1 Physical conditions and frictional properties in a slow slip event source region 2

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- 1819 Abstract:

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22 Recent geodetic studies have shown that slow slip events can occur on subduction 23 faults, including their shallow (< 15 km depth) parts where tsunamis are also generated. Although observations of such events are now widespread, the physical 24 25 conditions promoting shallow slow-slip events remain poorly understood. Here, we use full waveform inversion of controlled-source seismic data from the central 26 Hikurangi (New Zealand) subduction margin to constrain the physical conditions 27 28 in a region hosting slow slip. We find that the subduction fault is characterized by 29 compliant, overpressured and mechanically weak material. We identify sharp lateral variations in pore pressure, which reflect focused fluid flow along thrust 30 faults and have a fundamental influence on the distribution of mechanical 31 32 properties and frictional stability along the subduction fault. We then use highresolution data-derived mechanical properties to underpin rate-state friction 33 models of slow slip. These models show that shallow subduction fault rocks must 34 be nearly velocity-neutral to generate shallow frictional slow slip. Our results have 35 implications for understanding fault loading processes and slow transient fault slip 36 along megathrust faults. 37

39 In the last two decades, one of the most important advances in earthquake science has 40 been the discovery of a spectrum of transient slip-phenomena, such as slow slip-events 41 (SSEs), which occupy the continuum between fast, seismic slip (seconds) through to 42 steady, aseismic creep at plate motion rates. SSEs can last days to years and are widely 43 viewed as manifestations of conditional fault zone stability, in the transition from stick-slip 44 (velocity weakening) behavior to stable sliding (velocity strengthening) behavior^{1,2}. 45 However, the underlying physical mechanism for episodic, aseismic slip remains unclear 46 and there are a number of parameters including rock physical properties, low effective 47 stress linked to elevated pore-fluid pressure, and structural and/or lithological heterogeneities that may give rise to this phenomenon²⁻⁵. Better constraints on the 48 49 structural and physical conditions within the conditionally stable, SSE-hosting region of 50 megathrust faults is therefore crucial for understanding mechanisms of slow transient fault 51 slip, and their relationship to damaging seismic slip events.

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Seismic attributes^{6,7} and velocity images⁸⁻¹¹ from active-source seismic data provide an opportunity to infer the elastic properties and stress state of the plate interface and overlying accretionary wedge, particularly for shallow (<15 km deep) SSE regions where such methods can provide high-resolution results. SSEs at the central and northern Hikurangi subduction margin (HSM) occur at <15km depth^{12,13}, placing the SSE source within range of modern seismic imaging techniques such as full waveform inversion (FWI)¹⁴, from which high-resolution physical models of the Earth can be inferred¹⁵⁻¹⁶.

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61 In 2005, a regional grid of ~2800-line km of multichannel seismic (MCS) data (survey 05CM) was collected along the HSM¹⁷ (Fig. 1). Here, we derive elastic models of the 62 63 central HSM, through a combination of traveltime tomography and elastic FWI of downward extrapolated MCS data¹⁸⁻²⁰, along profile 05CM-38 (Methods, Figs. 2 and 3, 64 65 Extended Data Figs. 1, 2, 3, 4 and 5, Supplementary Videos 1, 2 and 3). This profile 66 spans the southern end of a region of shallow slow slip, within the along-strike transition from an interseismically locked megathrust in the south to an aseismically creeping 67 68 megathrust in the north¹³. Well-characterized SSEs typically occur here every 5 years, lasting 2-3 weeks, at <15 km below the seafloor^{13,21-22}. This region also hosted an SSE 69 70 that was dynamically triggered by the 2016 Mw 7.8 Kaikoura earthquake, over 250 km 71 away²¹⁻²². Following FWI of the MCS data, we estimate pore pressure and in-situ stresses 72 within the accretionary wedge by applying calibrated empirical relations between compressional P-wave velocity, porosity and effective stress¹⁰ (Methods). We then use 73 74 the physical parameters constrained by FWI to construct rate-state friction (RSF) models²³ of the shallow HSM, to investigate how upper plate strength and pore fluid 75 76 pressure influence slow-slip fault behavior. This study represents the first time that highly 77 detailed data on physical properties have been utilized to constrain such models.

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79 **Geological Setting.**

The HSM accommodates westward subduction of the Pacific Plate beneath the East Coast of New Zealand's North Island. In this area, the subducting Pacific Plate is composed of the Hikurangi Plateau, a Cretaceous Large Igneous Province²⁴. A broad sedimentary wedge has been accreted outboard of an actively deforming foundation of

84 pre-subduction Cretaceous and Paleogene marine formations that emerge above sealevel along the East Coast of North island^{25,26} (Fig 2). The incoming plate sequence is 85 86 comprised of volcanics and volcaniclastics of the Hikurangi Plateau and sedimentary 87 sequences overlying the Plateau (Fig. 2). Along our seismic transect, subducted unit 4 is 88 interpreted as a sequence of chalks and mudstones, while above reflector R7, unit 3 is inferred to consist of nannofossil chalks interbedded with tephras and clays²⁵. Reflector 89 90 R5B corresponds to a major regional unconformity, overlain by a >3 km thick, shale-rich 91 (53-80%) turbidite sequence and slope basin sediments (units 0 to 2; stratigraphic 92 nomenclature from ref.²⁶; Fig. 2). The subduction fault lies between units 3 and 4 in this 93 region (thick dashed line, Figs 2 and 3).

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95 Structural and physical characteristics of the HSM

96 We perform an advanced inversion and analysis of 12-km-long-offset seismic reflection 97 data across the central HSM using elastic time-domain FWI and reverse time migration 98 (RTM, Methods). Our results provide high-resolution models of elastic properties (i.e. P-99 wave velocity, ratio of P- and S-wave velocities, Lamé parameters) that show improve 100 correlations with lithostratigraphic interpretations (Figs. 2 and 3, Extended Data Figs. 1-2, Supplementary Figs. 1, 2), compared to earlier analyses^{17,27}. The P-wave velocity 101 102 model is then used to derive wedge mechanical properties and stress state (e.g. pore 103 fluid pressure, Fig. 3, Methods).

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Overall, this section of margin wedge is characterized by P-wave velocities ranging from
 ~1.6 km/s at the seafloor to a maximum of ~4.75 km/s at 7.5 km depth. Below the bottom

107 simulating reflector (BSR) and in the vicinity of the subduction fault (Figs. 2 and 3), 108 velocities strongly deviate from a normal compaction trend and suggest porosity 109 preservation associated with the presence of free gas and/or pressurized fluids²⁷. Within 110 the margin wedge, bulk moduli range from ~5 GPa at the seafloor to 17–32 GPa at ~7.5 111 km depth. Similarly, the shear modulus of the upper plate ranges from <1 GPa at the 112 seafloor to 6–14 GPa near the decollement (Fig. 3, Extended Data Figs. 6-7). We estimate 113 uncertainties in the final elastic parameters to be at most $\pm 20\%$ (Extended Data Fig. 7). 114 Low effective stress (<40 MPa) conditions are present throughout the wedge, linked to 115 elevated Hubbert-Rubey pore fluid pressure ratio (λ^* , Methods) values up to 0.89 along 116 the entire section (Fig. 3), which testify to the widespread overpressured nature of the 117 offshore central HSM. This last observation is in good agreement with the widespread 118 evidence of low permeability, clay-rich formations, acting as effective seals to vertical fluid flow²⁸. 119

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121 From east to west, we identify four structural domains for the margin wedge (Fig. 2). The active protothrust zone²⁹ is characterized by low-velocity sediments and high pore-fluid 122 pressures in the lower half of the section (units 3 and 4). Progressing landward, the outer 123 124 and inner Neogene accretionary wedges are differentiated by the degree of macro-scale deformation and shortening, ~5% and ~24% respectively. ~65 km from the trench, a 125 126 westward increase in velocity (+0.5 km/s, at ~3.5 km depth) marks the boundary between 127 the Neogene accretionary wedge and the deforming foundation of pre-subduction, 128 Cretaceous to Paleogene rocks (Fig. 2, Extended Data Fig. 8). The deforming foundation 129 is characterized by stiffer material and likely acts as a mechanical backstop behind the

accretionary wedge. A change in mechanical and frictional properties across this major
 regional boundary²⁷ is also suggested from the abrupt westward increase in local
 seismicity²² (Figs. 1 and 2).

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134 We find that distribution of pore fluid pressure (Fig. 3e) within the outer forearc is closely 135 tied to lithostratigraphy and that it correlates positively with the reflectivity intensity of our 136 RTM image (Fig. 2, Supplementary Fig. 1). Within the turbidite section, variations in pore fluid pressure ratio (λ^*) between unit 1 ($\lambda^* = 0.5 - 0.8$) and unit 2 ($\lambda^* = 0.4 \pm 0.1$) likely 137 reflect variations in clay content and grain size³⁰. In the vicinity of the subduction fault, 138 139 low seismic velocities within the Hikurangi Plateau cover sequence (unit 4) likely suggests 140 high pore fluid pressure and under-consolidation of subducted sediments^{9,10,31}, and we estimate $\lambda^* = 0.5 - 0.89$. In detail, these low-velocity zones are stratified, suggesting that 141 sedimentary layering produces permeability anisotropy that guides fluid flow laterally 142 143 along preferential strata, increasing the drainage path length and therefore affecting pore fluid pressure and effective stress^{32,33} (Fig. 4). Pronounced, ~100 m vertical variations in 144 145 elastic properties, ratio of P- and S- wave velocities and effective stress within units 3 and 4 (Fig. 3), may reflect focused flow and storage of pressurized fluids along higher 146 147 permeability sedimentary strata.

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Along the entire transect, sharp lateral transitions in P-wave velocity, elastic properties and estimated pressure regimes across the main thrust faults suggest a clear lateral partitioning of the margin into thrust blocks of distinct mechanical properties. Fault compartmentalization is particularly marked across the main thrust faults within the

153 Neogene wedge, which form low-velocity, low-rigidity, pressurized conduits of potentially 154 higher fault-permeability and likely play a key role in fluid drainage (Fig. 3h). Predicted 155 pore fluid pressure ratios within subducted strata are lower where footwall faults (group 156 C, Figs. 2, 3 and 4) connect with large thrust faults in the wedge that branch toward the 157 seabed (group A, Figs. 2, 3 and 4). We note that thrust faults terminating deeper beneath 158 the seabed (group B, Figs. 2, 3 and 4) appear less effective at relieving fluid-overpressure 159 at depth. From these observations, we identify two very compliant and highly 160 overpressured regions (regions I and III, Figs. 2, 3 and 4, Extended Data Fig. 6) 161 surrounding a stiffer portion of the subduction fault where elastic moduli increase by 162 ≥40%, and fluid overpressure reduces by up to 35% (region II, Figs. 2, 3 and 4, Extended 163 Data Fig. 6).

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165 Implications for fault stability and slow-slip

166 Modeled mechanisms for aseismic creep transients include mixed brittle-ductile 167 deformation^{34,35}, unstable aseismic slip on faults governed by rate-and-state friction 168 (RSF) with conditional frictional stability parameters, near-lithostatic pore-fluid pressures, or heterogeneous distributions of rate-weakening and rate-strengthening material^{2,4,5,36-} 169 170 ⁴⁰. Rate-state frictional stability of a material is described by the experimentally 171 determined parameters a and b: materials with b-a < 0 are velocity-strengthening, where 172 an increase in slip velocity causes an increase in friction; materials with b-a > 0 are 173 velocity-weakening, where increasing slip velocity leads to a drop in friction and 174 potentially unstable seismic slip. SSE conditions in RSF models are broadly inferred from 175 geophysical and numerical evidence^{2,36,37} or iterative parameter searches that select

176 parameter values to recreate SSE characteristics like recurrence interval and/or duration⁴¹. However, without data-constrained predictions of pore pressure and rigidity it 177 178 is difficult to assess whether these model-inferred properties are physically realistic 179 characterizations of subduction faults. Our FWI seismic images constrain the physical 180 properties of a shallow SSE source at higher resolution than has previously been 181 possible, thus providing the first opportunity to construct RSF models using high-182 resolution data-constrained physical parameters. These data show two prominent 183 differences between the shallow central HSM and previously modeled SSE conditions. 184 First, our data suggest that although pore-fluid pressure on the decollement is overpressured ($\lambda^* \sim 0.52 - 0.82$), it is not nearly as high as the near-lithostatic values 185 assumed in other SSE modeling studies (λ^* up to 0.999 in ref.³⁹, 0.998 in ref.⁴¹). However, 186 187 it is worth noting that from a methodological perspective, it remains virtually impossible to 188 reject the presence of highly pressurized material confined in thin layers below the 189 resolution dictated by the data (i.e. in layers <70 m thick, Methods). The λ^* values we 190 obtain for central HSM are comparable to those estimated for the offshore Nankai trough⁴², also a region of shallow slow slip⁴³. Second, elastic FWI shows that shear moduli 191 192 in the upper plate (<1 to 6–14 GPa) are significantly lower than the 25-50 GPa that have 193 typically been used in SSE models.

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Using the shallow elastic properties and effective normal stress constrained by FWI, we find that RSF numerical experiments with commonly used values of b-a (0.001 – 0.004) and d_c (2 – 10 mm) struggle to reproduce the slip style, durations and recurrence intervals of central Hikurangi SSEs ((b-a)/d_c ~ 0.1 – 2 m⁻¹, Fig. 5, Extended Data Fig. 9). These

199 models cannot fully reproduce the observed 5-year recurrence interval of central 200 Hikurangi SSEs, but models with reduced $(b-a)/d_c$ (0.075 – 0.0125 m⁻¹) approach the 201 observed recurrence intervals and magnitudes (Fig. 5b). For example, Figure 5 shows a 202 comparison of the transient aseismic slip modeled with parameters tuned to reproduce 203 SSEs in other studies (Fig. 5a, parameters from ref.⁴¹) and the predominantly seismic slip 204 modeled using shear moduli and effective normal stress from our FWI results along with 205 b-a (0.001) and d_c (8 mm) values at the lowest and highest (respectively) ends of the range of values used in previous studies³⁹⁻⁴¹ (Fig. 5b). In Fig 5b, slow-slip (upper panel) 206 207 occurs updip of a deeper seismogenic region (lower panel). Fault stability in RSF 208 continuum models is primarily determined by the effective fault stiffness ratio W/h*, where 209 W is the width of the velocity-weakening patch and h* is the critical cell size to generate 210 unstable slip events. This fault stiffness ratio depends on shear modulus, Poisson's ratio, 211 effective normal stress, RSF parameters (b-a and dc) and fault geometry. By implementing 212 the elastic properties from FWI at central HSM, we find that the fault instability parameter 213 W/h^* increases by up to two orders of magnitude relative to those of previous studies^{37,39,41}, thereby significantly limiting the range of the RSF parameter $(b-a)/d_c$ that 214 215 allows transient aseismic slip events ($(b-a/d_c) < 0.325 \text{ m}^{-1}$; b-a < ~0.00026 for d_c ~ 8 mm, 216 Fig. 5c). In particular, the higher effective normal stresses inferred by FWI tend to drive 217 the deeper portion of the fault towards seismic instability (Fig 5b, lower panel). The blue 218 envelope in Fig 5c shows the upper and lower bounds of W/h* stability relationships 219 associated with a range of FWI-derived near-fault shear moduli (6-14 GPa; Fig 3c; 220 Extended Data Figs. 6 and 9) and effective normal stresses (10-30 MPa; Fig 3f; Extended 221 Data Fig. 9). Although uncertainties in the FWI-derived mechanical properties are smaller than this range, this envelope shows that 30-100% variations in these parameters yield similarly limited ranges of (b-a)/d_c for frictional slow-slip, demonstrating that this result is largely insensitive to FWI uncertainties.

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226 One explanation for this departure is that b-a, the frictional property that determines 227 velocity-weakening or velocity-strengthening behavior, is nearly zero through most of the SSE patch. This conclusion is potentially unsatisfying⁴⁴, as it has been argued that SSE-228 229 hosting subduction zone faults worldwide would be unlikely to share such specific 230 frictional conditions. However, the near-velocity-neutral b-a values (b-a < ~ 0.001) 231 required for slow-slip in our Hikurangi RSF models are remarkably similar to 232 experimentally determined values (b-a ≤ 0.0015) for HSM sediments at plate tectonic 233 strain rates⁴⁵. Additionally, recent plate-rate laboratory experiments revealed near-234 velocity-neutral frictional slow-slip behavior in a wide variety of shallow fault gouges, 235 suggesting that strain rates consistent with steady plate motion may lead to lower 236 magnitude b-a than previous experiments have reported^{45,46} and such low values may in 237 fact be common. Alternatively, traditional RSF laws may not capture all of the mechanical processes responsible for shallow slow-slip⁴⁷. For example, recent models⁴⁷ show that 238 239 newly developed friction laws with slip-rate-dependent RSF parameters produce the wide 240 range of slow-slip behavior observed in nature over a broader range of mechanical 241 conditions than traditional RSF laws. Mechanically, these studies imply that subduction 242 fault rocks may weaken and slip unstably at sub-seismic slip rates, but rapidly 243 restrengthen and arrest unstable slip as slip rates approach earthquake velocities. The 244 physical mechanisms underlying rate-dependent frictional stability are not yet fully

resolved, but may involve increased dilation-hardening as slip accelerates to near-seismicrates.

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248 Additionally, heterogeneity of fault friction⁴ or effective normal stress^{39,48} may reduce the 249 effective size of the potentially unstable fault patch. Effective normal stress variations, 250 such as those observed here related to drainage of fluids by thrust fault branching from 251 the shallow subduction interface (Figs. 2, 3 and 4), have been shown to segment slowslip in RSF models by creating barriers to unstable slip propagation^{39,48}. Indeed, we find 252 253 that barriers to slow-slip propagation in our FWI-constrained RSF models localize in 254 regions with locally high upper plate shear modulus or sharp effective normal stress 255 gradients (Fig 3g; Extended Data Fig. 10). Homogeneously distributed slow-slip 256 segmentation arises spontaneously in our homogeneous property models (Extended Data Fig. 10), as has been reported in previous studies^{39,48}, but only models with 257 258 heterogeneous shear moduli and effective normal stress show persistent localized 259 segmentation over hundreds of slip cycles (Extended Data Fig. 10b,c). Abundant microseismicity downdip of the slow-slip region¹³ (Fig. 1) may reflect similar fault-slip 260 261 segmentation due to fault-controlled fluid compartmentalization, upper plate elastic and 262 hydrogeologic properties (Fig. 4), or meter to tens of meters-scale variations in rigidity or 263 fault geometry producing small, isolated unstable fault patches. Finally, it is important to 264 note that time-variable physical processes may cause fault stability to change over time, 265 as would be expected if SSEs occur in response to pore fluid overpressures gradually accumulating through the inter-event period^{49,50}. 266

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268 Advanced seismic imaging offers unique quantitative constraints on the physical 269 properties of the megathrust and overriding accretionary wedge over large areas, giving insight into the physical controls on shallow megathrust slip behaviors^{11,15-16}. Along the 270 271 central HSM, we find that the subduction fault is characterized by compliant, 272 overpressured and mechanically weak material with marked variations along dip (i.e. 273 regions with contrasting elastic and possibly frictional properties). We observe a strong 274 contrast in predicted pore pressure across thrust faults as well as across the subduction 275 thrust suggesting fault compartmentalization within the wedge and poorly-drained 276 conditions beneath the decollement. Thrust faults act as conduits for fluids, locally 277 reducing fluid pressure where these faults intersect the megathrust and creating meter-278 to-kilometer-scale heterogeneities in effective normal stress that may control fault slip 279 stability and/or segmentation. We show that RSF models using FWI-constrained physical 280 properties of the shallow central HSM are unable to reproduce slow slip behavior unless 281 the fault is nearly velocity-neutral (b-a < 0.001) or overpressured beyond the level 282 suggested by these data. This suggests that either shallow subduction zone fault rocks 283 are nearly velocity-neutral at plate tectonic loading rates or that a more complex process such as time-dependent fault pressurization⁴⁷ may be responsible for observed shallow 284 285 SSEs.

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502

503 Author contributions

A.F.A. conceived the study and analysed the seismic data. J.B. conducted the rate state friction modeling. A.F.A. and J.B. wrote the manuscript with contributions and edits from all other authors.

507

508 **Competing interests**

509 The authors declare no competing interests.

510

512 **Figure Captions:**

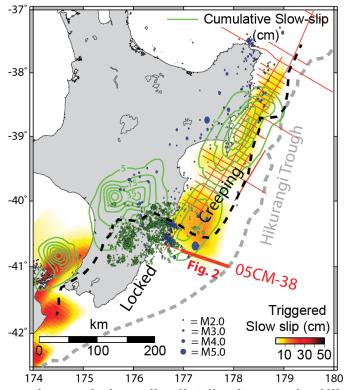
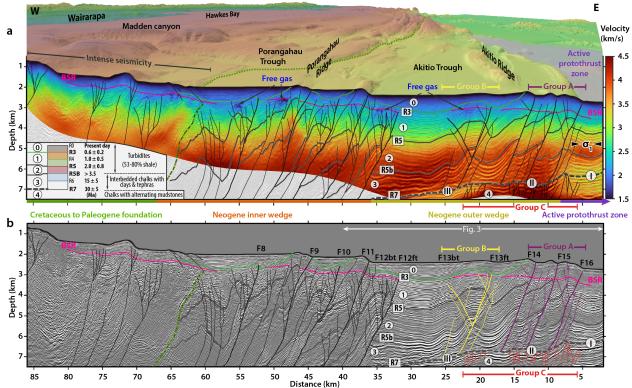
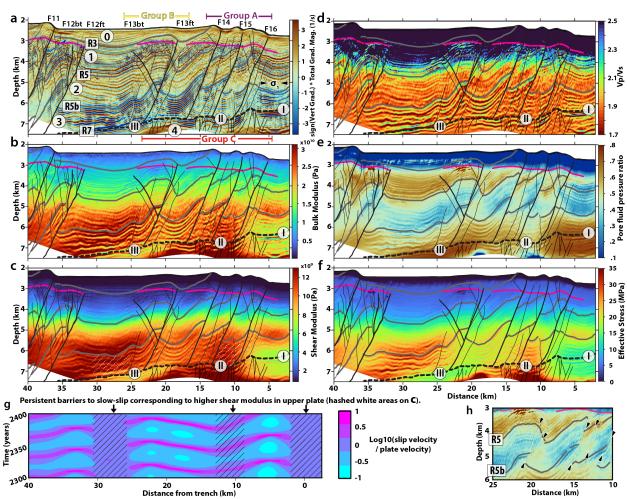




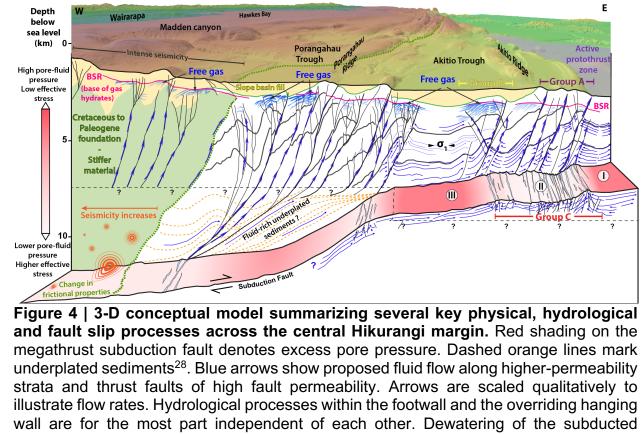
Figure 1 | Tectonic setting and slow slip distribution on the Hikurangi subduction 514 interface. Slow slip on the Hikurangi subduction interface following the M7.8 Kaikoura 515 516 earthquake²¹ (colours, see scale in cm) and cumulative slip in slow-slip events from 2002-2012 (green contours; from ref.¹³). Dashed gray line marks the location of the trench. 517 Dashed black line marks the geodetically determined along-strike transition from an 518 519 interseismically locked segment in the south to an aseismically creeping segment in the 520 north¹³ (i.e. interseismic coupling coefficient = 0.5). The blue circles are earthquakes from the GeoNet catalogue, and the green circles are the repeating earthquakes based on 521 waveform cross-correlation of 17,962 events from 2010-2017²². MCS profiles from the 522 523 05CM experiment are shown with red lines. Thick red line corresponds to Fig. 2. 524



525 526 Figure 2 | Seismic structure and geological interpretation across the central 527 Hikurangi margin. a, Composite P-wave velocity and reflectivity model along seismic 528 line 05CM-38 derived from elastic FWI and RTM at a maximum peak frequency of 18-20 Hz (Methods). Marker reflectors (solid green and gray lines) and units (numbered large 529 530 circles) identified along the seismic line are defined in the inset with their assigned 531 ages^{26,27}. Subducted unit 4 below reflector R7, correspond to unit MES and sequence "Y" 532 in refs.^{9,26}. The thick dashed gray line marks the megathrust subduction fault. Thick black 533 lines mark major thrust faults and associated frontal thrusts (ft) and back-thrusts 534 (bt)^{26,27}(labeled on **b**). Other minor faults are marked with thin black lines. Solid pink lines 535 mark bottom simulating reflections. Regions with contrasting elastic and frictional 536 properties along the subduction fault marked as I. II and III (Extended Data Fig. 6). The 537 dashed green line marks the limit between the Neogene accretionary wedge and the stiffer foundation of pre-subduction Cretaceous marine formations²⁶. **b**. Reflectivity image 538 539 derived from RTM (see Methods). Purple, yellow and red faults on b help characterize 540 fault groups A, B and C.



542 543 Figure 3 | Physical and mechanical characteristics of the subduction plate 544 boundary and outer Neogene accretionary wedge across the central Hikurangi 545 margin. a, Sign of vertical velocity gradient times the total velocity gradient magnitude (1/s); b, bulk modulus; c, shear modulus; and d, ratio of P-wave to S-wave velocities 546 obtained from elastic FWI (Methods). e, Estimated pore fluid pressure ratio and f, effective 547 548 stress estimated from P-wave velocities (Methods). Geological interpretations including 549 markers, reflectors and faults as in Fig. 2. g, Slip velocity with time and downdip distance 550 from the trench for a rate-and-state friction continuum model using shear moduli from FWI, constant effective normal stress of 13 MPa, and mildly velocity-weakening b-a = 551 552 0.001 (see Methods and Extended Data Fig. 12b). Spontaneous km-scale slow-slip 553 segmentation occurs at local shear modulus maxima (hashed areas on c (white) and g 554 (black)). h, Same as e but without the thrust faults. 555



sediments and fluid charging of the strata immediately above the subduction fault appear to be possible in places where faults within the footwall cut through the subduction fault (e.g. group C). As such, thrust fault depressurization of the shallow subduction fault likely influence the size of the regions with contrasting frictional properties along the subduction fault (i.e. regions I, II and III).

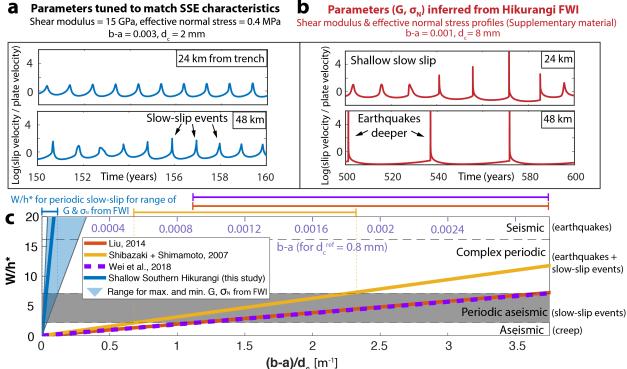


Figure 5 | Rate-state friction model results and stability phase diagram. Slip velocity 571 572 vs. time for fault patches 24 (upper panel) and 48 (lower panel) km downdip of the trench 573 from models with: a, mechanical and frictional parameters tuned to recreate SSE characteristics (after ref.⁴²) and, **b.** mechanical properties taken from seismic FWI results 574 575 from the shallow central Hikurangi margin. The seismically constrained model includes some shallow slow slip (upper panel) but the deeper portion (lower panel) predominantly 576 577 slips in earthquakes despite a mildly velocity-weakening value of b-a = 0.001. Higher 578 effective normal stress from FWI drives the deeper portions of the modeled fault towards seismic instability, and cannot fully reproduce the recurrence intervals and durations of 579 580 observed central Hikurangi SSEs, although models with lower (b-a)/dc approach SSE 581 behavior (**b**, upper panel). **c**, Representative stability regimes for RSF models from 582 various studies. Blue shaded area shows range of stability trajectories based on our 583 seismic inversions (10 MPa < effective stress (σ_N) < 30 MPa; 6 GPa < shear modulus (*G*) 584 < 14 GPa). Horizontal colored bars show ranges of RSF parameters predicted to allow 585 SSE-type periodic aseismic slip, highlighting the limited range of RSF parameters 586 expected to promote episodic slow-slip for the mechanical conditions inferred from 587 shallow central Hikurangi seismic FWI. 588

590 Methods:

591

592 Seismic imaging strategy.

593

Seismic velocity of the subsurface can be separated into two components: (1) a lowfrequency component, which affects the travel time, and (2) a high-frequency component which mainly affects the amplitude in the observed seismic signal⁵¹. A local optimization based full waveform inversion (FWI) can derive some of the high-frequency components but is dependent on the initial model to provide the low-frequency information⁵². Therefore, a kinematically sound initial model is necessary for FWI to converge to a meaningful solution.

601

To derive a kinematically correct starting model for FWI, we initially performed a linearized traveltime tomographic inversion of a downward extrapolated, 12-km-long offset, multichannel seismic profile following the methodology described in refs.^{18-20,53-56}.

605

606 **Downward extrapolation.**

607

Downward extrapolation^{57,58} is a technique that can be used to transform seismic field data acquired on the sea surface to a new datum at or near the seafloor, therefore simulating a different acquisition geometry. The resulting dataset is a synthetic oceanbottom experiment (SOBE¹⁸). A key advantage of downward extrapolation is that it moves the refracted energy turning just below the seafloor ahead of the seafloor reflection. In

this study, we used the Kirchhoff integral formulation of the downward extrapolation
 operator⁵⁷⁻⁵⁹ which appropriately accommodates a laterally varying extrapolation datum
 and non-uniform acquisition geometry.

616

617 Processing of the field data was accomplished during the downward extrapolation stage¹⁹. To minimize the bubble pulse effect, we first applied an optimal predictive 618 619 deconvolution filter to the observed field data. Second, we applied trace balancing to 620 preserve the continuity of the seismic wavefiled along the streamer. Third, we applied a 621 sixth-order Butterworth band-pass filter with corner frequencies of 3 - 30 Hz to the data. We then convolved the input signal with $H(t)/\sqrt{t}$ (with H the Heaviside step function and t 622 623 the time) to help better simulate a 2-D experiment and boost low frequencies with respect 624 to high frequencies. The downward extrapolated shot gathers had sources moved to the 625 nearest node of a 12.5 m grid, and 960 evenly spaced receivers starting 12.5 m behind 626 the source and extending to 12 km. The seismic energy was moved to a simulated datum 627 75 m above the seafloor.

628

629 **Traveltime tomography.**

630

Traveltimes of downward extrapolated first arrival P-wave refractions as well as reflections from the plate interface reflector were picked along 05CM-38 seismic line, for every fifth SOBE shot gather, representing a total of 327,632 picked traveltimes. The starting P-wave velocity model for tomographic inversion was a smooth version of the velocity structure from ref.²⁷.

We followed the inversion strategy of refs.^{18,54,56}. Forward calculation of travel-time arrivals was done using a shortest path method⁶⁰. The inversion sought to obtain the smoothest velocity model that fits the data within the assigned pick uncertainties. The goodness of the fit between observed (i.e. picked, T_{obs}) and synthetically calculated (T_{syn}) traveltimes was measured by the χ^2 value:

642

$$\chi^{2} = \frac{1}{N} \sum_{i=1}^{N} \frac{(T_{obs,i} - T_{syn,i})^{2}}{\sigma_{err,i}},$$
(1)

643

644 Where σ_{err} is a pick uncertainty (here, 12 ms) and N is the total number of picks. Models 645 were iteratively updated by minimizing a least squares cost function that penalizes a 646 combination of data misfit and model regularization. Our regularization operator penalized 647 the first and second order derivatives (gradient and curvature) of the velocity structure. 648 Horizontal derivatives were given a weight 4 times larger than vertical derivatives owing 649 to the fact that the final seismic velocity structure is expected to be rougher in the vertical 650 direction. Our final model fit the picked arrivals with a ~8 ms root-mean-square traveltime 651 misfit (Supplementary Video 1). 652

653 Elastic Full Waveform Inversion (FWI).

- 655 **Theoretical background**
- 656

The goal of FWI is to minimize the data residuals $\delta \mathbf{u} = \mathbf{u}^{\text{mod}} - \mathbf{u}^{\text{obs}}$ between the modelled data \mathbf{u}^{mod} and the observed data \mathbf{u}^{obs} to estimate the distribution of the material parameters **m** in the subsurface. The misfit is measured by the objective function^{61,62}:

$$S = \frac{1}{2} \delta \mathbf{u}^T \delta \mathbf{u}$$
(2)

The term $\delta \mathbf{u}^{T} \delta \mathbf{u}$ represents the residual energy, i.e. the seismic energy not explained by the actual model **m**. The objective function is minimized by updating the model parameters **m** at each iteration n using a steepest-descent gradient method:

664

$$\boldsymbol{m}_{n+1} = \boldsymbol{m}_n - \alpha_n \left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_n,\tag{3}$$

665

where $(\partial S/\partial \mathbf{m})_n$ is the gradient direction of the objective function with respect to the material parameters and α_n the step length. According to refs.^{14,61,62,63} the gradients for each elastic parameter can be expressed in time domain by a zero-lag correlation of displacement wavefields.

670

$$\frac{\partial S}{\partial \lambda} = -\sum_{shots} \int dt \left(\frac{\partial \overrightarrow{u_x}}{\partial x} + \frac{\partial \overrightarrow{u_z}}{\partial z} \right) \left(\frac{\partial \overleftarrow{u_x}}{\partial x} + \frac{\partial \overleftarrow{u_z}}{\partial z} \right)$$
(4)
$$\frac{\partial S}{\partial \mu} = -\sum_{shots} \int dt \left[2 \left(\frac{\partial \overrightarrow{u_x}}{\partial x} \frac{\partial \overleftarrow{u_x}}{\partial x} + \frac{\partial \overrightarrow{u_z}}{\partial z} \frac{\partial \overleftarrow{u_z}}{\partial z} \right) + \left(\frac{\partial \overrightarrow{u_x}}{\partial z} + \frac{\partial \overrightarrow{u_z}}{\partial x} \right) \left(\frac{\partial \overleftarrow{u_x}}{\partial z} + \frac{\partial \overleftarrow{u_z}}{\partial x} \right) \right]$$
$$\frac{\partial S}{\partial \rho} = -\sum_{shots} \int dt \left(\frac{\partial^2 \overrightarrow{u_x}}{\partial t^2} \overleftarrow{u_x} + \frac{\partial^2 \overrightarrow{u_z}}{\partial t^2} \overleftarrow{u_z} \right)$$

Where \rightarrow denotes an element of the forward modelled wavefield and \leftarrow denotes an element of the backward propagated data residuals wavefield, generated by propagating the residual data (known as the adjoint wavefield) from the receiver positions backwards in time in the elastic medium. The forward problem and backpropagation of the adjoint wavefield is solved by using a 10th order in space, 2nd order in time, 2-D time domain stress-velocity finite-difference (FD) code⁶⁴. As such, the displacements in equation (4) can be reformulated in terms of stresses and particle velocities⁶¹:

679

$$\begin{aligned} \frac{\partial S}{\partial \lambda} &= -\sum_{shots} \int dt \left[\frac{(\sigma_{xx} + \sigma_{zz})(\Sigma_{xx} + \Sigma_{zz})}{4(\lambda + \mu)^2} \right] \end{aligned} \tag{5} \\ \frac{\partial S}{\partial \mu} &= -\sum_{shots} \int dt \left[\frac{\sigma_{xz} \Sigma_{xz}}{\mu^2} \right. \\ &+ \frac{1}{4} \left(\frac{(\sigma_{xx} + \sigma_{zz})(\Sigma_{xx} + \Sigma_{zz})}{(\lambda + \mu)^2} + \frac{(\sigma_{xx} - \sigma_{zz})(\Sigma_{xx} - \Sigma_{zz})}{\mu^2} \right) \right] \\ \frac{\partial S}{\partial \rho} &= -\sum_{shots} \int dt \left[v_x \omega_x + v_z \omega_z \right] \end{aligned}$$

680

where σ_{ij} and Σ_{ij} are the stresses and v_i and ω_i are the particle velocities of the forward and back propagated wavefields, respectively. The gradients in terms of other material parameters *m*' can then be calculated by simple vector transformation⁶².

684

$$\frac{\partial S(\boldsymbol{m})}{\partial \boldsymbol{m}'} = \frac{\partial S(\boldsymbol{m})}{\partial \boldsymbol{m}} \frac{\partial \boldsymbol{m}}{\partial \boldsymbol{m}'}$$
(6)

685

686 Using the relationships between P-wave velocity Vp, S-wave velocity Vs, the Lamé

parameters λ , μ and density ρ, the gradient for V_p , V_s and ρ_{model} can be written as:

$$\frac{\partial S}{\partial V_p} = 2\rho V_p \left(\frac{\partial S}{\partial \lambda}\right) \tag{7}$$

$$\frac{\partial S}{\partial V_s} = -4\rho V_s \left(\frac{\partial S}{\partial \lambda}\right) + 2\rho V_s \left(\frac{\partial S}{\partial \mu}\right)$$

$$\frac{\partial S}{\partial \rho_{model}} = \left(V_p^2 - 2V_s^2\right) \left(\frac{\partial S}{\partial \lambda}\right) + V_s^2 \left(\frac{\partial S}{\partial \mu}\right) + \left(\frac{\partial S}{\partial \rho}\right)$$

To increase the convergence speed an appropriate preconditioning operator P is applied to the gradient $\partial S/\partial \mathbf{m}$

690

$$\left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n}^{p} = P_{n} \left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n}$$
(8)

691

692 Our preconditioning operator is an approximation to the spatial form of the diagonal of the 693 inverse Hessian (see ref.⁶⁵), which removes the geometrical spreading from the forward 694 and back propagated wavefields and therefore rebalances the contributions of deep and 695 shallow scatters in the gradients.

696

697 To further increase the convergence speed of the objective function, the conjugate 698 gradient direction for iteration steps $n \ge 2$ is calculated

699

$$\left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n}^{c} = \left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n}^{p} + \beta \left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n-1}^{c} \text{, with } \left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{1}^{c} = \left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{1}^{p} \tag{9}$$

$$\beta^{PR} = \frac{\left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n}^{P} \cdot \left[\left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n}^{P} - \left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n-1}^{P}\right]}{\left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n-1}^{P} \cdot \left(\frac{\partial S}{\partial \boldsymbol{m}}\right)_{n-1}^{P}}$$
(10)

703

by Polak-Ribiére is used⁶⁶, and $\beta = max\{0, \beta^{PR}\}$ provides a direction reset automatically. We normalize the material parameters and the gradients before the step length calculation. The optimum step length α_n in equation (3) is estimated by a line search algorithm⁶⁷.

708

It is worth noting, that using a conventional streamer acquisition geometry, refs.^{63,68} demonstrated that with this implementation of elastic FWI, the P-wave velocity, S-wave velocity and density models of the subsurface can be successfully reconstructed. Indeed, medium wavelength features of S-wave velocity are recoverable from the wide-angle Pwave amplitude-versus-offset response, exploiting the residual P-wavefield (reflected and transmitted), particularly around the critical angle.

715

716 **Practical considerations**

717

The P-wave velocity model obtained from the tomographic inversion step was used to constrain the starting models for elastic full waveform inversion (FWI, see refs.^{19,20,53,55,61}). We estimated a starting S-wave velocity model using the empirical relationships found in ref.⁶⁹. We followed a multistage FWI strategy alternating between model updates, where

722 we inverted simultaneously for P- and S-wave velocities, and source updates. We did not 723 invert for density, which was updated using empirical relationships with P-wave 724 velocities^{70,71}. With our elastic FWI inversion scheme we targeted arrivals in downward 725 extrapolated data whose spectra exhibit only limited offset dependence (Extended Data 726 Fig. 5). As such, we assumed for our elastic FWI that the principal attenuation effects can 727 be incorporated into an optimal source wavelet that is updated as part of the inversion 728 process. In a first stage, we ran 60 iterations of elastic FWI, where we targeted only the 729 wide-angle seismic energy in downward extrapolated data ahead of the seafloor reflection 730 and above the first seafloor multiple (Extended Data Figs. 1b, 2b and 3; Supplementary 731 Video 2). For this first stage, modelling was done on a 12.5 m grid and we followed a 732 sequential frequency inversion strategy from low to high frequencies to reconstruct the 733 models. A Butterworth bandpass filter with 6 poles and corner frequencies of 3-8 Hz, 3-734 10 Hz, 3-12 Hz and 3-15 Hz was used for iterations 0-8, 8-16, 16-24 and 24-60, 735 respectively. In a second stage, an additional 30 iterations of elastic FWI was performed 736 on a 6.25 m modelling grid and we targeted the reflected energy below the seafloor 737 reflection and above the first seafloor multiple (Extended Data Figs. 1c, 2c and 3; 738 Supplementary Video 3). For those 30 iterations, a Butterworth bandpass filter with 6 739 poles and corner frequencies of 3-20 Hz, 3-25Hz and finally 3-30 Hz was used. Typically, sources updates⁶² were run after each set of ~8–10 model updates. The final dominant 740 741 frequency of the FWI is ~18-20 Hz, for which a maximum resolution of a guarter dominant 742 wavelength corresponding to ~30 m at 2000 m/s and ~70 m at 5000 m/s.

743

744 Elastic Reverse Time Migration (RTM).

Reverse-Time Migration (RTM^{19,55,72,73}) is a prestack two-way wave-equation migration technique for accurate imaging in and below areas with large structural and velocity complexities. RTM offers the best accuracy and image fidelity among all seismic imaging methods, it has no dip limitation and it handles extreme lateral velocity variations using all possible arrivals.

751

752 Our RTM algorithm implements a modelling scheme similar to the one used for the FWI, 753 with two key differences. First, the "adjoint" back-propagated wavefield correspond to the 754 observed data instead of the data residual. Second, the zero-lag crosscorrelation 755 between the forward propagated source-wavefield and back-propagated receiver 756 wavefield is implemented using a pointing-vector imaging condition with illumination compensation and obliquity-correction⁷⁴. The imaging condition optimizes the match 757 758 between the two wavefields in order to generate the output reflectivity image. In other 759 words, the imaging condition dictates the guality and fidelity of the final RTM image.

760

761 **Porosity, pore-fluid pressure and effective stress prediction.**

762

We follow an approach similar to that of refs.^{10,31,75,76} to derive the state of stress within
the accretionary wedge from seismic P-wave velocities obtained from FWI.

765

To proceed, we first estimate a porosity-depth profile at a reference site seaward of the deformation front using Athy's relationship⁷⁷:

$$\varphi = \varphi_0 \exp(-\beta z),\tag{11}$$

769

where φ_0 is the initial porosity of the material at the seafloor, β is the rock compaction coefficient (i.e. 1/compaction length scale) and *z* is depth (m). The best fitting parameters for the Hikurangi margin are $\varphi_0 = 0.525$ and $\beta = 1/3000 = 0.000333$ (similar to ref.⁷⁶, and validated by recent drilling constraints⁷⁸).

774

With these parameters, we use equation (5) in ref.⁷⁵ to calculate the vertical effective stress (σ_z), defined as:

777

$$\sigma_z' = \frac{\left(\rho_s - \rho_f\right)g}{\beta} [(\ln\varphi_0 - \varphi_0) - (\ln\varphi - \varphi)],\tag{12}$$

778

where *g* is the gravitational acceleration (m.s⁻²), and ρ_s and ρ_f are the solid grain and fluid densities (kg.m⁻³), respectively. The best fitting parameters for the Hikurangi margin are $\rho_s = 2740 \ kg. m^{-3}$ and $\rho_f = 1030 \ kg. m^{-3}$ (from ref.⁷⁶). At the reference site (i.e. seaward of the deformation front), the sediments are under normal consolidation conditions ($\sigma'_1 > \sigma'_2 = \sigma'_3$, $\sigma'_z = \sigma'_1$, where σ'_1 , σ'_2 , and σ'_3 are the maximum, intermediate, and minimum principal effective stress, respectively). We then calculate mean effective stress (σ'_m) as:

$$\sigma'_{m} = \frac{\sigma'_{1} + \sigma'_{2} + \sigma'_{3}}{3} = \frac{(1+2R)}{3}\sigma'_{z}, \quad R = \frac{\sigma'_{3}}{\sigma'_{1}}$$
(13)

where R is an experimentally determined ratio between minimum and maximum principal effective stress (R = 0.6, from ref.⁷⁶).

790

Within the accretionary prism, a porosity-depth model is derived from FWI P-wave velocities using equation (9) in ref.⁷⁹, with high-consolidation state and a shale fraction of 0.6 validated from drilling constraints⁸⁰. We then convert the porosity to mean effective stress along the entire transect using the relationship derived at the reference site. We assume a forearc coefficient of friction of μ = 0.6; horizontal maximum principal effective stress; and hence the mean effective stress is a factor of 1.6 times the vertical effective stress within the accretionary prism ($\sigma'_{z,wedge}$):

798

$$\sigma'_{z,wedge} = \frac{\sigma'_m}{1.6}.$$
(14)

799

800 From there we derive pore fluid pressure (Pf), by substracting vertical effective stress 801 $(\sigma'_{z,wedge})$ from the lithostatic pressure (PI):

802

$$P_f = P_l - \sigma'_{z,wedge}.$$
 (15)

Finally, the Hubbert-Rubey pore fluid pressure ratio (λ^*) is calculated as the ratio of fluid pressure (Pf) minus hydrostatic pressure (Ph) to lithostatic pressure (Pl) minus hydrostatic pressure:

807

$$\lambda^* = (P_f - P_h) / (P_l - P_h).$$
(16)

808

A λ^* of zero means that there is no overpressure (i.e. hydrostatic), and is justified when there is efficient hydrogeological connection through the pore network to the ocean. On the other hand, a λ^* of 1 corresponds to full overpressure (i.e. lithostatic), and is justified in the presence of a perfect seal without any hydrofracturation.

813

814 **Rate-state frictional framework for SSEs**

815

816 Many slow-slip behaviors have been successfully modeled by numerical simulations of planar and non-planar faults in a rate-state friction (RSF) framework^{2,4,36-40,81,82}. RSF 817 818 constitutive laws describe the time-dependent evolution of friction according to the current 819 slip rate V and the history-dependent state variable θ (e.g., refs.^{83,84}). Different RSF laws 820 exist to explain different experimental and observational characteristics of seismic and aseismic slip. In this study we use the single state-variable 'ageing' law^{83,84,85} which has 821 been used in previous slow-slip modeling studies^{2,4,36,39,40,81} and is considered most 822 823 appropriate for slip that does not reach large earthquake velocities. The ageing law gives 824 the fault friction μ as:

825

$$\mu = \mu_0 + a \ln \frac{V}{V_0} + b \ln \frac{V_0 \theta}{d_C}$$
(17)

where μ_0 is the steady-state coefficient of friction at reference velocity V_0 , a is the directeffect RSF parameter, b is the evolution-effect RSF parameter, and d_c is the characteristic slip length. The state variable has units of time and represents the time-dependent contact evolution processes. The aging-law state variable evolves according to:

831

$$\dot{\theta} = 1 - \frac{V\theta}{d_c} \tag{18}$$

832

The RSF parameters a and b are experimentally determined material properties which control the frictional stability of the fault. For (b-a) > 0, the fault patch is velocity-weakening and potentially seismogenic, whereby an increase in velocity yields a decrease in friction. In contrast, for (b-a) < 0 the fault patch is velocity-strengthening and stable or conditionally stable, whereby an increase in slip velocity is countered by an increase in friction, which arrests unstable slip propagation.

839

840 Numerical Methods

841

We model a planar fault with RSF under plane-strain conditions loaded by an overriding elastic plate of thickness H and shear modulus G moving at plate velocity V. Over each timestep dt, elastic stresses are balanced by fault strength using the typical RSF model assumption that stress matches strength. We solve for the slip velocity that satisfies this

846 relationship, and this velocity is prescribed over the period dt in order to calculate elastic 847 strains at the beginning of the subsequent timestep. Each timestep is adaptively scaled 848 to capture both millisecond-scale seismic slip behavior as well as multi-year inter-event deformation as in ref.⁸⁶. We calculate quasistatic stress balances using the Fast 849 850 Lagrangian Analysis of Continua (FLAC) algorithm⁸⁷, which solves the wave-equation 851 while critically damping the inertial component of motion using inertial mass-scaling. We 852 also implement the standard radiation damping approximation to suppress seismic radiation associated with seismic slip (e.g. refs.^{2,86}). Full details of the numerical method 853 854 used in our models can be found in ref.²³.

855

856 Central Hikurangi Model Setup

857

858 The central Hikurangi SSE patch extends from at least 12 - 6 km depth beneath the East 859 coast of the North Island of New Zealand^{13,22}, although the updip limit of SSE slip is not 860 well-constrained due to a lack of seafloor geodetic data in this region. Ocean-bottom 861 pressure gauge data from the September-October 2014 SSE recorded slip near the 862 trench in the northern Hikurangi margin, suggesting that slip in the southern patch may 863 also propagate further updip towards the trench; however, similar experiments have not 864 yet been undertaken in the central Hikurangi margin. Here, we model the trench-865 perpendicular upper 80 km of the decollement, which extends from the trench to ~13 km 866 depth (Extended Data Fig. 9).

867

868 The model assumes plane-strain, but the two-dimensional geometry of the decollement 869 and overriding plate are used to calculate the overburden and thickness of the overriding 870 elastic plate. Effective normal stress on the fault is the difference between the weight of 871 the overlying rock column and the pore-fluid pressure at each point (Extended Data Fig. 872 9), as inferred from seismic FWI. Each fault patch is loaded at the trench-perpendicular 873 convergence rate of 4 cm/yr by an overriding thin elastic plate with thickness H equal to 874 the depth from the seafloor to the decollement, and shear modulus G equal to the average 875 of the seismologically inferred shear modulus of the upper plate directly above the patch 876 (Extended Data Fig. 9). Fault shear modulus G is equal to the seismologically inferred 877 shear modulus along the decollement as drawn in Figure 2 and Extended Data Figs. 6, 7 878 and 9.

879

Laboratory rock mechanical experiments show that b-a is dependent upon temperature, composition, fluid content, slip velocity, confining pressure and effective normal stress. However, in our model the values of b-a and d_c are the least well-constrained physical parameters. Therefore, to minimize the effect of b-a and d_c heterogeneity on the modeled slow-slip events, b-a is set constant and equal to 0.001 between 6 and 12 km depth, increasing linearly to -0.003 updip and downdip of this region; d_c is constant for all portions of the fault and is set to 2-10 mm as in previous studies (e.g., refs.^{41,48}).

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891 **Data availability.**

All multichannel seismic field data, seismic navigation and acquisition logs from the 05CM experiment are archived with the New Zealand government and freely available at the following address (<u>https://data.nzpam.govt.nz/GOLD/system/</u>). Our final two-dimensional elastic full waveform inversion velocity models⁸⁹ (doi: <u>10.26022/IEDA/330190</u>) can be found on the Marine Geoscience Data System.

897

898 **Code availability.**

The seismic processing and imaging codes associated with this paper are maintained by A.F.A. at the Institute for Geophysics at the University of Texas at Austin (<u>aarnulf@ig.utexas.edu</u>). Some components are available on request.

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