATERIAL: Aluminium AL6061 alloy
WEIGHT: 3.53 g

SLED 2D drawings

DRAWN APPV'D

18,48
8,40
6,97
9,24
4,62
9,24
8,50
9,24
16
8,50
8,50
18,48

Appendix I