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4 **1 Conduit processes during the February 11, 2010 Vulcanian eruption of**
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7 **2 Soufrière Hills, Montserrat**
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Abstract

We analyzed pumice from the February 11, 2010 Vulcanian explosion that immediately followed a large dome collapse at Soufrière Hills volcano. We obtained pre-explosive values of porosity, pressure, and depth by combining textural analyses and glass water content determinations. Our data suggest that the February 2010 explosion evacuated the upper 3 km of the conduit from the dense magma (≤ 10 vol.% porosity) it contained. The low porosity distribution in the volcanic conduit implies that the magma rising from the reservoir had time to extensively degas during emplacement. We use a conduit flow model to characterize the effects of permeability on ascent conditions. Model input parameters were fitted so as to match our pre-explosive porosity data, which yielded first-order constraints on conduit radius, mass flux, outgassing efficiency, and permeability. This parametric study suggests that efficient lateral gas escape is necessary to explain the low pre-explosive porosities. Steady-state solutions fitting the observed range of dome extrusion rate in the month preceding the February 11 event suggest permeabilities $< 10^{-13}$ m² deeper than 500 m, which are values typical of crack-supported permeability. Conversely, solutions with parameters consistent with bubble-supported permeability imply transient flow conditions prior to the February 11 event. The transient conditions imply that our data represent a snapshot of the porosity distribution within the conduit that does not preclude the temporary presence of much higher porosities in the conduit. Such unsteady conduit flow conditions are consistent with the irregular but active dome growth in the month prior to the February 11 event.

Keywords: fluid dynamics; magma porosity; magma permeability; textural analysis

1. Introduction

Vulcanian explosions are short-lived but powerful events that evacuate parts of the magma present in a volcanic conduit. They often take place during dome eruptions, with little to no precursor signs (Clarke et al., 2015). Their occurrence and intensity is closely linked to magma decompression, degassing, and outgassing (Spieler et al., 2004; Mueller et al., 2011). The current eruption at Soufrière Hills volcano, Montserrat, is an ideal case to shed light on what conditions the occurrence of Vulcanian explosions. Soufrière Hills has produced over the last two decades a remarkable range of such events, from explosions series separated by a few hours to isolated explosions of variable intensity (Druitt and Kokelaar, 2002; Wadge et al., 2014a). Some explosions were closely following partial dome collapse, whereas others occurred in the absence of dome. Previous studies of pre-explosive conduit conditions at Soufrière Hills volcano were done by Clarke et al. (2007), Burgisser et al. (2010), and Burgisser et al. (2011). They have shown that the magma filling the conduit prior to Vulcanian explosions consisted of a dense cap atop the conduit with a thickness of a few tens of meters, a 200–700 m thick region with heterogeneous vesicularities, and, at greater depth, a more homogeneous, low-porosity magma that was emplaced under partly open-system degassing. This conduit stratigraphy gives the vision of a strongly heterogeneous magma column immediately prior to its disruption. The data, however, was sampled among the products of a series of explosions that occurred in 1997, which yielded an average porosity distribution within the conduit. Here, we sampled a single Vulcanian event that occurred on February 11, 2010, to obtain a more accurate snapshot of the porosity distribution in the conduit just prior to explosion.

The February 11 event ended the fifth phase of lava extrusion since the beginning of the current eruption of Soufrière Hills volcano (Stinton et al., 2014a; Stinton et al., 2014b; Wadge et al., 2014b; Cole et al., 2014; Cole et al., 2015). This 4-month period of intense extrusive activity was marked by a succession of dome growth as lava lobes and spines followed by partial dome collapse. Five isolated Vulcanian explosions occurred near the end of this phase. The average extrusion rate during phase 5

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179
180 69 was 7 m³/s with wide variations (Stinton et al., 2014a). A rate of 9 m³/s was measured over January
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182 70 12–14, shortly after the most voluminous Vulcanian explosion to date on January 8 (Cole et al.,
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184 71 2014). A rate of 1.2 m³/s was measured over January 22–28, and a rate of 0.1 m³/s was measured from
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186 72 January 30 until February 5 when a Vulcanian explosion occurred (Stinton et al., 2014a). Another
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188 73 Vulcanian explosion took place on February 8. Lava extrusion soon resumed on the W side of the
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190 74 dome before changing direction to N a day before February 11, date at which the large Vulcanian
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192 75 explosion studied here took place during the last 20 minutes of the 107-min-long partial dome
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194 76 collapse (Stinton et al. 2014).

196 77 The triggering context of the February 11 event is noteworthy. There is a well-established link
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198 78 between magma ascent rate and the occurrence of Vulcanian explosion (Miwa et al., 2009; Degruyter
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200 79 et al., 2012; Cassidy et al., 2015). Despite changes in extrusion rate in the days leading to it, the
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202 80 February 11 event seems to have been driven more by shallow processes than by deeper changes such
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204 81 as an increase of ascent rate and/or of chamber pressure (Stinton et al., 2014b; Cole et al., 2015). This
205
206 82 complex event started by generation of pyroclastic density currents that occurred in rapid succession
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208 83 as a result of the collapse of the large dome that was present. The pulsatory Vulcanian explosion
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210 84 ensued the gravitational triggering of the event as a probable result of the unloading of the magma
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212 85 column. This makes the February 11 event an ideal case study to test whether the pre-explosive
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214 86 column was in a state close to that expected for dome-forming, effusive activity and, more broadly, to
215
216 87 characterize the state of the volcano prior to a Vulcanian explosion. There is a wealth of information
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218 88 that can be used to characterize such a state because quite a number of studies involving conduit flow
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220 89 modeling that have been conducted at Soufrière Hills focused on its effusive activity (e.g., Melnik and
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222 90 Sparks, 2002; Melnik and Sparks, 2005; Mason et al., 2006; Costa et al., 2007; Collombet, 2009;
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224 91 Kozono and Koyaguchi, 2010; Albino et al., 2011; Costa et al., 2012; Degruyter et al., 2012; Costa et
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226 92 al., 2013). These models have provided first-order constraints on the interplay between ascent rate,
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228 93 volatile exsolution, and outgassing.

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94 The transition between effusive behavior and explosive behavior is closely related to the way
95 the gas phase separates itself from the rest of the ascending magma. There is a complex relationship
96 between magma inflation by volatile exsolution and gas expansion and deflation by permeable flow
97 and outgassing. One important step was to link the magma permeability to the structure and geometry
98 of the bubble network (e.g., Klug et al., 2002; Rust and Cashman, 2004; Wright et al., 2006; Bouvet
99 de Maisonneuve et al., 2009; Wright et al., 2009; Degruyter et al., 2010; Burgisser et al., 2017;
100 Colombier et al., 2017; Vasseur and Wadworth, 2017). Extensive experimental work has shown that
101 bubbles growing in response to decompression may connect each other and form a permeable network
102 when a percolation threshold has been overcome. Such threshold occurs at 30–80 vol.% porosity (e.g.,
103 Lindoo et al., 2016). Recently, Burgisser et al. (2017) proposed a permeability relationship that
104 includes a percolation threshold. It was built using experimentally decompressed natural melts and
105 included samples bearing deformed bubbles. Natural samples, however, are permeable at porosities
106 below this percolation threshold because the gas pathways are no longer made of interconnected
107 bubbles. Below 10–15 vol.% porosity, the pathways are made of a network of cracks and permeability
108 drops from $\sim 10^{-14}$ to $< 10^{-17}$ m² (Farquharson et al., 2015; Farquharson et al., 2016). While the
109 presence of cracks has been confirmed at shallow depth (Heiken et al., 1988; Castro et al., 2012b;
110 Lavallée et al., 2013; Kendrick et al., 2016), their existence at the depth of several kilometers is more
111 speculative for intermediate and evolved magma compositions because the water dissolved in the melt
112 lowers its viscosity and keeps the brittle behavior out of reach of reasonable strain rates (e.g.,
113 Edmonds et al., 2010; Cordonnier et al., 2012). Experiments on porous volcanic rock and magma
114 have shown that ductile behavior can be expected even at shallow depths within the conduit (Heap et
115 al., 2015; Heap et al., 2017).

116 The relationship between the creation of gas pathways by bubble connection or by brittle
117 behavior of the melt has only started to be addressed (Kushnir et al., 2017). Permeability supported by
118 bubbles is sensitive to the presence of crystals (e.g., Parmigiani et al., 2017) and shear can strongly
119 reorganize the permeable network (e.g., Laumonier et al., 2011; Pistone et al., 2012). Relationships

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298 120 describing permeability supported by cracks are not easily scaled up from laboratory to conduit
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300 121 characteristic sizes (Farquharson and Wadsworth, 2018). Another obstacle is that permeability has a
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302 122 hysteretic behavior that depends on whether it is being generated by expansion and exsolution of
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304 123 bubbles or by collapse (Rust and Cashman, 2004; Farquharson et al., 2016). In the case of collapse,
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306 124 porosity reduction can be accompanied by permeability reduction if the driving force is shear
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308 125 (Kolzenburg and Russell, 2014) or gravitation (Michaut et al., 2013). Such densification can also
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310 126 occur without significant reduction in permeability if the main mechanism is selective collapse of the
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312 127 smallest vesicles because of surface tension (Kennedy et al., 2016). The complexity of these
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314 128 interactions between crystal-bearing melt and networks of bubbles and cracks is such that there is
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316 129 currently no unified framework to describe magma outgassing at depth.

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318 130 We first present a combination of textural analyses and glass water content determinations of
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320 131 pumice emitted by the February 11, 2010 Vulcanian explosion that yields pre-explosive values of
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322 132 porosity, pressure, and depth. We then show that some permeability relationships calibrated for high
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324 133 (>15 vol.%) porosity can also be used to empirically represent the behavior of magma permeability at
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326 134 low porosity. We use one of these permeability relationships and a conduit flow model to characterize
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328 135 the pre-explosive conditions of the February 2010 event by fitting model outputs to our data on pre-
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330 136 explosive porosities and pressures.

332 333 137 **2. Methods**

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335
336 138 Twenty-three samples from the February 2010 eruption were collected for analysis (Table S1).
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338 139 Thirteen samples were from pumice-rich pyroclastic density current deposits in Farm River valley
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340 140 (AMO210 label prefix, pumice levee facies on Fig. 7.11 in Stinton et al., 2014b). Ten samples were
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342 141 pumices from fallout deposits at Harris Lookout, Spanish Point, and at White's Bottom Ghaut (WP
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344 142 label prefix, fallout deposits of Stinton et al., 2014b). All samples from fallout and some samples from
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346 143 levee that correspond to the “pumice boulders” of Cole et al. (2015) were texturally homogeneous

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357 144 pumices. The other levee samples were texturally heterogeneous pumice with some clasts showing
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359 145 macroscopic banding with sharp to lobate or crenulate boundaries between the dense and vesicular
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361 146 parts (Farquharson and Wadsworth, 2018). Only one representative crystalline dense clast was
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363 147 analyzed (AMO210B) because such texture has been shown to originate from to the dome (Burgisser
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365 148 et al., 2010) and our focus was to characterize deeper sourced material.

367 149 Small cores $\sim 2 \text{ cm}^3$ were drilled in each pumice. The half of the core closest to the clast surface
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369 150 was discarded so as to avoid weathering effects, while the other half was cut in two, one being
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371 151 subjected to textural analysis and the other being used for H_2O measurement. This procedure ensured
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373 152 that the various analyses characterize the same volume of sample. The size of this volume and the
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375 153 image analysis techniques we used imposed an upper limit to the vesicle size that could be
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377 154 characterized ($\sim 1 \text{ mm}$ across). As in the 1997 deposits (Giachetti et al., 2010), most pumices produced
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379 155 by the February 11 event that are smaller than $\sim 30 \text{ cm}$ lack radial gradients in vesicle abundance or
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381 156 size. Some vesicular blocks larger than this exhibit anastomosed regions with vesicles up to several
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383 157 cm, which is well above the sizes our method can measure. Such blocks were avoided in our study to
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385 158 ensure that we obtained representative vesicle size distributions of all analyzed clasts. Drawing from
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387 159 the observations done of the 1997 flows, where similar blocks were sampled closer to the dome to
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389 160 minimize transport-induced breakage (Giachetti et al., 2010), regions with large voids tend to be
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391 161 concentrated in the center of the clasts, which suggest a post-fragmentation origin (i.e. such large
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393 162 voids belong to the syn-explosive, coalesced vesicle population defined below). Avoiding sampling
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395 163 clasts with large voids does not affect the representativeness of our reconstruction of the magma
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397 164 column because the effect of post-fragmentation bubbles is removed by the procedure described
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399 165 below that converts pumice porosities to pre-explosive conditions (Burgisser et al., 2010).

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401 166 The textural characterization of the samples was done by combining Scanning Electron
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403 167 Microscopy (SEM) and element mapping by Energy Dispersive Spectroscopy (EDS). Polished
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405 168 sections were imaged using a LEO STEREOSCAN 440 (LEICA) SEM operating at 20 kV

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416 169 accelerating voltage (Université Savoie Mont Blanc) in backscattered electron mode (BSE) to which
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418 170 is attached an EDS probe QUANTAX EDS (Bruker AXS). Images were acquired using the BSE
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420 171 mode (Fig. 1A) and the elements Si, Fe, Mg, Al, and Ca at two different resolutions to ensure that the
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422 172 full range of object sizes was represented. The combination of resolutions was either one image at $\times 50$
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424 173 and 2 to 3 images at $\times 1000$ for the WP sample suite, or 1 to 2 $\times 50$ images and 4 $\times 2000$ images for the
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426 174 AMO sample suite. Images resolution was such that the respective pixel sizes at magnifications of
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428 175 either $\times 1000$, or $\times 2000$ were identical. The $\times 50$ images of samples AMO210B, G, J, and L were
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430 176 composed by tiling 9×100 images, which added a reconstruction uncertainty of 2 vol.% on measured
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432 177 proportions. Instead of SEM images, the $\times 50$ images of samples AMO210D, F, H, and Q were 2D
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434 178 slices of 3D volumes with voxel edge-length of 7–10 μm obtained by X-ray tomography (Phoenix
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436 179 Nanotom 180 at ISTO, Université d'Orléans) following the procedure described in Castro et al.
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438 180 (2012a). In these four samples, oxides and plagioclases were segmented manually from the
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440 181 ferromagnesian minerals based on X-ray attenuation level (Supplementary Fig. S1) and the respective
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442 182 proportions of ferromagnesian minerals were assumed constant at the values provided by Murphy et
443
444 183 al. (2000). Images were used to quantify in each sample the amounts of phenocrysts, microlite,
445
446 184 vesicles, and glass (Table 1) following the resolution assembly procedure of Giachetti et al. (2010)
447
448 185 and the quantification method described in Drignon et al. (2016) (Supplementary Text S1 and Fig.
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450 186 S2).

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452 187 Glass water contents of the 20 samples listed in Table 2 were measured by using the Flash 2000
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454 188 elemental analyzer (ISTO, Université d'Orléans). Samples were crushed with an automatic grinder
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456 189 without removing phenocrysts to obtain ~ 7 mg of powder $< 30 \mu\text{m}$. Following the procedure outlined
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458 190 in Drignon et al. (2016), tin capsules containing the powders were placed in a furnace where they
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460 191 were heated to $\sim 1800^\circ\text{C}$ in the presence of O_2 . A helium flux transported the liberated H in H_2O form,
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462 192 which was discriminated from other volatiles by chromatography and analyzed by thermal
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464 193 conductivity. We used the certified standard PYRO (5 wt.% H_2O by Karl Fisher titration, Burgisser et

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474
475 194 al., 2010). Total amounts of H given by the elemental analyzer were converted to bulk H₂O content
476
477 195 using H and O molar masses (Table 2). Each sample was analyzed three times in order to quantify
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479 196 measurement error. The resulting relative uncertainty is comparable to that of the standard that was
480
481 197 analyzed at regular intervals during a measurement day.

482
483 198 Vesicles were subdivided in four populations using the criteria of Giachetti et al. (2010) (Fig.
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485 199 S2). Large, deformed vesicles of equivalent size >300 μm across and circularity <0.2 were divided
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487 200 into two populations. One population was composed of large angular voids existing between crystal
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489 201 fragments that are similar to those observed in the 1997 Vulcanian pumices (Fig. 1B, Giachetti et al.,
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491 202 2010). We assumed that these voids were formed in response to the decompression accompanying the
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493 203 Vulcanian explosion. The other population was composed of the remaining large vesicles, which were
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495 204 considered as pre-explosive vesicles. The third population was composed of small, isolated, and
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497 205 rounded vesicles of equivalent size <50 μm across and circularity >0.4. The fourth population was
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499 206 composed of all the remaining vesicles, which were often interconnected. These last two populations
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501 207 have been interpreted by Giachetti et al. (2010) as having nucleated, grown, and coalesced in a syn-
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503 208 explosive fashion. As our automatic process cannot discriminate between the two first populations,
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505 209 the voids belonging to the first population were visually identified thanks to their association to
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507 210 broken crystals. They were manually assigned to the syn-explosive, connected vesicle population by
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509 211 removing them one by one from the automatically segmented images (Table 2).

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511 212 The bubble-free vesicles and oxide number densities (i.e. number of objects per unit volume of
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513 213 melt plus crystal) were obtained from the SEM and tomography images using the stereological
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515 214 transformations from Cheng and Lemlich (1983) as explained in Giachetti et al. (2010). Having only
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517 215 two levels of magnifications yields size distributions with artifacts around the cut-off length scale
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519 216 (Supplementary Text S2 and Fig. S4). Total number densities reported in Table 2, however, are
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521 217 dominated by small vesicles and oxides that are below the cut-off scale. As a result, they are not
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523 218 sensitive to such artifacts.

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219 As in Drignon et al. (2016), two physical models were successively used to convert variables
220 measured in the pumice to pre-explosive conditions (Table 3). The first model uses the vesicularities
221 and interstitial glass water contents to estimate pre-explosive pressures and porosities (Burgisser et al.,
222 2010). It has four free parameters (two related to bubble populations, one related to the quench
223 pressure, and one related to outgassing), which combined yield 11 sets of pre-explosive pressures and
224 porosities. The set with the reference values (see *Results* section) of the free parameters was kept as
225 the average set and the two sets with the largest and smallest porosity values at any pressure were kept
226 as extrema to characterize model uncertainty. Analytical uncertainties for each sample were calculated
227 with an additional four sets of outputs that used the average values of the free parameters and the
228 respective minimum and maximum values of glass water content and vesicularity.

229 Pre-explosive pressures were then converted into pre-explosive depths thanks to the second
230 model (Burgisser et al., 2011). Briefly, each sample is assumed to represent a slice of the magma
231 column and the slice thickness is adjusted so that the pressure at its base due to the overlying load
232 equals that determined by the first model. As in Drignon et al. (2016), two end-members scenarios
233 were considered. The first assumes that pressure is magma-static, i.e. that the pressure in the magma
234 column is created by the sole weight of magma because conduit walls are fully rigid. In the second
235 scenario pressure is lithostatic, which implies that the conduit walls are not rigid. The pressure
236 distribution within the conduit during eruption is, however, expected to be controlled dynamically.
237 The higher the porosity is in the magma, the more the dynamic pressure deviates from a linear trend.
238 Conversely, gas-poor conditions limit dynamic effects. Magma- and lithostatic pressure gradients
239 frame most dynamic pressure distributions in gas-rich conditions (Burgisser et al., 2011). Here, we
240 use the a posteriori argument that the conduit was mostly filled by low-porosity magma to linearly
241 relate pressure and depth.

2.1. Conduit flow modeling

243 Two permeability relationships were used to quantify gas–melt separation during magma
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591
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593 244 ascent:

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596 245 $k_K = a_K \phi_c^{b_K}$ (1)

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599 246 $k_B = \frac{\phi_c^{2.73} d^2}{800}$ (2)

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602 247 where a_K and b_K are fitting constants, d is the bubble equivalent diameter in m, and ϕ_c is the connected
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604 248 porosity, which is volume of interconnected bubbles that span the entire sample from side to side,
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606 249 divided by the total sample volume. Equation (1) is from Klug and Cashman (1996) and Eq. (2) is
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608 250 from Burgisser et al. (2017) when neglecting bubble deformation and thus assuming spherical
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610 251 bubbles. The bubble equivalent diameter is given by:

611
612 252 $d^3 = \frac{6\phi_t}{\pi N_T(1 - \phi_t)}$ (3)

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614
615 253 where ϕ_t is the total porosity and N_T is the number of bubble per unit volume of melt and crystals. The
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617 254 connected porosity is given by (Burgisser et al., 2017):

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619
620 255 $\phi_c = \frac{\phi_t}{1 + \exp[c_1(1.5 \times 10^6 d(\phi_t^{-1/3} - 1)f^{-0.128} - c_2)]}$ (4)

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622
623 256 where $c_1=0.342$, $c_2= 33.2$, and f is the ratio of the standard deviation of the bubble size distribution
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625 257 over d , which is a measure of the degree of polydispersity of the bubble population¹. The percolation
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627 258 threshold is modeled by setting $\phi_c=0$ when the total porosity is below the percolation porosity, ϕ_p :

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629
630 259 $\phi_p = \left[1 + \frac{c_2 + c_3}{1.5 \times 10^6 d} f^{0.128}\right]^{-3}$ (5)

631
632
633 260 where $c_3=6$.

634
635 261 Kozono and Koyaguchi (2010) provided a simple algebraic equation that relates pressure and

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640
641 ¹ The equation 19 in Burgisser et al. (2017) should read: $\phi_c = \frac{\phi_t}{1 + \exp[-c_\phi(1.5d_a(\phi_t^{-1/3} - 1)f^{-0.128} - c_p)]}$

650
651
652 262 porosity in a volcanic conduit and that approximates a steady state solution of a popular 1D, two-
653
654 263 phase conduit flow model (Kozono and Koyaguchi, 2009a; Kozono and Koyaguchi, 2009b; Degruyter
655
656 264 et al., 2012; Burgisser et al., 2017). For simplicity, we refer to this simplified formula as the 0D model
657
658 265 (Kozono and Koyaguchi, 2010):

$$266 \quad 1 - \frac{n\rho_{mc}RT(1-\phi_t)}{(1-n)P\phi_t}(1-E_w) + \Pi + \frac{1-\phi_t}{1-n}\Theta = 0 \quad (6)$$

$$267 \quad \Pi = \frac{8\mu_{mc}k_j}{\mu_g r_c^2 \phi_t} \quad (7)$$

$$268 \quad \Theta = \frac{k_j \rho_{mc}^2 g (1-\phi_t) \pi r_c^2}{\mu_g Q \phi_t} \quad (8)$$

269 where n is the gas mass-flow rate fraction, $\mu_g=2\times 10^{-5}$ Pa s is the gas viscosity, r_c is the conduit radius
671
672 270 in m, $g=9.81$ m/s² is the gravity acceleration, μ_{mc} is the bulk (liquid and crystal) suspension viscosity
673
674 271 in Pa s, ρ_{mc} is the bulk (liquid and crystal) density in kg/m³, T is the temperature in K, P is the
675
676 272 pressure in Pa, $R=462$ J/K kg is the specific gas constant for H₂O gas, k_j is either of k_B or k_K , and Q is
677
678 273 the mass flux in kg/s. The parameter E_w is defined as (Kozono and Koyaguchi, 2010):

$$274 \quad E_w = \frac{\pi r_c^2 q_w}{nQ} \quad (9)$$

275 where q_w is the flow rate of gas escaping laterally. The gas mass-flow rate fraction is:

$$276 \quad n = \frac{n_0 - s\sqrt{P}}{1 - s\sqrt{P}} \quad (10)$$

277 where the initial water content, $n_0 = s\sqrt{\rho_w g L}$, is a function of the conduit length, L , of the solubility
691
692 278 constant, s , and of wallrock density, $\rho_w=2600$ kg/m³. For comparison purposes, we converted mass
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694 279 fluxes to representative ascent rates by using bubble-free magma density and assuming a constant
695
696 280 conduit radius of 15 m (e.g., Wadge et al., 2014b) except where mentioned.

281 Fitting of five free parameters (Q , r_c , E_w , N_T , and f) was done by minimizing the sum of squared
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700 282 differences between the measured porosities and those given by Eq. (6) for the 19 pre-explosive

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711 283 pressures determined from sample analysis. The parameter combinations having squared difference
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713 284 falling within the 95% level confidence were considered as plausible solutions. If S_i is the sum of
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715 285 squared differences for a given combination of the free parameters and S_m is the minimum sum of
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717 286 squared differences of the entire parametric sweep, the 95% level of confidence is given by:

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720 287
$$S_i \leq S_m \left(1 + \frac{p}{o-p} F_{1-\alpha}^{p, o-p} \right) = 1.1858 S_m \quad (11)$$

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722
723 288 where $p=5$ is the number of parameters, $o=19$ is the number of observations, $\alpha=0.95$ is the level of
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725 289 confidence, and F is the $(1-\alpha)$ quantile of the F distribution with p and $(o-p)$ degrees of freedom.

726
727 290 We set the temperature, T , to 850 °C (Barclay et al., 1998; Murphy et al., 2000) and the liquid
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729 291 phase is considered as a single-phase suspension of silicate melt and crystals with a density, ρ_{mc} , of
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731 292 2450 kg/m³ (Burgisser et al., 2011). The effect of dissolved water on melt viscosity followed the
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733 293 relationship by Hess and Dingwell (1996) and the effect of crystals on bulk suspension viscosity, μ_{mc} ,
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735 294 was calculated using Krieger and Dougherty (1959) with a maximum packing of 0.65 and an Einstein
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737 295 coefficient of 2.5. The crystal content was set to 55 vol.% based on our data (Text S3, Fig. S5). Such a
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739 296 high value implies that magma rheology is non-Newtonian. Robust rheological relationships of
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741 297 realistic mixtures of phenocrysts and highly elongated microlites are currently not available, but
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743 298 various non-Newtonian approximations of the behavior of crystal-rich suspension have been proposed
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745 299 (e.g., Caricchi et al., 2007; Costa et al., 2009; Mader et al., 2013). In our case, the 0D approximation
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747 300 assumes a Newtonian liquid–wall friction that neglects such effects. This choice is motivated by the
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749 301 fact that our modeling focuses on the effusive regime with low gas volume fraction, which limits the
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751 302 upward acceleration within the conduit.

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753
754 303 **3. Results**
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756

757 304 Our samples from the February 11 event have bulk vesicularities of 44–78 vol.% and vesicle-
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759 305 free glass contents of 23–73 vol.%, except AMO210B that has 7.5±2.4 vol.% glass (Table 1). Isolated

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769
770 306 syn-explosive vesicles, connected syn-explosive vesicles, and connected pre-explosive vesicles are
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772 307 present in the respective proportions of $1 \pm 1.1:87 \pm 7.0:12$, where the uncertainties have been attributed
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774 308 to the first two bubble populations and the percentage of the last population is such that the three sum
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776 309 to 100% of the total vesicle volume fraction. The pre-explosive vesicles are large, deformed and
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778 310 coalesced. Such textures can be due to deflation occurring either pre-explosively, or syn-explosively.
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780 311 The dominant population of syn-eruptive vesicles, however, displays convex surfaces that suggest net
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782 312 inflation. Many fallout pumices also suggest net inflation because of their bloated shapes. Glass water
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784 313 contents range from 0.4 to 2.2 wt.%, except again AMO210B that has 7.4 ± 2.4 wt.% water (Table 2).
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786 314 The outlier values of AMO210B are due to the very low amount of bulk glass content, 3.6 ± 1.1 vol.%.
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788 315 Considering that glass content is deduced by subtraction, which makes the quantification of small
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790 316 amounts of glass difficult and that AMO210B has a large (14 vol.% bulk) amount of unclassified
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792 317 mineral phases, we decided to leave AMO210B out of the analysis, which then comprises 19 samples.
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794 318 This is consistent with the fact that 7.4 wt.% glass water is much higher than the amount of water
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796 319 thought to be contained in the magmatic reservoir (4.6 wt.%, Barclay et al., 1998).

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798 320 In using the model that converts vesicularities and interstitial glass water contents to pre-
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800 321 explosive pressures and porosities, a magma temperature of 850 °C and a bubble-free magma density
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802 322 of 2450 kg/m^3 (i.e., melt plus crystals) is assumed (Burgisser et al., 2010). The two free parameters
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804 323 linked to bubble populations were constrained by the proportions of the three vesicle types and their
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806 324 uncertainties. The model assumes that only the pre-explosive vesicles existed in the conduit prior to
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808 325 the explosion and thus that the gas contained in the syn-explosive vesicles was either dissolved in the
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810 326 melt or has been outgassed during the explosion. Following Burgisser et al. (2010), the parameter
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812 327 constraining the amount of overpressure that clasts can sustain was set to the reference value of $1 \text{ }_{+1}^{-0.5}$.
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814 328 The parameter that quantifies outgassing is the ratio between the amount of gas lost by outgassing
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816 329 during magma fragmentation and the total amount of gas present during the explosion. The upper and
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818 330 lower values of this parameter were chosen so that the maximum total water content is <4.6 wt.%,
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820 331 which corresponds to a saturation pressure of 130 MPa (Barclay et al., 1998), and so that all clasts had

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828
829 332 net syn-explosive inflation, as suggested by textural observations. These conditions imply that
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831 333 between 10 and 76% of the gas present syn-explosively was outgassed, with an assumed reference
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833 334 value of 50% for this poorly constrained parameter that has a modest effect on pre-explosive
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835 335 pressures.
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837
838 336 Figure 2 shows the pre-explosive pressures as a function of the pre-explosive porosities. Clasts
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840 337 originated from 8–70 MPa with porosities from 1 to 10 vol.%. Uncertainties on the porosities are
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842 338 dominated by model assumptions whereas uncertainties in pre-explosive pressures reflect the natural
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844 339 variability of glass content in the samples. The number of samples is large enough to give a
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846 340 representative pressure-porosity distribution but too small to yield a reliable estimate of the upper pre-
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848 341 explosive pressure limit (Drignon et al., 2016). The right vertical axis of Fig. 2 shows approximate
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850 342 pre-explosive depths that suggest a drawdown depth of ~3 km. Depths were estimated thanks to two
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852 343 end-member scenarios of overpressure (magma- and litho-static) in the conduit. There are only small
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854 344 differences between these two scenarios because of the low pre-explosive porosities (Table 3), so a
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856 345 single depth axis with an intrinsic uncertainty of $\pm 5\%$ is used in Fig. 2.

857
858 346 Overall, our data indicate that the single Vulcanian event of February 11 evacuated at least the
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860 347 upper 3 km of a conduit that was filled by a low-porosity, high-crystallinity magma. To have ≤ 10
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862 348 vol.% porosity suggests that the magma rising from the reservoir had time to extensively degas during
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864 349 emplacement. One possibility is that the magmatic column was significantly permeable to gas, but
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866 350 such low porosities are generally associated with low permeability values. Another is that magma
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868 351 porosity varied rapidly, which implies that our data captures only a snapshot of the conduit state just
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870 352 prior to explosion. In both cases, there must have been specific conditions that allowed the magma to
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872 353 quickly develop significant permeability while its porosity was increasing in response to
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874 354 decompression and ascent from the magmatic reservoir.

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876 355 Most bubble-supported permeability relationships depend on magma porosity to first order, and
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878 356 tend towards impermeability when extrapolated at low porosity for natural products of effusive

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888 357 eruptions (e.g., Mueller et al., 2005; Rust and Cashman, 2011). Figure 3A illustrates that trend for a
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890 358 representative suite of natural samples from dome-forming eruptions at Soufrière Hills volcano and
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892 359 Colima volcano, Mexico (Farquharson et al., 2015; Farquharson et al., 2016; Farquharson and
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894 360 Wadsworth, 2018). There are several reasons for the scatter in the data at a given porosity value. One
895
896 361 reason is the 1–2 orders of magnitudes of permeability variation as a function of sample orientation
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898 362 the permeable network is anisotropic. Another reason is the transition from crack-supported
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900 363 permeability at low connected porosity to vesicle-supported permeability at connected porosities
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902 364 larger than ~10 vol.%. Finally, samples have heterogeneities that are large compared to sample size. It
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904 365 has been shown that these two types of permeabilities can be represented with two distinct sets of
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906 366 power-law coefficients (Farquharson et al., 2015; Heap and Kennedy, 2016; Kushnir et al., 2016). The
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908 367 wide data scatter, however, drove us to select the broader approach of representing both types with a
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910 368 single relationship.

911
912 369 Figure 3A shows how the two permeability relationships, k_B and k_K , fit the entire range of the
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914 370 natural data. The relationship k_K is a power law depending on ϕ_c with coefficients that are not directly
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916 371 related to characteristics of the bubble network ($a_K=1.1\times 10^{-11}$ m² and $b_K=3.35$). The relationship k_B
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918 372 includes information about the bubble network, namely the bubble number density, N_T , and a measure
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920 373 of the spread of the bubble size distribution, f . It yields a good fit of all the data when f is allowed to
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922 374 exceed natural bounds (the best-fit value is $f=10^{10.2}$ with $N_T=10^{12.4}$ m⁻³). Both relationships can thus
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924 375 *empirically* represent the behavior of magma permeability at low porosity, regardless of geometry (by
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926 376 bubble connections or by brittle behavior of the melt) or generation mechanism (by dilatation or by
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928 377 collapse).

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930 378 The percolation threshold occurs when $\phi_c/\phi_t=0.114$, which is obtained by setting $\phi_p=\phi_t$ in Eqs.
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932 379 (4–5). As the maximum value of ϕ_t is 1, the maximum value of ϕ_c for bubble percolation is 11.4
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934 380 vol.%, which corresponds approximately to the boundary between crack- and bubble-supported
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936 381 regimes (Fig. 3A). This threshold does not affect the best-fits of k_K and k_B (i.e. ϕ_t is always $>\phi_p$) but it

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947 382 limits the possibility of reaching permeabilities much higher than those best-fits curves (e.g., $\phi_i < \phi_p$ in
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949 383 most of the gray region of Fig. 3A). If, however, Eq. (5) is neglected (i.e. if ϕ_c is given by Eq. (4) even
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951 384 if $\phi_i < \phi_p$), the whole span of values covered by the data (and the gray region of Fig. 3A) can be
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953 385 represented by k_K or k_B , regardless of permeability type. Here we focus on k_B because it has been
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955 386 calibrated jointly with ϕ_c , but similar conclusions can be drawn by using the simpler form of k_K . The
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957 387 full range of permeabilities covered by the data of Fig. 3A can be represented by k_B when
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959 388 $10^8 \leq N_T \leq 10^{19} \text{ m}^{-3}$, $10^{-1} \leq f \leq 10^{12}$, and the percolation threshold is neglected. When used in a conduit flow
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961 389 model as closure relationship, k_K helps characterizing magma ascent dynamics. We fitted outputs of a
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963 390 simplified conduit model to our data of Fig. 2 to provide first-order constraints on the type of
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965 391 permeability and other important parameters such as mass flux and conduit radius.

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968 392 The 0D model relates conduit pressure to magma porosity and depends on the initial (basal)
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970 393 water content, n_0 . Two combinations of conduit length, L , and solubility constant, s , were used so as
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972 394 to obtain $n_0 \approx 4.6 \text{ wt.}\%$ ($s = 4.11 \times 10^{-6} \text{ Pa}^{-1/2}$, $L = 5 \text{ km}$ and $s = 3.4 \times 10^{-6} \text{ Pa}^{-1/2}$, $L = 6 \text{ km}$, respectively). The
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974 395 first combination is consistent with previous work on conduit flow modeling at Soufrière Hills
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976 396 volcano (Collombet, 2009; Degruyter et al., 2012) and the second combination is a fit of s to the Liu
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978 397 et al. (2005) solubility relationship that was used in the processing of our data to reconstruct pre-
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980 398 explosive pressures and porosities (Fig. 2). For a given pair of L and s , five free parameters were
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982 399 selected for a grid search: the mass flux, Q , the conduit radius, r_c , the ratio of lateral gas flow rate to
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984 400 the vertical gas flow rate, E_w , the bubble number density, N_T , and the spread of the bubble size
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986 401 distribution, f . This choice is motivated by the fact that all the other variables of the model, such as T
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988 402 or ρ_{mc} , are known much more accurately than these five parameters. The parameter E_w quantifies how
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990 403 efficiently the gas is evacuated through the conduit walls into the wallrock versus how the gas is
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992 404 transported vertically within the conduit (Kozono and Koyaguchi, 2010). Vanishing E_w values thus
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994 405 imply conduit wall impermeability and large E_w imply high wallrock permeability. The ranges of $10^{-3} \leq Q \leq 10^5 \text{ kg/s}$,
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996 406 $1 \leq r_c \leq 50 \text{ m}$, $0 \leq E_w \leq 1$, $10^8 \leq N_T \leq 10^{19} \text{ m}^{-3}$, and $10^{-1} \leq f \leq 10^{12}$ were chosen so as to ensure

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1005
1006 407 solutions with a wide gamut of mass fluxes at the vent, conduit wall permeability, and magma
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1008 408 permeabilities that cover the data range shown in Fig. 3A. Eleven values were used for each
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1010 409 parameter, yielding 1.6×10^5 unique combinations. Another 11-value sweep was done with a narrower
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1012 410 range for E_w ($0.8 \leq E_w \leq 1$) to gain accuracy on this parameter because $E_w < 0.8$ systematically yielded
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1014 411 poor fits. Parameter combinations that verified Eq. (11) were considered solutions that fit our data
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1016 412 (Fig. 2) within the 95% level of confidence.

1018 413 The grid search results are very similar for the two conduit lengths explored, so we only report
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1020 414 those with $L=5$ km and $s=4.11 \times 10^{-6}$ Pa $^{-1/2}$ for conciseness. The sum of squared differences at the 95%
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1022 415 level of confidence are 1.7×10^{-3} , which is well above the sum of squared differences of the data
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1024 416 uncertainties, $\sim 10^{-6}$, and below that of the reconstruction model uncertainties, $\sim 10^{-2}$. The range of
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1026 417 solutions we select as best fits thus produce porosity–pressure curves that are within the range of
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1028 418 model uncertainties shown in Fig. 2. All solutions fall within a very narrow range of E_w values (0.9–
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1030 419 0.94), which implies that conduit walls must be permeable to gas flow. The four other parameters
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1032 420 have more scattered values, except N_T and Q that have strongly correlated values. Figure 4A shows
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1034 421 the number of solutions sharing the same pairwise values of N_T and Q . There are, for instance, 53
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1036 422 combinations of r_c , E_w , and f that fit our data within the 95% level of confidence with $N_T = 10^{14.6}$ m $^{-3}$
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1038 423 and $Q = 10^{0.2}$ kg/s, which is represented by a circle of size 53 on Fig. 4A. The solutions parallel a
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1040 424 power law, $Q \sim N_T^{-2/3}$, that stems from Eq. (6) and that is made visible because these two parameters are
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1042 425 varied over several orders of magnitude. Figure 4B shows the number of solutions sharing the same
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1044 426 pairwise values of N_T and f . The presence of a percolation threshold was ignored during the grid
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1046 427 search. If such a threshold is taken into account, all the solutions lying below the dashed line of Fig.
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1048 428 4B are no longer valid because gas escape is impossible.

1050 429 Typical measured densities are 10^{10} – 3×10^{16} m $^{-3}$ for isolated, syn-explosive bubbles and 2×10^8 –
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1052 430 4×10^{10} m $^{-3}$ for pre-explosive bubbles (Fig. S6). The pre-explosive population represents the lowest
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1054 431 expected number densities in the magma column just prior to explosion because it results from the

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1064
1065 432 growth and coalescence of bubbles transported from (and/or nucleated in) the magma reservoir. The
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1067 433 syn-explosive population is a reasonable upper estimate of the highest bubble number densities
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1069 434 expected to occur in the magma column prior to explosion because it results from the sudden
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1071 435 decompression of the column by the explosion, which occurred at a rate larger than that
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1073 436 accompanying magma ascent from the reservoir.

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1076 437 The full range of measured N_T is indicated on Fig. 4A, as well as the range of observed
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1078 438 extrusion rates, from $10^{4.3}$ kg/s over January 12–14, to $10^{3.5}$ kg/s over January 22–28, and to $10^{2.4}$ kg/s
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1080 439 over January 30–February 5. Solutions fitting the observed range of extrusion rate, $10^{2.4}$ – $10^{4.3}$ kg/s,
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1082 440 comprise a narrow range of N_T ($10^{10.2}$ – $10^{11.3}$ m⁻³) and large f values ($10^{6.8}$ – 10^{12} , Fig. 4B). Such f values
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1084 441 are orders of magnitude above natural vesicle distributions (0.1–10; Burgisser et al., 2017).
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1086 442 Conversely, solutions that have N_T values within the observed range, f values within the natural range,
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1088 443 and that would be compatible with a percolation threshold correspond to very low mass fluxes ($10^{-2.2}$ –
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1090 444 $10^{0.67}$ kg/s, Fig. 4A). There are thus two sets of remarkable solutions: one high-flux set that fits
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1092 445 observed extrusion rates and that has permeability behavior inconsistent with gas bubbles, and a low-
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1094 446 flux set that has Q values well below those observed and that has N_T and f values consistent with
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1096 447 bubble-supported permeability.

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1098 448 Each solution defines a curve of porosity vs. permeability. Figure 3A shows the permeability
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1100 449 behavior of the high-flux solutions and Fig. 3B shows the permeability behavior of the low-flux
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1102 450 solutions. The high-flux set covers the field occupied by most samples, whereas the low-flux set
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1104 451 comprises permeabilities that are systematically lower than their natural counterparts at any values of
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1106 452 connected porosity.

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1108 453 Conduit evacuation and replenishment must occur on a time scale faster than the travel time
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1110 454 stemming from the mass fluxes from the 0D model to be consistent with the model assumption of
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1112 455 steady state. The January 8 explosion and the associated conduit evacuation were large enough to
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1114 456 disturb the upward flow of magma feeding the dome because it is the largest single Vulcanian

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1123
1124 457 explosion to date (Cole et al., 2014). Steady-state conditions could thus only occur within the month
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1126 458 preceding the February 11 explosion. Within that period, the timing of conduit replenishment depends
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1128 459 on the observed dome growth rate and on conduit radius.
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1131 460 Observations indicate that lava extrusion was occurring irregularly during the month preceding
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1133 461 the explosion (Stinton et al., 2014a). Several studies have suggested that the conduit feeding the
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1135 462 current eruption at Soufrière Hills volcano is cylindrical in its upper part but takes the shape of a dike
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1137 463 at depth (Costa et al., 2007; Costa et al., 2012). The commonly admitted geometry is a 15-m radius
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1139 464 cylinder that extends from the vent down to 2 km to a dike of 5 by 400 m that extends from 2 km
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1141 465 down to the reservoir at ~5 km depth. Ascent speed is proportional to conduit area and the dike area is
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1143 466 equivalent to a 25-m radius cylinder. The largest suggested value of conduit radius is 40 m from
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1145 467 volumetric strain data measured during the 29 July 2008 Vulcanian explosion (Young and Gottsmann,
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1147 468 2015). Figure 5 shows the distance that a parcel of magma could have covered from January 8 to
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1149 469 February 11 at the observed rates of extrusion when conduit radii of 15, 25, and 40 m are considered.
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1151 470 A conduit of 5 km in length would have been fully replenished within ~15 days after the January 8
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1153 471 explosion for a radius of 15 m, whereas ~12% of the conduit (760 m) would have been replenished
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1155 472 during the month between the two explosions for a 40-m radius. The two minor Vulcanian explosions
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1157 473 that occurred in the few days before February 11 caused negligible additional vertical movement.
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1159 474 Because strong temporal variations of the flux were likely during that period (Odbert et al., 2014), the
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1161 475 information conveyed by Fig. 5 is an order-of-magnitude estimate of the conduit replenishment rate.

1162 476 Conduit evacuation and refilling estimates are helpful to decide which solutions calculated by
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1164 477 the 0D model are compatible with steady-state conditions. Notwithstanding the strong dependence on
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1166 478 conduit radius, Fig. 5 suggests that ascent times shorter than 2–4 weeks are necessary to ensure steady
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1168 479 state. Figure 6 shows the predicted ascent time as a function of conduit radius for the span of high-
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1170 480 and low-mass flux solutions, respectively. Both solutions sets comprise the full range of explored
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1172 481 conduit radii, but only a small fraction of the 0D model solutions are compatible with steady-state

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1183 482 conditions. These solutions all belong to the high mass flux set and correspond to $Q > 10^{3.5}$ kg/s and
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1185 483 $r_c < 25$ m.
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1188 484 In summary, low mass flux solutions are calculated assuming steady-state conditions that are
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1190 485 incompatible with the natural observations but have permeability parameters (N_T and f) consistent
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1192 486 with bubble-supported permeability. Conversely, high mass flux solutions assume steady-state
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1194 487 conditions that could be compatible with natural observations but have permeability parameters
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1196 488 inconsistent with bubble-supported permeability.
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1198 489 **4. Discussion**

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1201
1202 490 Our data suggest that the February 11 explosion took place while the magmatic column was
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1204 491 dense and that it evacuated the upper 3 km of the conduit. The extensively outgassed magmatic
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1206 492 column just prior to the explosion can be compared with similar data collected from the 1997
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1208 493 Vulcanian explosion series (Fig. 7). Drawdown depths from 2010 are comparable with the 2.5–3.5 km
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1210 494 values inferred for 1997 (Druitt et al., 2002; Burgisser et al., 2011). Porosities deeper than 1 km are
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1212 495 < 10 vol.% in both cases, but the distribution of shallow porosities differ. The larger porosities, up to
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1214 496 60 vol.%, of the 1997 explosion at shallow level complicate the conversion between pre-explosive
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1216 497 pressures and depths, which depend strongly on the presence of overpressures in the conduit.
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1218 498 Comparing instead pre-explosive pressures removes the need to assume overpressure mechanisms.
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1220 499 The high porosity 1997 data correspond to pressures < 10 MPa with a few low-porosity samples < 2
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1222 500 MPa, whereas our 2010 data has only one, 10 vol.% sample at < 10 MPa. The absence of low porosity
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1224 501 cap reflects a sampling bias, as the only dense sample was an outlier left out of our analysis. The
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1226 502 absence of > 10 vol.% porosity samples in 2010 can be due to a combination of three factors. First, the
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1228 503 number of samples is smaller for the 2010 event than for the 1997 events. Second, the 2010 data
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1230 504 sampled one explosion, whereas the 1997 data was a random sampling of several explosions. Finally,
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1232 505 the shallow parts of the magmatic column could have been more outgassed in 2010 than in 1997.
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1242 506 Several studies have suggested that the conduit feeding the current eruption at Soufrière Hills
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1244 507 volcano is cylindrical in its upper part but takes the shape of a dike at depth (see discussion in Wadge
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1246 508 et al., 2014b). The sampling depth of both the 1997 explosions (Burgisser et al., 2011) and the 2010
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1248 509 event is 2.5–3.5 km, which is comparable to that of the conduit-dyke junction (~2 km, Wadge et al.,
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1250 510 2014b). This geometrical change may adversely affect the kinematics of the decompression front that
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1252 511 feeds the Vulcanian explosions, thereby interrupting conduit evacuation.

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1254 512 Dense magmatic columns prior to explosive eruptions have also been inferred at Merapi
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1256 513 volcano, Indonesia (Fig. 7). Drignon et al. (2016) suggested low-porosity distributions of <10 vol.%
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1258 514 deeper than 1 km prior to the opening and paroxysmal stages of the 2010 Merapi eruption. The
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1260 515 drawdown depth is more variable at Merapi (4–10 km) than at Soufrière Hills volcano, but both
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1262 516 volcanoes display extensive outgassing at depth. At Soufrière Hills, this creates a puzzling situation
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1264 517 because the release of CO₂ during dome growth points to the existence of gas pathways that transfer
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1266 518 the gas from the deeper parts of the magmatic system to the surface (Edmonds et al., 2010). The
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1268 519 percolation of CO₂ through a poorly vesicular magmatic column is difficult to reconcile with the fact
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1270 520 that large permeabilities are promoted in magmas where bubbles are numerous and large enough to
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1272 521 form permeable networks (e.g., Burgisser et al., 2017).

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1274 522 In an attempt to quantify how low permeabilities have to be to produce such dense magmatic
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1276 523 columns, we used the fact that bubble-based permeability relationships recover to first order the
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1278 524 behavior of crack-supported permeability. We focused on k_B and assumed no lower limit for
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1280 525 percolation. This relationship recovers the full range of a representative suite of eruptive products.
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1282 526 These products, however, correspond to magmas that have undergone decompression, degassing, and
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1284 527 outgassing. They are thus not directly representative of the permeable network at depth. The k_B
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1286 528 relationship has been shown to represent the bubble-supported permeability of experimental melts at
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1288 529 high pressure (Burgisser et al., 2017). It has not, however, been tested on bubble-supported
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1290 530 permeability of crystal-bearing melts (Okumura et al., 2012; Parmigiani et al., 2017) or on crack-

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1301 531 supported permeability under high pressure conditions (Kushnir et al., 2017) because of scaling issues
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1303 532 (e.g., Farquharson and Wadsworth, 2018). As a result, we cannot exclude that magma permeability at
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1305 533 depth deviates from the trend depicted in Fig. 3. Our first-order approach would thus benefit from
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1307 534 future progress on the nature of magma permeability at depth.
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1310 535 The 0D model fits of our pressure and porosity data point to a fairly narrow range of values for
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1312 536 the ratio of horizontal to vertical gas flux ($0.9 \leq E_w \leq 0.94$). This is consistent with the expectation that
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1314 537 lateral gas escape favors porosity reduction (e.g., Kozono and Koyaguchi, 2012). The importance of
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1316 538 wallrock permeability in controlling outgassing has long been pointed out (Jaupart and Allegre, 1991;
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1318 539 Taisne and Jaupart, 2008; Farquharson et al., 2015). Recently, Chevalier et al. (2017) have refined this
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1320 540 view by suggesting that the lowest of wallrock permeability and horizontal magma permeability
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1322 541 controls lateral gas loss. If magma permeability is supported by the bubble network, bubble
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1324 542 elongation has the potential to reduce the horizontal permeability to very low values (Klug et al.,
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1326 543 2002; Wright et al., 2006; Degruyter et al., 2010; Burgisser et al., 2017), which opens the possibility
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1328 544 that such permeability reduction exerts a control on the amount of lateral outgassing that exceeds that
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1330 545 of wallrock permeability.

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1332 546 Our model outputs suggest that outgassing of a bubble network can be efficient at low
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1334 547 permeabilities provided that magma ascent is slow enough. This general result is consistent with
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1336 548 findings from other conduit flow model studies (Kozono and Koyaguchi, 2010; Degruyter et al.,
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1338 549 2012). Although such combination of low permeability and ascent rate can explain the pre-explosive
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1340 550 porosity distribution within the conduit, it is inconsistent with the extrusion rates and the course of the
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1342 551 eruption during the month prior to the February 11 event. Whether due to transient magma flow and
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1344 552 to the fact that permeability was not supported by a bubble network, this mismatch make it impossible
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1346 553 to obtain an estimate of the number density of the bubbles that nucleated during ascent from the
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1348 554 reservoir or, more likely, that were inherited from the reservoir (Edmonds et al., 2014; Edmonds et al.,
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1350 555 2015; Edmonds et al., 2016). The only constraint brought by our work is thus that measured number

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1360 556 densities of pre-explosive bubbles (10^8 – 10^{10} m⁻³) mark the upper limit of actual number densities
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1362 557 because bubbles are expected to rarefy during ascent as coalescence and outgassing proceeds (e.g.,
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1364 558 Gardner, 2007; Martel and Iacono-Marziano, 2015).

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1367 559 Fits of the 0D model with permeabilities expected from connected gas bubbles feature very
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1369 560 small discharge rates that suggest near stalling of the magmatic column just prior to the February 11
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1371 561 explosion. These fits cannot be used quantitatively because the steady state conditions assumed by the
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1373 562 model are not consistent with the observations. This opens the possibility that our data represent a
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1375 563 snapshot of a transient state of the conduit, such as relatively brief and multiple stalling of the
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1377 564 ascending magma (Lensky et al., 2008). Seismic record shows sub-daily activity cycles in the days
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1379 565 before February 11 (Stinton et al., 2014b), the last activity peaks before dome collapse occurring
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1381 566 every 7–8 h. The last magma stalling could not have occurred over more than a couple of hours before
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1383 567 the explosion. Magma outgassing is thus efficient enough to occur in less than a few hours, which is
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1385 568 consistent with observations (Rodgers et al., 2016) done over the whole course of the Soufrière Hills
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1387 569 eruption. After dome collapse, for instance, outgassing decays in hours to a few days (Edmonds et al.,
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1389 570 2003). Hour-long, large outgassing events have been measured (Edmonds and Herd, 2007). These
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1391 571 considerations suggest that unsteady flow was likely, which implies that rapid redistribution of
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1393 572 porosity can occur over timescales of hours or less. A fruitful research direction would thus be to
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1395 573 develop 2D, transient conduit flow models where the processes of degassing and outgassing are fully
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1397 574 coupled to test whether the feedbacks between porosity reorganization and permeability development
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1399 575 can be that fast.

1400 576 The high mass flux ($>10^{3.5}$ kg/s) fits of the 0D model with conduit radii <25 m are compatible
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1402 577 with steady-state flow within the conduit in the days to weeks prior to February 11 (Stinton et al.,
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1404 578 2014a). Calculated permeabilities are $<10^{-13}$ m² deeper than 500 m (Figs. 2–3), which are values
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1406 579 typical of crack-supported permeability. Cracks have been shown to occur by magma brittle failure,
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1408 580 which leads to shear bands (Hale and Wadge, 2008) or stick-slip motion (Costa et al., 2012; Costa et

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1419 581 al., 2013). Such cracks, however, are only likely to occur shallowly (Kendrick et al., 2013).
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1421 582 Considering the high crystal volume fraction in the Soufrière Hills magma (Murphy et al., 2000) and
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1423 583 the presence of gas in the reservoir, one possibility to explain permeability development at depth and
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1425 584 at very low gas volume fraction is the interaction of bubbles and crystals (Parmigiani et al., 2017) in a
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1427 585 shearing environment (Laumonier et al., 2011). In the absence of more conclusive evidence, we
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1429 586 speculate that this scenario is less likely than that involving transient porosity redistribution.
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1432 587 **5. Conclusions**

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1435 588 We analyzed pumices from the February 11, 2010 Vulcanian explosion that immediately
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1437 589 followed a large dome collapse at Soufrière Hills volcano. We obtained pre-explosive values of
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1439 590 porosity, pressure, and depth by combining textural analyses and glass water content determinations.
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1441 591 Our data suggest that the February 11 explosion evacuated the upper 3 km of the conduit from the
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1443 592 dense (≤ 10 vol.% porosity) magma it contained. Such drawdown depth is comparable to that inferred
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1445 593 for the 1997 Vulcanian explosion series (Burgisser et al., 2010). The low porosity distribution in the
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1447 594 volcanic conduit suggests that the magma rising from the reservoir has had time to extensively degas.
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1449 595 We used a conduit flow model to characterize conditions allowing the magma to develop
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1451 596 significant permeability and outgassing that counteract the increase in porosity caused by ascent and
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1453 597 decompression. We used permeability relationships that were calibrated for high (> 15 vol.%) porosity
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1455 598 but that also empirically represent the behavior of magma permeability at low porosity, regardless of
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1457 599 geometry (by bubble interconnection or by melt fracturing) and generation mechanism (by inflation or
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1459 600 by collapse). The conduit flow model is an algebraic equation relating pressure and porosity (Kozono
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1461 601 and Koyaguchi, 2010) that approximates steady-state solutions of a 1D two-phase conduit flow model
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1463 602 (Kozono and Koyaguchi, 2009b; Degruyter et al., 2012). Model input parameters were fitted so as to
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1465 603 match our pre-explosive porosity data, which yielded first-order constraints on conduit radius, mass
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1467 604 flux, outgassing efficiency, and permeability.
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1478 605 Model fits point to high ratios of horizontal to vertical gas flux ($0.9 \leq E_w \leq 0.94$). Efficient lateral
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1480 606 gas escape is thus necessary to explain the low pre-explosive porosities. Solutions fitting the observed
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1482 607 range of lava extrusion rate in the month preceding the February 11 event assume steady-state
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1484 608 conditions that could be compatible with natural observations but have permeability parameters
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1486 609 inconsistent with bubble-supported permeability. Conversely, solutions with permeability parameters
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1488 610 (N_T and f) consistent with bubble-supported permeability are associated to mass fluxes so low that the
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1490 611 steady-state assumption is incompatible with the natural observations.

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1492 612 Our modeling suggests two possible scenarios to explain the low pre-explosive porosities. The
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1494 613 first possibility is that fast ascent prior to February 11 ensured steady-state conditions, in which case
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1496 614 our modeling suggests permeabilities $< 10^{-13} \text{ m}^2$ deeper than 500 m. These values typical of crack-
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1498 615 supported permeability (Farquharson et al., 2015; Farquharson et al., 2016) bring an additional
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1500 616 confirmation of the gas pathways at depth that have been inferred from gas measurements at the vent
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1502 617 (Edmonds et al., 2003), but the empirical nature of our permeability relationship leaves their genesis
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1504 618 unexplained. The second possibility is that transient flow conditions prevailed prior to the February 11
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1506 619 event, in which case our data are a snapshot of the porosity distributions within the conduit that does
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1508 620 not preclude much higher porosities to have existed in the conduit. This scenario is consistent with the
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1510 621 irregular but active dome growth in the month prior to the February 11 event. In particular, near
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1512 622 stalling of the magmatic column and extensive outgassing could have happened at most a couple of
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1514 623 hours before dome collapse. Taking into account observations on the degassing patterns over the
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1516 624 whole course of Soufrière Hills eruption, this suggests that porosity redistribution can occur over
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1518 625 timescales of hours or less.

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634 **References**

635 Albino, F., Pinel, V., Massol, H., Collombet, M., 2011. Conditions for detection of ground
636 deformation induced by conduit flow and evolution. *J. Geophys. Res. Solid Earth* 116,
637 B06201. <https://doi.org/10.1029/2010JB007871>

638 Barclay, J., Rutherford, M.J., Carroll, M.R., Murphy, M.D., Devine, J.D., Gardner, J., Sparks, R.S.J.,
639 1998. Experimental phase equilibria constraints on pre-eruptive storage conditions of the
640 Soufriere Hills magma. *Geophys. Res. Lett.* 25, 3437–3440.

641 Bouvet de Maisonneuve, C., Bachmann, O., Burgisser, A., 2009. Characterization of juvenile
642 pyroclasts from the Kos Plateau Tuff (Aegean Arc): insights into the eruptive dynamics of a
643 large rhyolitic eruption. *Bull. Volcanol.* 71, 643–658. [https://doi.org/10.1007/s00445-008-](https://doi.org/10.1007/s00445-008-0250-x)
644 0250-x

645 Burgisser, A., Arbaret, L., Druitt, T.H., Giachetti, T., 2011. Pre-explosive conduit conditions of the
646 1997 Vulcanian explosions at Soufrière Hills Volcano, Montserrat: II. Overpressure and depth
647 distributions. *J. Volcanol. Geotherm. Res.* 199, 193–205.

648 Burgisser, A., Chevalier, L., Gardner, J.E., Castro, J.M., 2017. The percolation threshold and
649 permeability evolution of ascending magmas. *Earth Planet. Sci. Lett.* 470, 37–47.
650 <https://doi.org/10.1016/j.epsl.2017.04.023>

651 Burgisser, A., Poussineau, S., Arbaret, L., Druitt, T.H., Giachetti, T., Bourdier, J.-L., 2010. Pre-
652 explosive conduit conditions of the 1997 Vulcanian explosions at Soufrière Hills Volcano,
653 Montserrat: I. Pressure and vesicularity distributions. *J. Volcanol. Geotherm. Res.* 194, 27–
654 41. <https://doi.org/10.1016/j.jvolgeores.2010.04.008>

655 Caricchi, L., Burlini, L., Ulmer, P., Gerya, T., Vassalli, M., Papale, P., 2007. Non-Newtonian
656 rheology of crystal-bearing magmas and implications for magma ascent dynamics. *Earth*
657 *Planet. Sci. Lett.* 264, 402–419.

658 Cassidy, M., Cole, P.D., Hicks, K.E., Varley, N.R., Peters, N., Lerner, A.H., 2015. Rapid and slow:
659 Varying magma ascent rates as a mechanism for Vulcanian explosions. *Earth Planet. Sci.*
660 *Lett.* 420, 73–84. <https://doi.org/10.1016/j.epsl.2015.03.025>

661 Castro, J.M., Burgisser, A., Schipper, C.I., Mancini, S., 2012a. Mechanisms of bubble coalescence in
662 silicic magmas. *Bull. Volcanol.* 74, 2339–2352. <https://doi.org/10.1007/s00445-012-0666-1>

663 Castro, J.M., Cordonnier, B., Tuffen, H., Tobin, M.J., Puskar, L., Martin, M.C., Bechtel, H.A., 2012b.
664 The role of melt-fracture degassing in defusing explosive rhyolite eruptions at volcán Chaitén.
665 *Earth Planet. Sci. Lett.* 333–334, 63–69. <https://doi.org/10.1016/j.epsl.2012.04.024>

666 Cheng, H.C., Lemlich, R., 1983. Errors in the Measurement of Bubble Size Distribution in Foam. *Ind.*
667 *Eng. Chem. Fundam.* 22, 105–109. <https://doi.org/10.1021/i100009a018>

668 Chevalier, L., Collombet, M., Pinel, V., 2017. Temporal evolution of magma flow and degassing
669 conditions during dome growth, insights from 2D numerical modeling. *J. Volcanol.*
670 *Geotherm. Res.* 333–334, 116–133. <https://doi.org/10.1016/j.jvolgeores.2017.01.016>

671 Clarke, A.B., Esposti Ongaro, T., Belousov, A., 2015. Vulcanian Eruptions, in: Sigurdsson, H. (Ed.),
672 *The Encyclopedia of Volcanoes (Second Edition)*. Academic Press, Amsterdam, pp. 505–518.
673 <https://doi.org/10.1016/B978-0-12-385938-9.00028-6>

674 Clarke, A.B., Stephens, S., Teasdale, R., Sparks, R.S.J., Diller, K., 2007. Petrologic constraints on the
675 decompression history of magma prior to Vulcanian explosions at the Soufrière Hills volcano,
676 Montserrat. *J. Volcanol. Geotherm. Res.* 161, 261–274.
677 <https://doi.org/10.1016/j.jvolgeores.2006.11.007>

678 Cole, P.D., Smith, P.J., Stinton, A.J., Odbert, H.M., Bernstein, M.L., Komorowski, J.C., Stewart, R.,
679 2014. Vulcanian explosions at Soufrière Hills Volcano, Montserrat between 2008 and 2010.
680 *Geol. Soc. Lond. Mem.* 39, 93–111. <https://doi.org/10.1144/M39.5>

681 Cole, P.D., Stinton, A.J., Odbert, H.M., Bonadonna, C., Stewart, R.C., 2015. An inclined Vulcanian
682 explosion and associated products. *J. Geol. Soc.* 172, 287–293.

1653
1654
1655
1656
1657
1658
1659
1660
1661
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1663
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1705
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1707
1708
1709
1710
1711

- 683 <https://doi.org/10.1144/jgs2014-099>
- 684 Collombet, M., 2009. Two-dimensional gas loss for silicic magma flows: toward more realistic
685 numerical models. *Geophys. J. Int.* 177, 309–318.
- 686 Colombier, M., Wadsworth, F. B., Gurioli, L., Scheu, B., Kueppers, U., Di Muro, A., & Dingwell, D.
687 B. (2017). The evolution of pore connectivity in volcanic rocks. *Earth and Planetary Science*
688 *Letters*, 462, 99-109.
- 689 Cordonnier, B., Caricchi, L., Pistone, M., Castro, J., Hess, K.-U., Gottschaller, S., Manga, M.,
690 Dingwell, D.B., Burlini, L., 2012. The viscous-brittle transition of crystal-bearing silicic melt:
691 Direct observation of magma rupture and healing. *Geology* 40, 611–614.
- 692 Costa, A., Caricchi, L., Bagdassarov, N., 2009. A model for the rheology of particle-bearing
693 suspensions and partially molten rocks. *Geochem. Geophys. Geosystems* 10.
- 694 Costa, A., Melnik, O., Sparks, R.S.J., 2007. Controls of conduit geometry and wallrock elasticity on
695 lava dome eruptions. *Earth Planet. Sci. Lett.* 260, 137–151.
696 <https://doi.org/10.1016/j.epsl.2007.05.024>
- 697 Costa, A., Wadge, G., Melnik, O., 2012. Cyclic extrusion of a lava dome based on a stick-slip
698 mechanism. *Earth Planet. Sci. Lett.* 337–338, 39–46.
699 <https://doi.org/10.1016/j.epsl.2012.05.011>
- 700 Costa, A., Wadge, G., Stewart, R., Odbert, H., 2013. Coupled subdaily and multiweek cycles during
701 the lava dome eruption of Soufrière Hills Volcano, Montserrat. *J. Geophys. Res. Solid Earth*
702 118, 1895–1903. <https://doi.org/10.1002/jgrb.50095>
- 703 Degruyter, W., Bachmann, O., Burgisser, A., 2010. Controls on magma permeability in the volcanic
704 conduit during the climactic phase of the Kos Plateau Tuff eruption (Aegean Arc). *Bull.*
705 *Volcanol.* 72, 63–74. <https://doi.org/10.1007/s00445-009-0302-x>
- 706 Degruyter, W., Bachmann, O., Burgisser, A., Manga, M., 2012. The effects of outgassing on the
707 transition between effusive and explosive silicic eruptions. *Earth Planet. Sci. Lett.* 349–350,
708 161–170. <https://doi.org/10.1016/j.epsl.2012.06.056>
- 709 Drignon, M.J., Bechon, T., Arbaret, L., Burgisser, A., Komorowski, J.-C., Caroline, M., Hayden, M.,
710 Yaputra, R., 2016. Preexplosive conduit conditions during the 2010 eruption of Merapi
711 volcano (Java, Indonesia). *Geophys. Res. Lett.* 43, 11,595-11,602.
712 <https://doi.org/10.1002/2016GL071153>
- 713 Druitt, T.H., Kokelaar, B.P., 2002. The eruption of Soufriere Hills Volcano, Montserrat, from 1995 to
714 1999.
- 715 Druitt, T.H., Young, S.R., Baptie, B., Bonadonna, C., Calder, E.S., Clarke, A. b., Cole, P.D., Harford,
716 C.L., Herd, R.A., Lockett, R., Ryan, G., Voight, B., 2002. Episodes of cyclic Vulcanian
717 explosive activity with fountain collapse at Soufrière Hills volcano, Montserrat. pp. 281-306
718 TY2-KW-0.
- 719 Edmonds, M., Aiuppa, A., Humphreys, M., Moretti, R., Giudice, G., Martin, R.S., Herd, R.A.,
720 Christopher, T., 2010. Excess volatiles supplied by mingling of mafic magma at an andesite
721 arc volcano. *Geochem. Geophys. Geosystems* 11.
- 722 Edmonds, M., Brett, A., Herd, R.A., Humphreys, M.C.S., Woods, A., 2015. Magnetite-bubble
723 aggregates at mixing interfaces in andesite magma bodies. *Geol. Soc. Lond. Spec. Publ.* 410,
724 95–121. <https://doi.org/10.1144/SP410.7>
- 725 Edmonds, M., Herd, R.A., 2007. A volcanic degassing event at the explosive-effusive transition.
726 *Geophys. Res. Lett.* 34. <https://doi.org/10.1029/2007GL031379>
- 727 Edmonds, M., Humphreys, M.C.S., Hauri, E.H., Herd, R.A., Wadge, G., Rawson, H., Ledden, R.,
728 Plail, M., Barclay, J., Aiuppa, A., Christopher, T.E., Giudice, G., Guida, R., 2014. Pre-
729 eruptive vapour and its role in controlling eruption style and longevity at Soufrière Hills
730 Volcano. *Geol. Soc. Lond. Mem.* 39, 291–315. <https://doi.org/10.1144/M39.16>
- 731 Edmonds, M., Kohn, S.C., Hauri, E.H., Humphreys, M.C.S., Cassidy, M., 2016. Extensive, water-rich
732 magma reservoir beneath southern Montserrat. *Lithos* 252–253, 216–233.
733 <https://doi.org/10.1016/j.lithos.2016.02.026>

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1764
1765
1766
1767
1768
1769
1770

- 734 Edmonds, M., Oppenheimer, C., Pyle, D.M., Herd, R.A., Thompson, G., 2003. SO₂ emissions from
735 Soufrière Hills Volcano and their relationship to conduit permeability, hydrothermal
736 interaction and degassing regime. *J. Volcanol. Geotherm. Res.* 124, 23–43.
- 737 Farquharson, J., Heap, M.J., Varley, N.R., Baud, P., Reuschlé, T., 2015. Permeability and porosity
738 relationships of edifice-forming andesites: A combined field and laboratory study. *J.*
739 *Volcanol. Geotherm. Res.* 297, 52–68. <https://doi.org/10.1016/j.jvolgeores.2015.03.016>
- 740 Farquharson, J.I., Heap, M.J., Lavallée, Y., Varley, N.R., Baud, P., 2016. Evidence for the
741 development of permeability anisotropy in lava domes and volcanic conduits. *J. Volcanol.*
742 *Geotherm. Res.* 323, 163–185. <https://doi.org/10.1016/j.jvolgeores.2016.05.007>
- 743 Farquharson, J.I., Wadsworth, F.B., 2018. Upscaling permeability in anisotropic volcanic systems. *J.*
744 *Volcanol. Geotherm. Res.* 364, 35–47. <https://doi.org/10.1016/j.jvolgeores.2018.09.002>
- 745 Gardner, J.E., 2007. Bubble coalescence in rhyolitic melts during decompression from high pressure.
746 *J. Volcanol. Geotherm. Res.* 166, 161–176.
- 747 Giachetti, T., Druitt, T.H., Burgisser, A., Arbaret, L., Galven, C., 2010. Bubble nucleation, growth
748 and coalescence during the 1997 Vulcanian explosions of Soufrière Hills Volcano,
749 Montserrat. *J. Volcanol. Geotherm. Res.* 193, 215–231.
- 750 Hale, A.J., Wadge, G., 2008. The transition from endogenous to exogenous growth of lava domes
751 with the development of shear bands. *J. Volcanol. Geotherm. Res.* 171, 237–257.
- 752 Heap, M. J., & Kennedy, B. M. (2016). Exploring the scale-dependent permeability of fractured
753 andesite. *Earth and Planetary Science Letters*, 447, 139-150.
- 754 Heap, M.J., Farquharson, J.I., Baud, P., Lavallée, Y., Reuschlé, T., 2015. Fracture and compaction of
755 andesite in a volcanic edifice. *Bull. Volcanol.* 77, 55. <https://doi.org/10.1007/s00445-015-0938-7>.
- 756 Heap, M.J., Violay, M., Wadsworth, F.B., Vasseur, J., 2017. From rock to magma and back again:
757 The evolution of temperature and deformation mechanism in conduit margin zones. *Earth*
758 *Planet. Sci. Lett.* 463, 92–100. <https://doi.org/10.1016/j.epsl.2017.01.021>
- 759 Heiken, G., Wohletz, K., Eichelberger, J., 1988. Fracture fillings and intrusive pyroclasts, Inyo
760 Domes, California. *J. Geophys. Res. Solid Earth* 93, 4335–4350.
761 <https://doi.org/10.1029/JB093iB05p04335>
- 762 Hess, K.-U., Dingwell, D.B., 1996. Viscosities of hydrous leucogranitic melts: A non-Arrhenian
763 model. *Am. Mineral.* 81, 1297–1300.
- 764 Jaupart, C., Allegre, C., 1991. Gas content, eruption rate and instabilities of eruption regime in silicic
765 volcanoes. *Earth Planet. Sci. Lett.* 102, 413–429.
- 766 Kendrick, J.E., Lavallée, Y., Hess, K.-U., Heap, M.J., Gaunt, H.E., Meredith, P.G., Dingwell, D.B.,
767 2013. Tracking the permeable porous network during strain-dependent magmatic flow. *J.*
768 *Volcanol. Geotherm. Res.* 260, 117–126. <https://doi.org/10.1016/j.jvolgeores.2013.05.012>
- 769 Kendrick, J.E., Lavallée, Y., Varley, N.R., Wadsworth, F.B., Lamb, O.D., Vasseur, J., 2016. Blowing
770 off steam: Tuffisite formation as a regulator for lava dome eruptions. *Front. Earth Sci.* 4.
771 <https://doi.org/10.3389/feart.2016.00041>
- 772 Kennedy, B.M., Wadsworth, F.B., Vasseur, J., Ian Schipper, C., Mark Jellinek, A., von Aulock, F.W.,
773 Hess, K.-U., Kelly Russell, J., Lavallée, Y., Nichols, A.R.L., Dingwell, D.B., 2016. Surface
774 tension driven processes densify and retain permeability in magma and lava. *Earth Planet.*
775 *Sci. Lett.* 433, 116–124. <https://doi.org/10.1016/j.epsl.2015.10.031>
- 776 Klug, C., Cashman, K.V., 1996. Permeability development in vesiculating magmas: implications for
777 fragmentation. *Bull. Volcanol.* 58, 87–100.
- 778 Klug, C., Cashman, K.V., Bacon, C.R., 2002. Structure and physical characteristics of pumice from
779 the climactic eruption of Mount Mazama (Crater Lake), Oregon. *Bull. Volcanol.* 64, 486–501.
- 780 Kolzenburg, S., Russell, J.K., 2014. Welding of pyroclastic conduit infill: A mechanism for cyclical
781 explosive eruptions. *J. Geophys. Res. Solid Earth* 119, 5305–5323.
782 <https://doi.org/10.1002/2013JB010931>
- 783 Kozono, T., Koyaguchi, T., 2012. Effects of gas escape and crystallization on the complexity of
784

1771
1772
1773 785 conduit flow dynamics during lava dome eruptions. *J. Geophys. Res.* 117.
1774 786 Kozono, T., Koyaguchi, T., 2010. A simple formula for calculating porosity of magma in volcanic
1775 787 conduits during dome-forming eruptions. *Earth Planets Space* 62, 483–488.
1776 788 Kozono, T., Koyaguchi, T., 2009a. Effects of relative motion between gas and liquid on 1-
1777 789 dimensional steady flow in silicic volcanic conduits: 1. An analytical method. *J. Volcanol.*
1778 790 *Geotherm. Res.* 180, 21–36.
1779 791 Kozono, T., Koyaguchi, T., 2009b. Effects of relative motion between gas and liquid on 1-
1780 792 dimensional steady flow in silicic volcanic conduits: 2. Origin of diversity of eruption styles.
1781 793 *J. Volcanol. Geotherm. Res.* 180, 37–49.
1782 794 Krieger, I.M., Dougherty, T.J., 1959. A mechanism for non-Newtonian flow in suspensions of rigid
1783 795 spheres. *Trans. Soc. Rheol.* III, 137–152.
1784 796 Kushnir, A.R.L., Martel, C., Bourdier, J.-L., Heap, M.J., Reuschlé, T., Erdmann, S., Komorowski, J.-
1785 797 C., Cholik, N., 2016. Probing permeability and microstructure: Unravelling the role of a low-
1786 798 permeability dome on the explosivity of Merapi (Indonesia). *J. Volcanol. Geotherm. Res.*
1787 799 316, 56–71. <https://doi.org/10.1016/j.jvolgeores.2016.02.012>
1788 800 Kushnir, A.R.L., Martel, C., Champallier, R., Arbaret, L., 2017. In situ confirmation of permeability
1789 801 development in shearing bubble-bearing melts and implications for volcanic outgassing. *Earth*
1790 802 *Planet. Sci. Lett.* 458, 315–326. <https://doi.org/10.1016/j.epsl.2016.10.053>
1791 803 Laumonier, M., Arbaret, L., Burgisser, A., Champallier, R., 2011. Porosity redistribution enhanced by
1792 804 strain localization in crystal-rich magmas. *Geology* 39, 715–718.
1793 805 <https://doi.org/10.1130/G31803.1>
1794 806 Lavallée, Y., Benson, P.M., Heap, M.J., Hess, K.-U., Flaws, A., Schillinger, B., Meredith, P.G.,
1795 807 Dingwell, D.B., 2013. Reconstructing magma failure and the degassing network of dome-
1796 808 building eruptions. *Geology* 41, 515–518.
1797 809 Lensky, N.G., Sparks, R.S.J., Navon, O., Lyakhovsky, V., 2008. Cyclic activity at Soufrière Hills
1798 810 Volcano, Montserrat: degassing-induced pressurization and stick-slip extrusion. pp. 169-188
1799 811 TY2-KW-0.
1800 812 Lindoo, A., Larsen, J.F., Cashman, K.V., Dunn, A.L., Neill, O.K., 2016. An experimental study of
1801 813 permeability development as a function of crystal-free melt viscosity. *Earth Planet. Sci. Lett.*
1802 814 435, 45–54. <https://doi.org/10.1016/j.epsl.2015.11.035>
1803 815 Liu, Y., Zhang, Y., Behrens, H., 2005. Solubility of H₂O in rhyolitic melts at low pressures and a new
1804 816 empirical model for mixed H₂O-CO₂ solubility in rhyolitic melts. *J. Volcanol. Geotherm.*
1805 817 *Res.* 143, 219–235.
1806 818 Mader, H.M., Llewellyn, E.W., Mueller, S.P., 2013. The rheology of two-phase magmas: A review
1807 819 and analysis. *J. Volcanol. Geotherm. Res.* 257, 135–158.
1808 820 <https://doi.org/10.1016/j.jvolgeores.2013.02.014>
1809 821 Martel, C., Iacono-Marziano, G., 2015. Timescales of bubble coalescence, outgassing, and foam
1810 822 collapse in decompressed rhyolitic melts. *Earth Planet. Sci. Lett.* 412, 173–185.
1811 823 <https://doi.org/10.1016/j.epsl.2014.12.010>
1812 824 Mason, R.M., Starostin, A.B., Melnik, O.E., Sparks, R.S.J., 2006. From Vulcanian explosions to
1813 825 sustained explosive eruptions: The role of diffusive mass transfer in conduit flow dynamics. *J.*
1814 826 *Volcanol. Geotherm. Res.* 153, 148–165.
1815 827 Melnik, O., Sparks, R.S.J., 2005. Controls on conduit magma flow dynamics during lava dome
1816 828 building eruptions. *J. Geophys. Res.* 110.
1817 829 Melnik, O., Sparks, R.S.J., 2002. Dynamics of magma ascent and lava extrusion at Soufrière Hills
1818 830 Volcano, Montserrat. *Geol. Soc. Lond. Mem.* 21, 153–171.
1819 831 <https://doi.org/10.1144/GSL.MEM.2002.021.01.07>
1820 832 Michaut, C., Ricard, Y., Bercovici, D., Sparks, R.S.J., 2013. Eruption cyclicity at silicic volcanoes
1821 833 potentially caused by magmatic gas waves. *Nat. Geosci.* 6, 856–860.
1822 834 Miwa, T., Toramaru, A., Iguchi, M., 2009. Correlations of volcanic ash texture with explosion
1823 835 earthquakes from vulcanian eruptions at Sakurajima volcano, Japan. *J. Volcanol. Geotherm.*

1830
1831
1832 836 Res. 184, 473–486.

1833 837 Mueller, S., Melnik, O., Spieler, O., Scheu, B., Dingwell, D.B., 2005. Permeability and degassing of
1834 838 dome lavas undergoing rapid decompression: An experimental determination. *Bull. Volcanol.*
1835 839 67, 526–538.

1836 840 Mueller, S., Scheu, B., Kueppers, U., Spieler, O., Richard, D., Dingwell, D.B., 2011. The porosity of
1837 841 pyroclasts as an indicator of volcanic explosivity. *J. Volcanol. Geotherm. Res.* 203, 168–174.
1838 842 <https://doi.org/10.1016/j.jvolgeores.2011.04.006>

1839 843 Murphy, M.D., Sparks, R.S.J., Barclay, J., Carroll, M.R., Brewer, T.S., 2000. Remobilization of
1840 844 andesite magma by intrusion of mafic magma at the Soufriere Hills Volcano, Montserrat,
1841 845 West Indies. *J. Petrol.* 41, 21–42.

1842 846 Odbert, H.M., Stewart, R.C., Wadge, G., 2014. Cyclic phenomena at the Soufrière Hills Volcano,
1843 847 Montserrat. *Geol. Soc. Lond. Mem.* 39, 41–60. <https://doi.org/10.1144/M39.2>

1844 848 Okumura, S., Nakamura, M., Nakano, T., Uesugi, K., Tsuchiyama, A., 2012. Experimental constraints
1845 849 on permeable gas transport in crystalline silicic magmas. *Contrib. Mineral. Petrol.* 164, 493–
1846 850 501.

1847 851 Parmigiani, A., Degruyter W., Leclaire S., Huber C., Bachmann O., 2017. The mechanics of shallow
1848 852 magma reservoir outgassing. *Geochem. Geophys. Geosystems* 18, 2887–2905.
1849 853 <https://doi.org/10.1002/2017GC006912>

1850 854 Pistone, M., Caricchi, L., Ulmer, P., Burlini, L., Ardia, P., Reusser, E., Marone, F., Arbaret, L., 2012.
1851 855 Deformation experiments of bubble- and crystal-bearing magmas: Rheological and
1852 856 microstructural analysis. *J. Geophys. Res.* 117.

1853 857 Rodgers, M., Smith, P.J., Mather, T.A., Pyle, D.M., 2016. Quiescent-explosive transitions during
1854 858 dome-forming volcanic eruptions: Using seismicity to probe the volcanic processes leading to
1855 859 the 29 July 2008 vulcanian explosion of Soufrière Hills Volcano, Montserrat. *J. Geophys.*
1856 860 *Res. Solid Earth* 121, 8453–8471. <https://doi.org/10.1002/2016JB013180>

1857 861 Rust, A.C., Cashman, K.V., 2011. Permeability controls on expansion and size distributions of
1858 862 pyroclasts. *J. Geophys. Res.* 116.

1859 863 Rust, A.C., Cashman, K.V., 2004. Permeability of vesicular silicic magma: inertial and hysteresis
1860 864 effects. *Earth Planet. Sci. Lett.* 228, 93–107.

1861 865 Spieler, O., Kennedy, B., Kueppers, U., Dingwell, D.B., Scheu, B., Taddeucci, J., 2004. The
1862 866 fragmentation threshold of pyroclastic rocks. *Earth Planet. Sci. Lett.* 226, 139–148.

1863 867 Stinton, A.J., Cole, P.D., Odbert, H.M., Christopher, T., Avard, G., Bernstein, M., 2014a. Dome
1864 868 growth and valley fill during Phase 5 (8 October 2009–11 February 2010) at the Soufrière
1865 869 Hills Volcano, Montserrat. *Geol. Soc. Lond. Mem.* 39, 113–131.
1866 870 <https://doi.org/10.1144/M39.6>

1867 871 Stinton, A.J., Cole, P.D., Stewart, R.C., Odbert, H.M., Smith, P., 2014b. The 11 February 2010 partial
1868 872 dome collapse at Soufrière Hills Volcano, Montserrat. *Geol. Soc. Lond. Mem.* 39, 133–152.
1869 873 <https://doi.org/10.1144/M39.7>

1870 874 Taisne, B., Jaupart, C., 2008. Magma degassing and intermittent lava dome growth. *Geophys. Res.*
1871 875 *Lett.* 35.

1872 876 Vasseur, J., & Wadsworth, F. B. (2017). Sphere models for pore geometry and fluid permeability in
1873 877 heterogeneous magmas. *Bulletin of Volcanology*, 79(11), 77.

1874 878 Wadge, G., Robertson, R.E.A., Voight, B., 2014a. The Eruption of Soufriere Hills Volcano,
1875 879 Montserrat from 2000 to 2010. Geological Society of London.

1876 880 Wadge, G., Voight, B., Sparks, R.S.J., Cole, P.D., Loughlin, S.C., Robertson, R.E.A., 2014b. An
1877 881 overview of the eruption of Soufrière Hills Volcano, Montserrat from 2000 to 2010. *Geol.*
1878 882 *Soc. Lond. Mem.* 39, 1–40. <https://doi.org/10.1144/M39.1>

1879 883 Williamson, B.J., Di Muro, A., Horwell, C.J., Spieler, O., Llewellyn, E.W., 2010. Injection of
1880 884 vesicular magma into an andesitic dome at the effusive–explosive transition. *Earth Planet.*
1881 885 *Sci. Lett.* 295, 83–90. <https://doi.org/10.1016/j.epsl.2010.03.027>

1882 886 Wright, H.M.N., Cashman, K.V., Gottesfeld, E.H., Roberts, J.J., 2009. Pore structure of volcanic

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887 clasts: Measurements of permeability and electrical conductivity. *Earth Planet. Sci. Lett.* 280,
888 93–104.
889 Wright, H.M.N., Roberts, J.J., Cashman, K.V., 2006. Permeability of anisotropic tube pumice: Model
890 calculations and measurements. *Geophys. Res. Lett.* 33.
891 Young, N.K., Gottsmann, J., 2015. Shallow crustal mechanics from volumetric strain data: Insights
892 from Soufrière Hills Volcano, Montserrat. *J. Geophys. Res. Solid Earth* 120, 1559–1571.
893 <https://doi.org/10.1002/2014JB011551>

Figure Captions

Fig. 1: Representative pumice from the 2010 event. A) SEM image (BSE) with a red frame surrounding the region selected for textural analysis to avoid corners affected by the vignetting sometimes occurring at $\times 50$ magnification. B) Analyzed region showing the different analyzed objects: oxides (red), plagioclases (green), orthopyroxenes (cyan), clinopyroxenes and amphiboles (blue), matrix (yellow), vesicles with circularity < 0.2 and equivalent size $> 300 \mu\text{m}$ (grey), and other vesicles (black). All objects were discriminated by chemical (EDS) mapping except the large, deformed vesicles that were manually outlined.

Fig. 2: Pre-explosive magmatic columns represented by porosity as a function of pressure and depth. Triangles indicate the average model outputs for each sample, grey areas cover the ranges of outputs of the 10 parametric model runs, and error bars represent the combined effects of natural variability and analytical uncertainty on each sample. The solid black curve indicates closed-system degassing if the pure water saturation pressure is 130 MPa.

Fig. 3: Permeability as a function of connected porosity for various input parameters of two relationships (k_B and k_K). Data are from natural products of dome-forming eruptions at Colima volcano (diamonds, Farquharson et al., 2015; Farquharson et al., 2016) and Soufrière Hills (triangles, Farquharson and Wadsworth, 2018). Black-filled symbols indicate permeability values in the direction parallel to gas channels (vesicles or cracks),

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913 white-filled symbols indicate permeabilities perpendicular to gas channels, and gray-
914 filled symbols indicate permeabilities measured regardless of orientation. The limit
915 between crack- and bubble-supported permeability is from Farquharson et al. (2015) and
916 Kushnir et al. (2016). It also corresponds approximately to the percolation threshold (see
917 text). A) The grey area covers the span of curves that correspond to high mass flux
918 solutions. It is bounded by curves with the highest (dashed line) and lowest (solid line)
919 values of bubble number density (N_T), respectively. The thick continuous curve is the
920 best-fit of all the data for k_K and the dotted curve is the best-fit for k_B . B) The grey area
921 covers the span of curves that correspond to low mass flux solutions. It is bounded by
922 curves with the highest (dashed line) and lowest (solid line) values of bubble number
923 density (N_T), respectively.

Fig. 4: Solutions of the five-parameters sweep that fall within the 95% level of confidence.

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925 Circle sizes are proportional to the number of solutions that have identical values for the
926 parameter pairs represented by graph axes but different combinations of the three other
927 parameters. Circles are colored according to whether they represent high-flux solutions
928 ($10^{2.4}$ – $10^{4.3}$ kg/s, black), low-flux solutions ($10^{-0.6}$ – 10 kg/s, white), or other solutions
929 (grey) that fit neither the observed extrusion rates nor the measured values of N_T and f .
930 A) Bubble number density (N_T) as a function of mass flux (Q). Grey bars indicate the
931 range of values measured by photogrammetry (x-axis) and by textural analysis (y-axis).
932 The dashed line indicates the slope of the relationship between Q and N_T given by Eq.
933 (6). B) Bubble number density (N_T) as a function of the spread in bubble sizes (f). The
934 dashed line marks the limit between solutions that are compatible with a percolation
935 threshold (“yes”) and the solutions that ignore the percolation threshold (“no”).

Fig. 5: Distance covered by a parcel of magma between the explosions of January 8 and
February 11. Curves are calculated by linear interpolation between the observed average

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938 rates of extrusion (Stinton et al., 2014a) and assuming various constant conduit radii (15,
939 25, and 40 m). Stars mark explosion times, and the horizontal dashed line is set at the
940 inferred conduit length of 5 km.

941 **Fig. 6:** Magma ascent time from the reservoir to the surface as a function of conduit radius.
942 Curves are labeled according to the value of mass flux. The dark grey area covers the
943 ascent rates that are compatible with steady-state conduit replenishment. Light grey areas
944 span combinations of mass fluxes and conduit radius that are solutions of the 0D model.
945 Cases of high and low mass flux solutions are indicated by the labels “high Q” and “low
946 Q”, respectively.

947 **Fig. 7:** Comparison of different pre-explosive magmatic columns represented by porosity as a
948 function of pressure. Merapi data are from Drignon et al. (2016). Soufrière Hills Volcano
949 (SHV) data are from Clarke et al. (2007) as reanalyzed by Burgisser et al. (2010) and
950 from Burgisser et al. (2010) (label “1997a”), from Williamson et al. (2010) (label
951 “1997b”), and this study (label “Feb. 11, 2010”).

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Tables

Table 1: Sample phase proportions in vol.%. Values in parenthesis are one standard deviation, not analyzed is “n.a.”, and not detected is “n.d.”. Abbreviations OPx, CPx+A, and Plag respectively mean orthopyroxene, clinopyroxene plus amphibole, and plagioclase.

Sample	Vesicle	Oxide ^a	OPx ^a	CPx+A ^a	Plag ^a	Glass ^a	Quartz ^a	Other ^a
AMO210A	65.3 (1.0)	1.5 (0.9)	5.3 (0.8)	8.9 (0.1)	38.6 (5.5)	45.6 (6.8)	n.d.	n.d.
AMO210B	51.8 (1.6)	3.5 (0.8)	10.1 (0.7)	5.1 (0.4)	38.3 (1.6)	7.5 (2.4)	7.3 (2.4)	28.3 (1.7)
AMO210C	67.8 (1.4)	1.2 (1.5)	2.9 (1.0)	8.4 (7.7)	46 (12)	45 (12)	n.d.	n.d.
AMO210D	54.5 (3.1)	1.9 (1.2)	2.3 (1.0) ^b	4.9 (2.1) ^b	30.3 (3.5)	60.7 (4.8)	0 ^b	0 ^b
AMO210E	71.0 (0.2)	3.9 (2.2)	20.3 (0.8)	7.4 (4.6)	36.2 (3.8)	31.2 (4.0)	n.d.	n.d.
AMO210F	61.5 (1.1)	2.2 (0.4)	4.8 (1.1) ^b	10.0 (2.3) ^b	48.7 (5.3)	34.4 (1.9)	0 ^b	0 ^b
AMO210G	43.5 (5.2)	1.8 (0.1)	7.7 (2.7)	4.7 (1.9)	26.6 (4.9)	37.4 (6.7)	1.1 (0.1)	20.7 (1.2)
AMO210H	55.6 (4.2)	2.8 (1.6)	5.9 (1.3) ^b	12.4 (2.8) ^b	43.4 (5.6)	35.5 (6.5)	0 ^b	0 ^b
AMO210I	59.7 (1.4)	2.4 (2.8)	11.7 (1.0)	3.9 (0.8)	53.8 (9.9)	27.9 (9.3)	n.d.	n.d.
AMO210J	60.1 (2.0)	6.0 (1.1)	4.4 (3.6)	16.0 (0.1)	35.4 (1.9)	23.4 (1.5)	0.2 (0.1)	14.5 (1.0)
AMO210K	73.6 (0.7)	4.1 (4.5)	1.9 (1.2)	1.8 (0.3)	53 (11)	39.2 (7.5)	n.d.	n.d.
AMO210L	63.5 (2.0)	4.0 (0.3)	5.7 (1.2)	8.5 (1.3)	39.5 (4.1)	23.2 (3.9)	0.3 (0.2)	18.7 (0.8)
AMO210Q	69.8 (0.9)	1.3 (0.4)	1.5 (0.7) ^b	3.1 (1.5) ^b	34.2 (5.9)	59.9 (4.5)	0 ^b	0 ^b
WP1.095A	71.7 (0.3)	2.0 (0.1)	5.1 (2.0)	5.4 (3.3)	39.3 (1.1)	48.2 (0.9)	n.d.	n.d.
WP1.095B	56.6 (0.1)	2.4 (0.5)	7.4 (0.7)	4.3 (3.6)	44.6 (4.1)	41.2 (6.7)	n.d.	n.d.
WP1.108A	62.9 (0.2)	3.0 (1.0)	3.1 (0.5)	1.7 (0.3)	44.1 (5.0)	47.9 (4.7)	n.d.	n.d.
WP1.108B	77.4 (0.8)	1.1 (0.1)	2.3 (0.1)	5.2 (0.4)	39.5 (1.2)	51.7 (3.0)	n.d.	n.d.
WP2.200A	77.1 (0.2)	1.2 (0.04)	10 (10)	7.6 (0.1)	44.5 (6.1)	36.6 (3.6)	n.d.	n.d.
WP2.200B	74.5 (0.5)	3.6 (1.0)	1.6 (0.1)	2.2 (0.4)	34.6 (0.6)	57.9 (2.8)	n.d.	n.d.
WP2.201A	76.7 (0.1)	1.5 (1.4)	2.0 (0.7)	3.0 (3.5)	52.2 (3.7)	41.3 (3.7)	n.d.	n.d.
WP2.201B	77.8 (0.1)	0.3 (0.4)	3.1 (1.6)	4.0 (2.7)	43.5 (0.4)	49.2 (4.8)	n.d.	n.d.
WP2.329A	58.4 (0.7)	2.2 (1.0)	4.3 (1.8)	11.2 (0.3)	9.0 (3.6)	73.2 (5.7)	n.d.	n.d.
WP2.329B	70.6 (1.1)	2.5 (0.7)	37.3 (0.4)	4.3 (0.4)	20.6 (1.3)	34.7 (2.4)	n.d.	n.d.

^a Bubble-free values.

^b Small magnification image was a slice from a tomography scan. Values were determined by assuming that all the segmented minerals minus plagioclases and oxides were ferromagnesian minerals and using the ratio $(CPx+A)/(CPx+A+OPx) = 0.68$ and $OPx/(CPx+A+OPx) = 0.32$ (Murphy et al., 2000).

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964 **Table 2:** Sample glass water contents and textural characteristics. Values in parenthesis are one
965 standard deviation. Columns “Syn isol”, “Syn conn”, and “Pre conn” respectively represent the
966 proportions (to 100%) of syn-explosive and isolated vesicles, syn-explosive and connected vesicles,
967 and pre-explosive and connected vesicles. Not analyzed is “n.a.” and N_T are bubble-free number
968 densities.

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Sample	H ₂ O bulk (wt.%)	H ₂ O glass (wt.%)	Syn isol	Syn conn	Pre Conn	Bubble N_T (m ⁻³)	Oxide N_T (m ⁻³)
AMO210A	0.89 (0.049)	1.64 (0.33)	0.9	91.0	8.1	3.6×10^{15} (1.2×10^{14})	2.1×10^{18} (5.3×10^{16})
AMO210B	0.56 (0.031)	7.43 (2.44)	1.3	94.0	4.7	1.2×10^{16} (4.6×10^{14})	1.1×10^{17} (3.7×10^{15})
AMO210C	1.03 (0.057)	1.97 (0.83)	1.2	87.1	11.7	1.5×10^{16} (4.0×10^{14})	1.1×10^{16} (5.0×10^{14})
AMO210D	0.55 (0.030)	0.75 (0.14)	2.1	94.3	3.6	1.5×10^{16} (4.2×10^{14})	1.3×10^{17} (4.4×10^{15})
AMO210E	0.70 (0.077)	2.03 (0.59)	0.4	82.0	17.6	2.0×10^{16} (6.2×10^{14})	1.1×10^{17} (4.5×10^{15})
AMO210F	0.69 (0.049)	1.47 (0.29)	1.5	92.3	6.2	2.2×10^{16} (6.2×10^{14})	1.1×10^{17} (4.4×10^{15})
AMO210G	0.74 (0.041)	1.99 (0.46)	2.1	89.2	8.7	1.2×10^{16} (3.3×10^{14})	1.1×10^{17} (4.0×10^{15})
AMO210H	0.52 (0.029)	0.73 (0.31)	1.0	83.4	15.6	3.8×10^{16} (7.7×10^{14})	2.4×10^{17} (6.5×10^{15})
AMO210I	n.a.	n.a.	n.a.	n.a.	n.a.	2.3×10^{16} (6.0×10^{14})	1.9×10^{17} (5.9×10^{15})
AMO210J	n.a.	n.a.	n.a.	n.a.	n.a.	3.2×10^{16} (8.2×10^{14})	3.7×10^{17} (1.0×10^{16})
AMO210K	n.a.	n.a.	n.a.	n.a.	n.a.	1.3×10^{16} (3.5×10^{14})	1.2×10^{17} (4.1×10^{15})
AMO210L	0.55 (0.030)	1.88 (0.41)	0.2	92.2	7.6	1.6×10^{16} (4.2×10^{14})	4.9×10^{17} (1.8×10^{16})
AMO210Q	1.00 (0.055)	1.63 (0.22)	0.4	86.1	13.5	7.7×10^{15} (1.8×10^{14})	3.2×10^{17} (9.4×10^{15})
WP1.095A	0.55 (0.030)	0.95 (0.20)	0.5	89.8	9.6	1.9×10^{16} (4.4×10^{14})	3.9×10^{16} (1.6×10^{15})
WP1.095B	0.44 (0.024)	0.89 (0.29)	0.9	82.8	16.2	2.1×10^{16} (5.3×10^{14})	5.3×10^{16} (2.0×10^{15})
WP1.108A	0.66 (0.019)	1.41 (0.18)	0.7	88.8	10.5	1.5×10^{16} (3.9×10^{14})	2.5×10^{17} (6.8×10^{15})
WP1.108B	1.12 (0.027)	2.05 (0.15)	0.3	67.0	32.7	1.4×10^{16} (3.1×10^{14})	8.9×10^{16} (2.4×10^{15})
WP2.200A	0.56 (0.031)	1.16 (0.29)	0.3	92.5	7.3	1.5×10^{16} (4.3×10^{14})	2.9×10^{17} (8.8×10^{15})
WP2.200B	0.65 (0.023)	1.11 (0.08)	0.2	92.2	7.6	3.1×10^{16} (4.9×10^{14})	6.1×10^{15} (3.1×10^{14})
WP2.201A	0.54 (0.035)	1.20 (0.28)	0.2	87.6	12.2	2.7×10^{16} (5.6×10^{14})	3.8×10^{16} (1.4×10^{15})
WP2.201B	1.09 (0.11)	2.16 (0.39)	0.1	88.1	11.8	2.0×10^{16} (4.2×10^{14})	6.1×10^{15} (2.3×10^{14})
WP2.329A	0.56 (0.004)	0.43 (0.07)	0.3	73.0	26.7	4.7×10^{16} (7.0×10^{14})	1.2×10^{17} (3.4×10^{15})
WP2.329B	0.55 (0.005)	1.59 (0.13)	0.1	89.6	10.3	2.6×10^{16} (4.2×10^{14})	9.5×10^{16} (2.9×10^{15})

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972 **Table 3:** Results on the pre-explosive conduit conditions. Values in parenthesis are one
973 standard deviation and the plus and minus signs indicate positive and negative errors. Total gas is the
974 total amount of syn-explosive gas. Depths are measured from the vent down and are considering
975 respectively magma-static (Magm. depth) and litho-static (Lith. depth) conduit pressure gradient.

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Sample	Melt H ₂ O (wt%)	Pressure (MPa)	Porosity (vol.%)	Total gas (wt%)	Magm. depth (km)	Lith. depth (km)
AMO210A	2.27 (0.32)	38.7 (+9.3,-10.3)	2.818 (0.027)	0.73	1.7	1.5
AMO210C	2.65 (0.82)	50.8 (+24.7,-30.7)	2.331 (0.038)	0.79	2.2	2.0
AMO210D	1.23 (0.14)	12.7 (+2.5,-2.8)	6.243 (0.061)	0.55	0.6	0.5
AMO210E	2.79 (0.58)	55.6 (+18.9,-21.8)	2.370 (0.007)	0.88	2.4	2.2
AMO210F	2.04 (0.29)	31.9 (+7.8,-8.6)	3.070 (0.028)	0.66	1.4	1.2
AMO210G	2.37 (0.45)	41.7 (+13.2,-15.1)	1.603 (0.049)	0.44	1.8	1.6
AMO210H	1.22 (0.31)	12.5 (+5.2,-6.4)	6.505 (0.081)	0.57	0.6	0.5
AMO210L	2.48 (0.41)	45.3 (+12.5,-14.1)	2.300 (0.047)	0.69	2.0	1.8
AMO210Q	2.36 (0.22)	41.4 (+6.6,-7.1)	3.029 (0.029)	0.84	1.8	1.6
WP1.095A	1.73 (0.19)	23.7 (+4.6,-5.0)	5.504 (0.006)	0.89	1.1	0.9
WP1.095B	1.40 (0.29)	16.1 (+5.6,-6.7)	5.258 (0.002)	0.58	0.7	0.6
WP1.108A	2.00 (0.18)	30.7 (+4.7,-5.1)	3.290 (0.005)	0.68	1.4	1.2
WP1.108B	3.02 (0.15)	64.0 (+5.4,-5.6)	2.637 (0.033)	1.12	2.8	2.5
WP2.200A	2.12 (0.29)	34.3 (+7.9,-8.8)	4.756 (0.006)	1.11	1.5	1.3
WP2.200B	1.98 (0.08)	30.3 (+2.2,-2.3)	4.821 (0.015)	1.00	1.4	1.2
WP2.201A	2.15 (0.28)	35.2 (+7.8,-8.6)	4.570 (0.004)	1.09	1.6	1.4
WP2.201B	3.15 (0.38)	68.8 (+14.0,-15.2)	2.508 (0.005)	1.15	3.0	2.7
WP2.329A	0.96 (0.07)	8.0 (+1.0,-1.1)	10.436 (0.003)	0.60	0.4	0.3
WP2.329B	2.34 (0.12)	40.8 (+3.8,-3.9)	3.154 (0.035)	0.86	1.8	1.6

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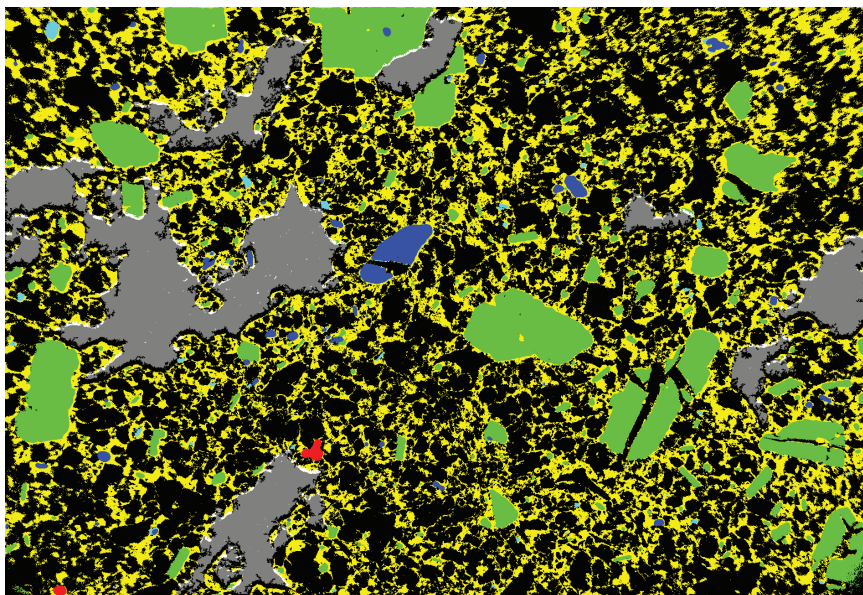
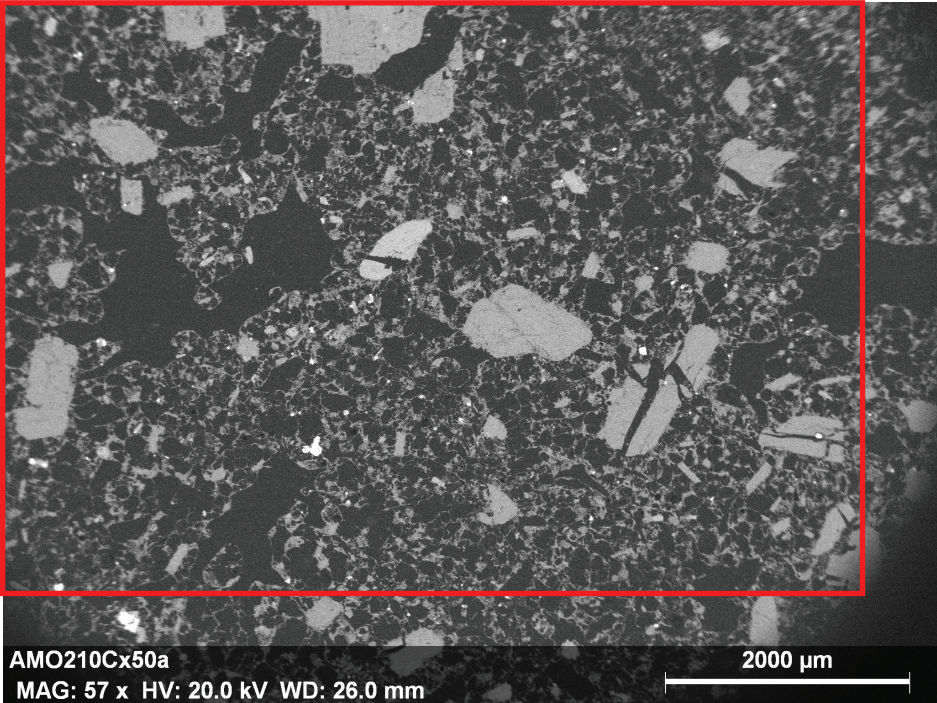


FIGURE 1

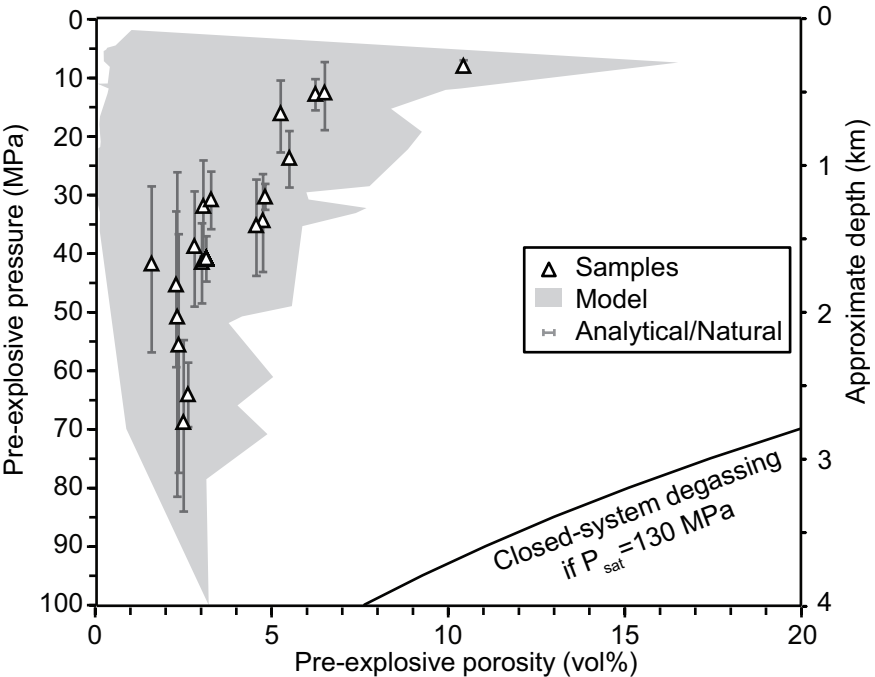


FIGURE 2

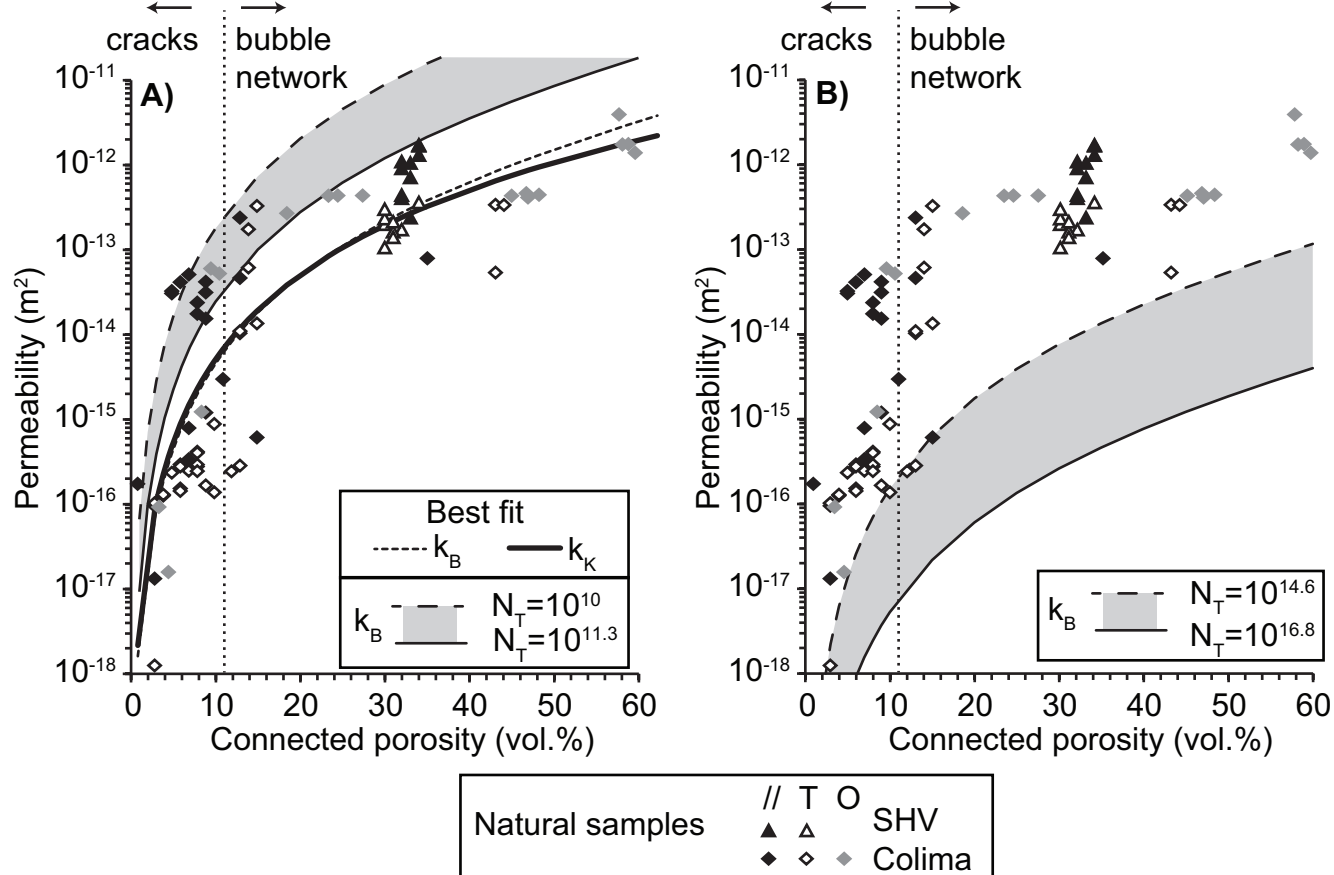


FIGURE 3

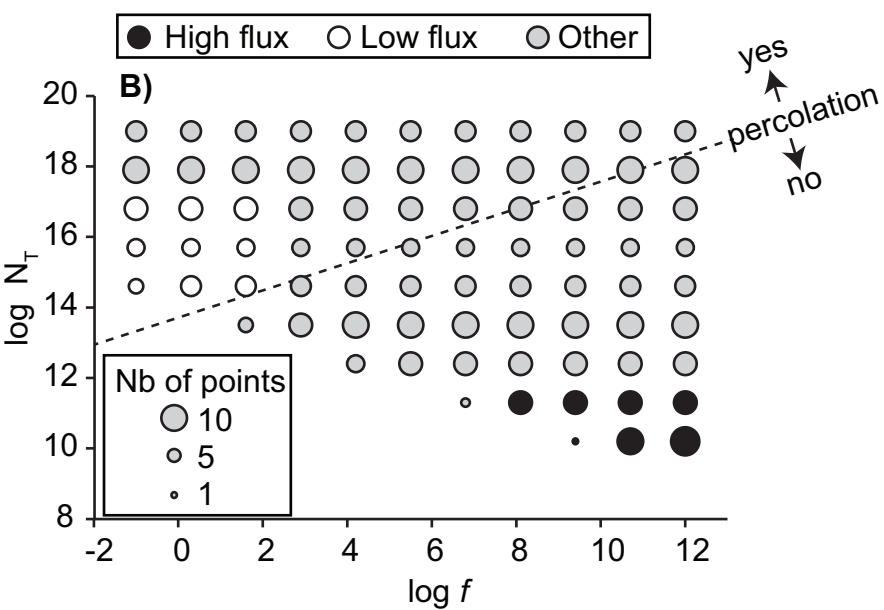
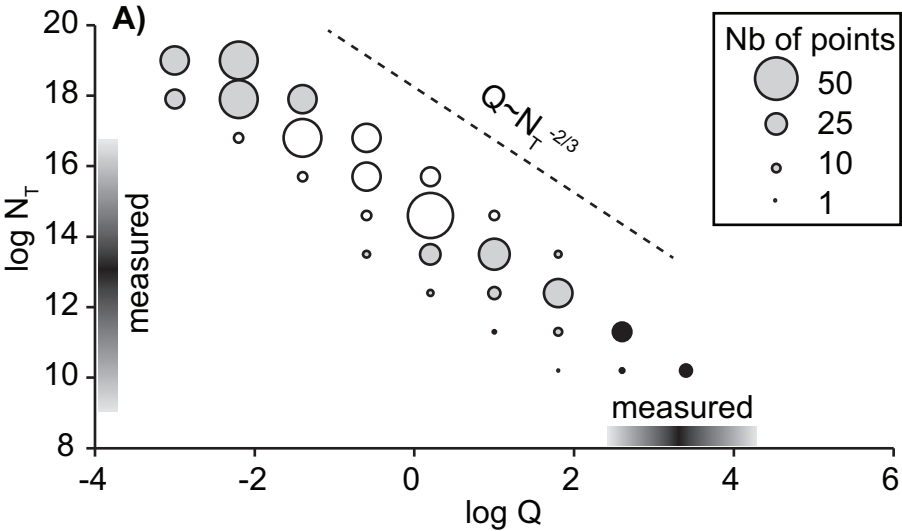


FIGURE 4

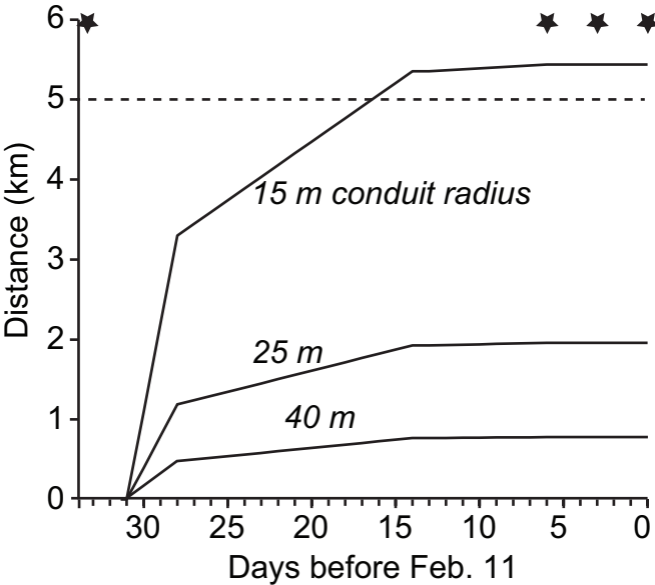


FIGURE 5

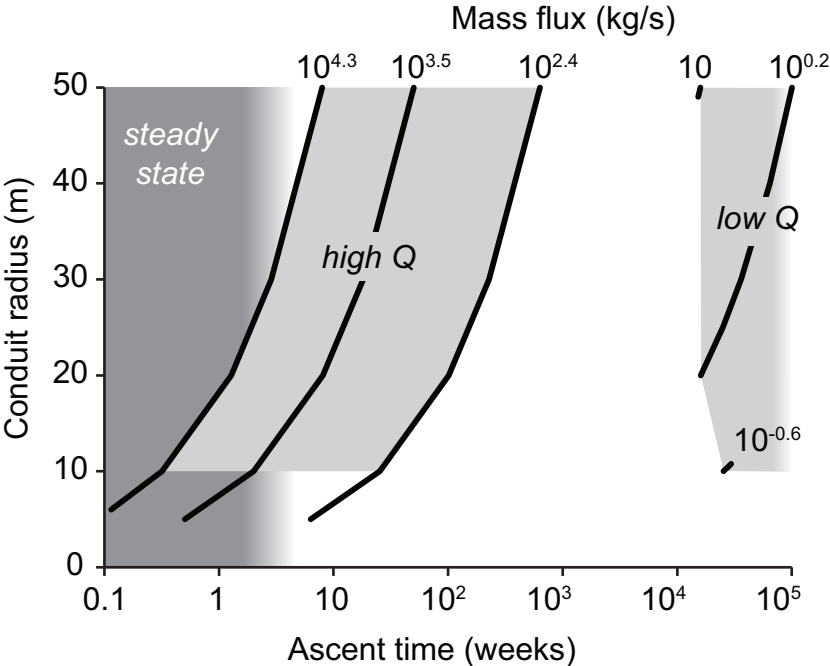


FIGURE 6

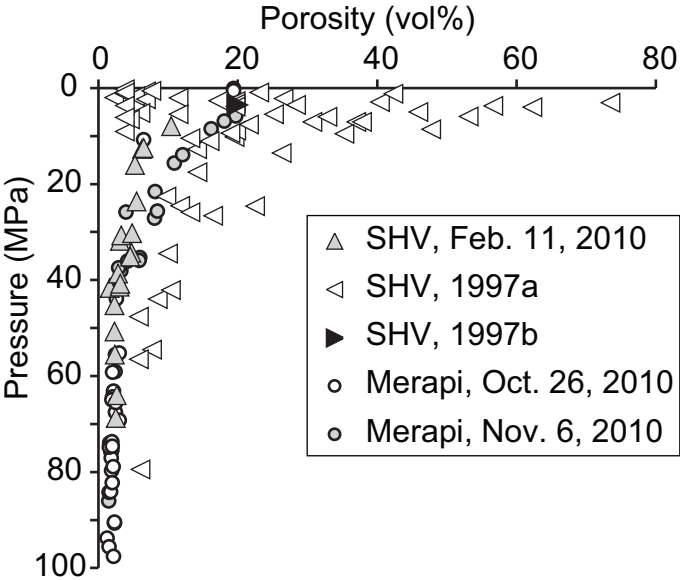


FIGURE 7

Conduit processes during the February 11, 2010 Vulcanian eruption of Soufrière Hills, Montserrat

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Supplementary Information

This Supplementary Information includes text providing additional details on the textural analysis and the conduit flow modeling (Text S1–S5), one table with GPS coordinates of the sampling locations (Table S1), and 6 figures (Figs. S1–S6).

Supplementary Text S1.

Weight fractions of water in the glass, X_{gl} , were calculated by neglecting the weight of the vesicles:

$$X_{gl} = \frac{X_{bulk} \sum_i V_i \rho_i - X_a C V_{a+cpx} \rho_a}{V_{gl} \rho_{gl}} \quad (S1)$$

where X_{bulk} is the bulk H₂O weight fraction, $X_a = 0.02$ is the H₂O weight fraction in amphibole, $C = 0.95$ is the assumed constant ratio between the volume fraction of amphibole and that of amphibole plus clinopyroxene (Murphy et al., 2000), V_i are volume fractions, and ρ_i are densities. The sum is $\sum_i V_i \rho_i = V_{opx} \rho_{opx} + V_{a+cpx} \rho_{a+cpx} + V_{al} \rho_{al} + V_{ox} \rho_{ox} + V_{qz} \rho_{qz} + V_{plg} \rho_{plg} + V_{oth} \rho_{oth}$ and the subscripts *opx*, *a+cpx*, *gl*, *ox*, *qz*, *plg*, *oth*, and *a* mean orthopyroxene, amphibole plus clinopyroxene, glass, oxide, quartz, plagioclase, other, and amphibole, respectively and where densities are $\rho_{opx} = \rho_{a+cpx} = \rho_a = \rho_{oth} = 3300 \text{ kg/m}^3$, $\rho_{gl} = 2380 \text{ kg/m}^3$, $\rho_{ox} = 4720 \text{ kg/m}^3$, $\rho_{qz} = 2650 \text{ kg/m}^3$, and $\rho_{plg} = 2570 \text{ kg/m}^3$. Uncertainties on X_{gl} were calculated by error propagation (Drignon et al., 2016). The mineral separation procedure from Drignon et al. (2016) was adjusted to the phases present in our samples (Fig. 1B). Let F_j be the final binary images with the additional subscripts *ves* and *m+gl* being vesicles and matrix plus glass, respectively. Let I_k be the segmented elemental images per zoom level with $k = \text{Al, Si-m, Si-h, Fe-h, Fe-m, Mg, and Ca}$ (*X-m* and *X-h* are medium and high threshold levels). The series of Boolean manipulations to obtain the final images reads:

$$\begin{aligned} F_{ves} &= I_{ves} \text{ OR NOT}(I_{Al} \text{ OR } I_{Ca} \text{ OR } I_{Fe} \text{ OR } I_{Mg} \text{ OR } I_{Si-h} \text{ OR } I_{Si-m} \text{ OR } I_{Fe-h} \text{ OR } I_{Fe-m}) \\ F_{ox} &= I_{Fe-h} \\ J_i &= I_i - F_{ves} - F_{ox} \\ F_{a+cpx} &= J_{Ca} \text{ AND } J_{Mg} \\ K_i &= J_i - F_{a+cpx} \\ F_{opx} &= K_{Fe-m} \text{ AND } K_{Mg} \\ L_i &= K_i - F_{opx} \\ F_{plg} &= L_{Ca} \text{ AND } L_{Al} \\ M_i &= L_i - F_{plg} \\ F_{qz} &= M_{Si-h} \\ N_i &= M_i - F_{qz} \\ F_{m+gl} &= N_{Ca} \text{ OR } N_{Fe-m} \text{ OR } N_{Mg} \text{ OR } N_{Si-m} \text{ OR } N_{Si-h} \text{ OR } N_{Al} \\ F_{oth} &= 100\% - F_{ves} - F_{ox} - F_{a+cpx} - F_{opx} - F_{plg} - F_{qz} - F_{m+gl} \end{aligned} \quad (S2)$$

The sign minus implies image subtraction so that $A-B$ corresponds to $A \text{ AND NOT } B$ in Boolean notation, and 100% corresponds to a full image area. Figure S2 illustrates the steps summarized by Eq. (S2)

Supplementary Text S2.

Figure S4 shows how bubble and oxide number densities were calculated by combining two image magnifications for sample AMO210A. This sample features a strong mismatch of size distribution between the two magnifications around 30 μm . The reconstruction procedure smooths this mismatch and creates a break in slope that translates into an apparent bimodality of the distribution across that length scale. The bubble-free number density reported in Table 2, however, is a cumulative sum of the distribution shown in Fig. S4. The cumulative sum is not sensitive to this artifact because it affects a number of bubbles much smaller (typically by 2–3 orders of magnitude) than that of the sum.

Supplementary Text S3.

Figure S5 shows bubble-free crystal content as a function of pre-explosive pressure. The natural variability far exceeds the trend calculated by a fit based on experimental data of crystal growth kinetics in the Soufriere Hills Volcano magma (Kozono and Koyaguchi, 2010), so we opted for a constant, average value of

crystal content.

Table S1: Sample locations in standard UTM zone 20N coordinates.

Location	Easting	Northing	Elevation (m)	Location
AMO210	589338	1852498	24	Farm River valley
WP1.095	588597	1851421	259	Harris Lookout
WP1.108	590487	1851591	33	Spanish Point
WP2.200	589696	1850761	116	White's Bottom Ghaut
WP2.201	590067	1850532	94	White's Bottom Ghaut
WP2.329b	588373	1851291	279	Harris Lookout

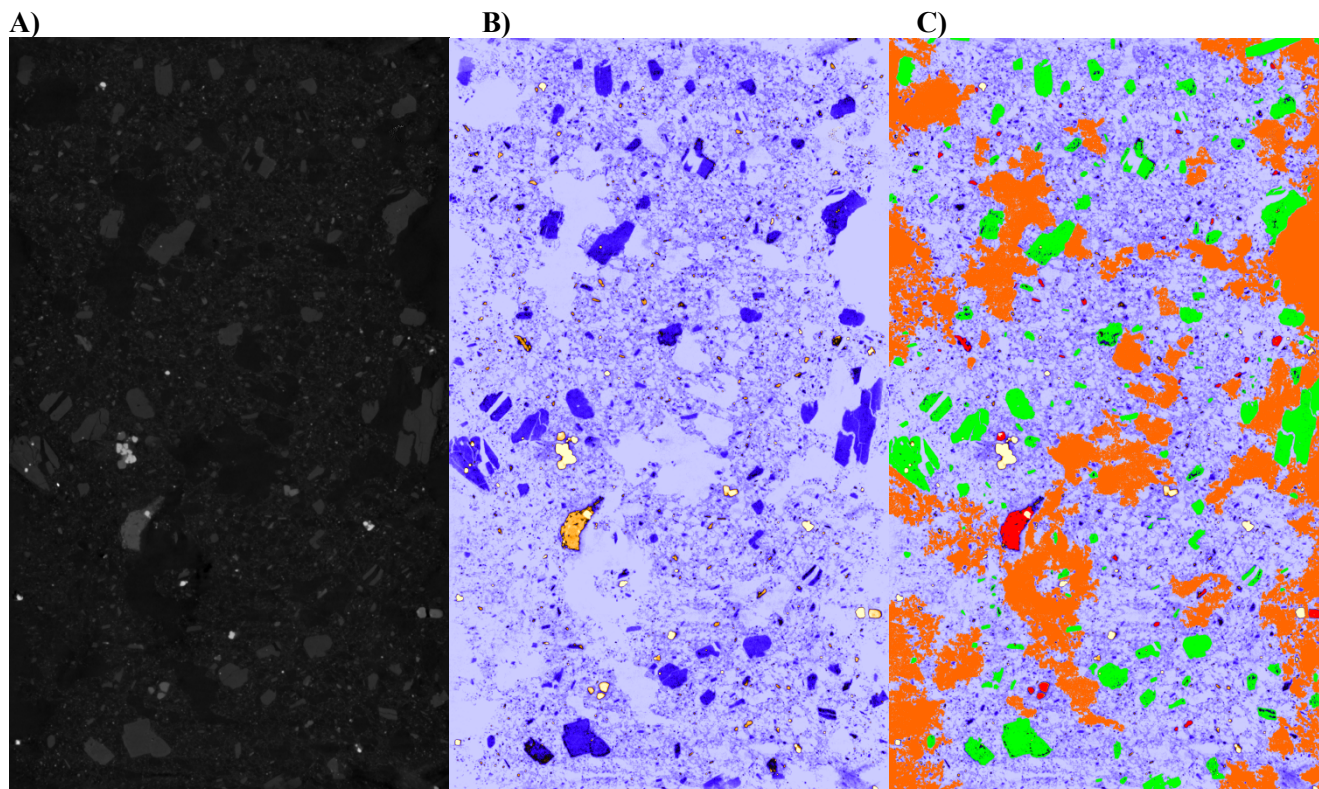


Figure S1: Representative tomographic slice of sample AMO210Q. Each image spans 1.34 cm horizontally. A) Grayscale image of X-ray attenuation levels. B) Same image as A) but with a color scheme highlighting the different mineral phases to aid automatic and manual segmentations. C) Segmented image. Analyzed objects are oxides (pale yellow), plagioclases (green), other minerals (red to dark yellow shades), matrix (dark shades of blue), vesicles with circularity < 0.2 and equivalent size $> 300 \mu\text{m}$ (orange), and other vesicles (light blue).

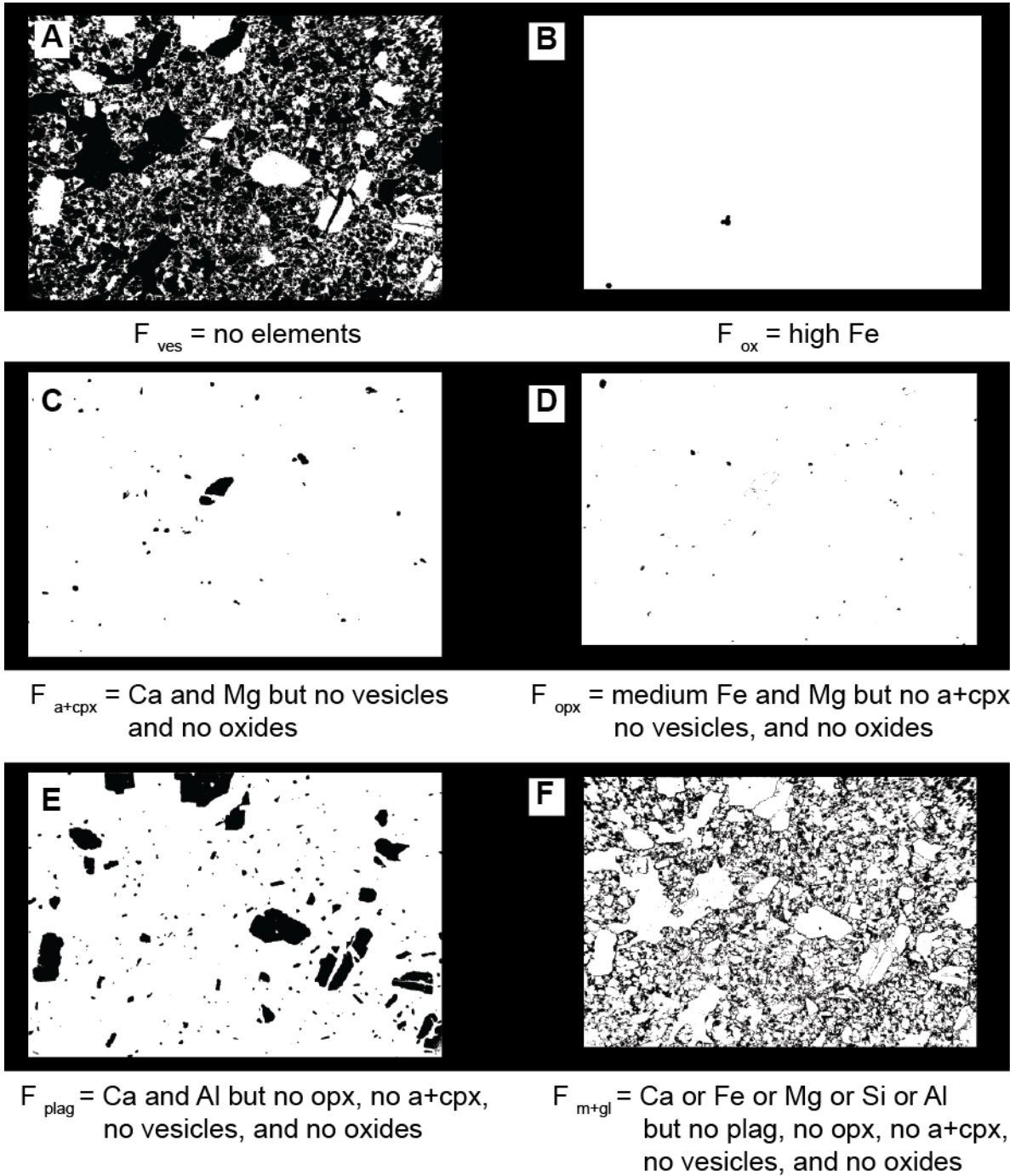


Figure S2: Mineral phase quantification by EDS for sample AMO210C (same image as that of Fig. 1). Images A)–F) correspond to the successive steps summarized in Eq. (S2) that result in the composite image on Fig. 1B.

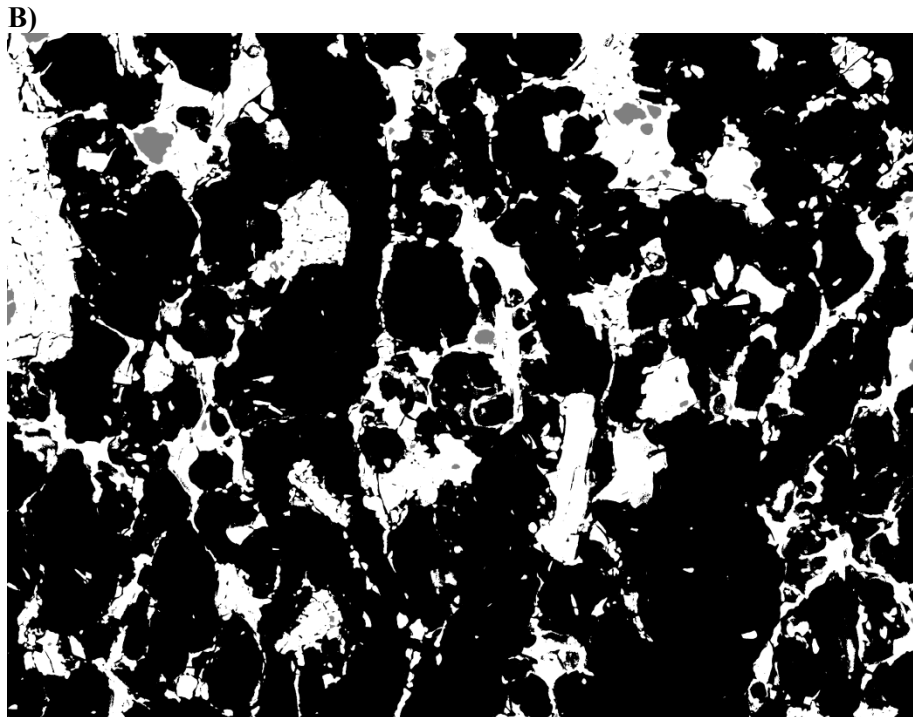
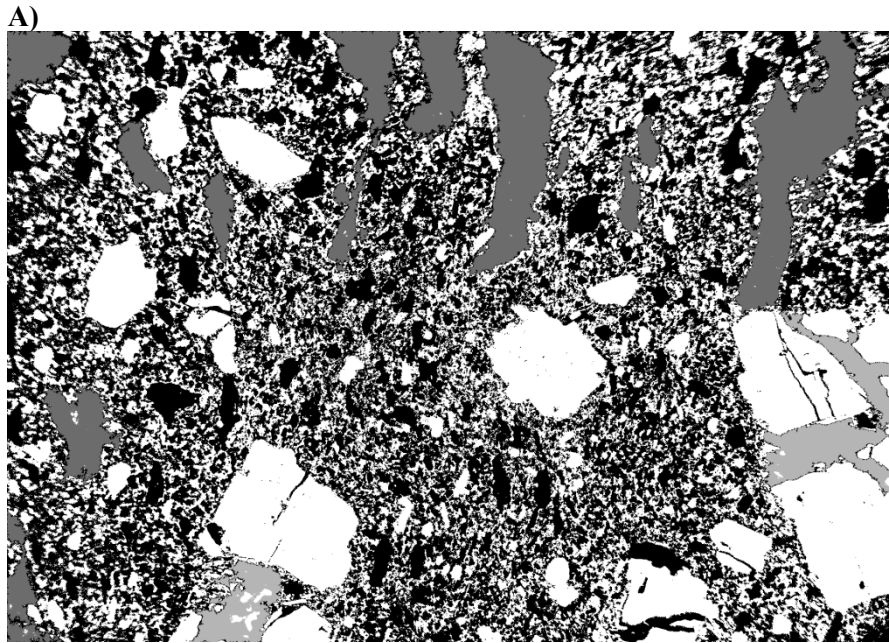


Figure S3: Representative pumice WP1.059B from the 2010 event. Minerals and glass are white. A) Composite grayscale $\times 50$ image spanning 7 mm horizontally that contains parts of three of the four vesicle populations. Large vesicles $>300\ \mu\text{m}$ across and circularity <0.2 are divided into two populations. Population 1 (light grey) is composed of large, syn-explosive angular voids existing between crystal fragments that were segmented by hand. Population 2 (dark grey) is composed of the remaining large vesicles, which are classified as pre-explosive. The coarse part of population 3 (black) is composed of all the vesicles that do not belong to the first two populations. B) Composite grayscale $\times 1000$ image spanning $436\ \mu\text{m}$ horizontally that contains parts of populations 3 and 4. Black vesicles compose the fine part of population 3. Population 4 (grey) is composed of rounded, syn-eruptive vesicles $<50\ \mu\text{m}$ across and circularity >0.4 .

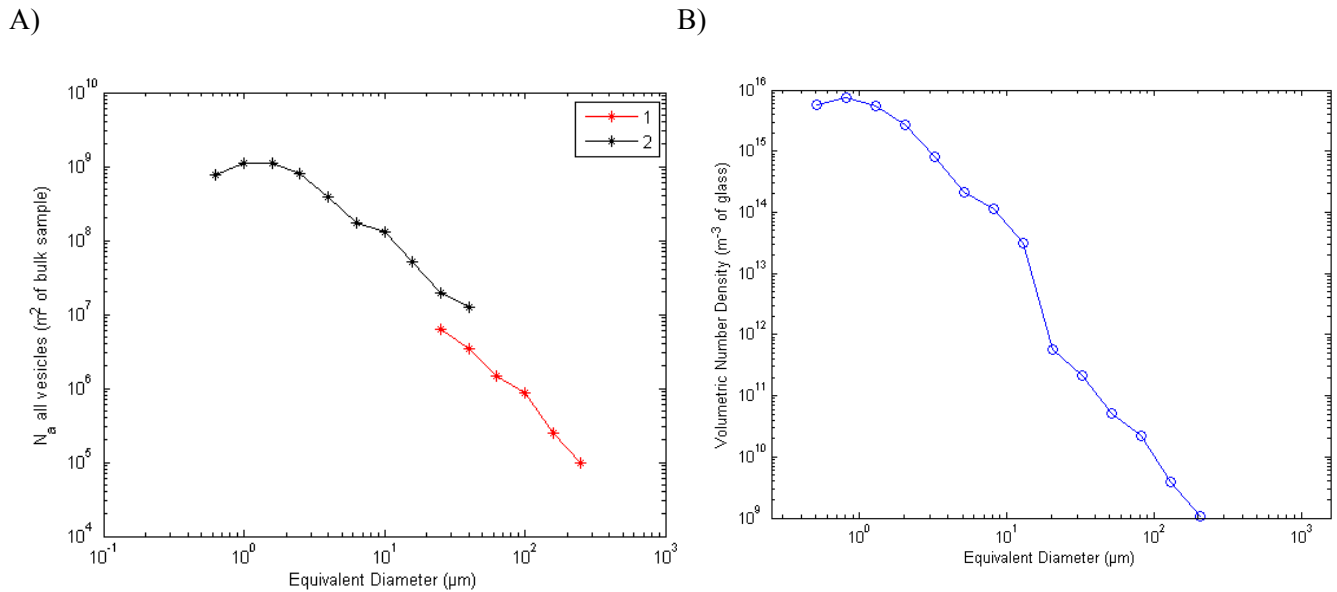


Figure S4: Bubble size distribution reconstruction of sample AMO210A following the method by Giachetti et al. (2010). A) Number of all vesicles per m^2 of glass for each magnification used (1: $\times 2000$ and 2: $\times 50$). B) Combination of the 2 magnifications with a cut-off of $30 \mu m$ followed by 3D conversion obtained using 2D data and stereological transformations from Cheng and Lemlich (1983). The number density reported in Table 2 for AMO210A is the cumulative sum of the distribution in B).

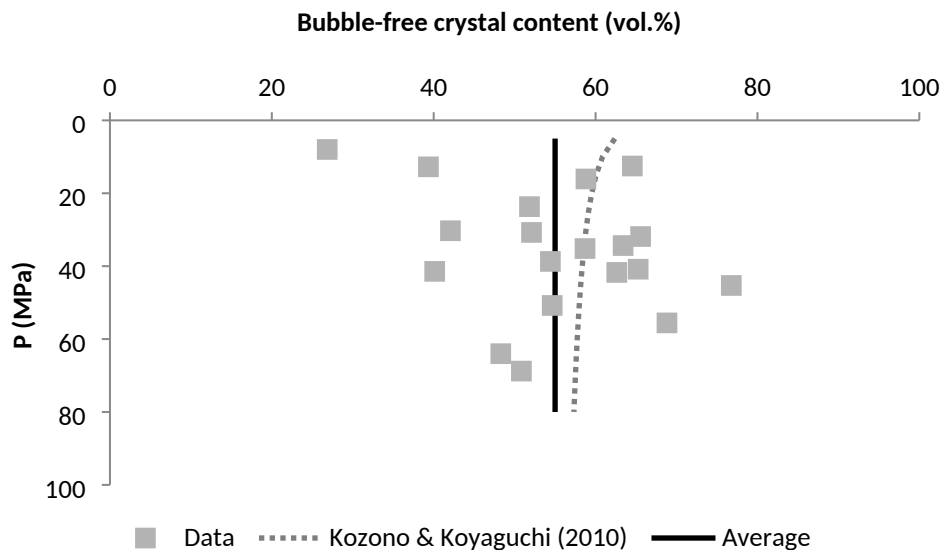


Figure S5: Sample crystal contents (squares) as a function of pre-explosive pressure (P). The vertical line indicates the average value of 55 vol.% that we chose in our simulations. The dotted line corresponds to the fit based on experimental data of crystal growth kinetics for the Soufriere Hills Volcano magma used by Kozono and Koyaguchi (2010).

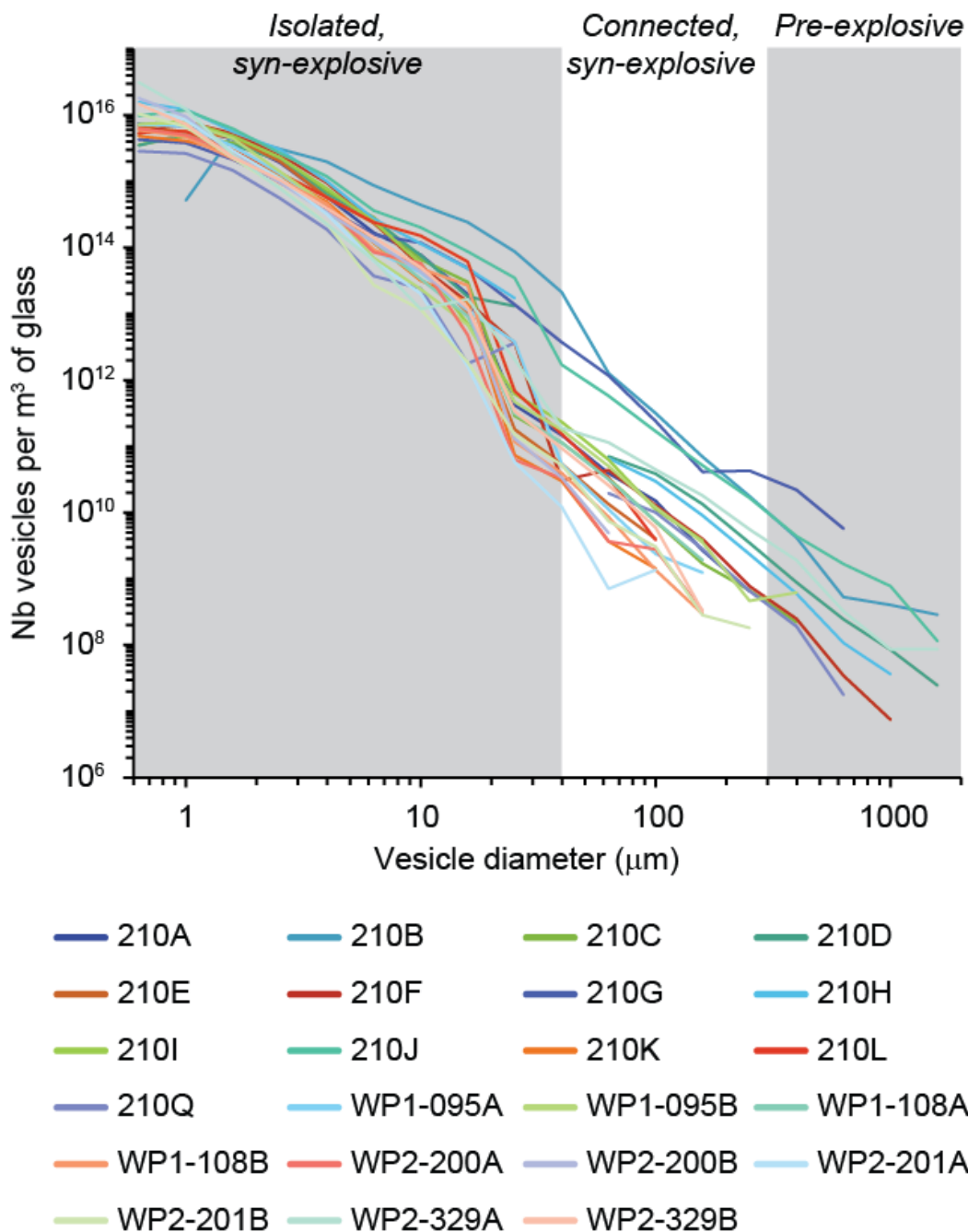


Figure S6: Bubble size distributions of samples listed in Table 2. Vertical boundaries roughly correspond to vesicle origin (pre- or syn-explosive). These boundaries are only indicative because the origin discrimination is made on the joint basis of size and circularity.