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Five statistical models for Likert-type experimental data on acceptability judgments

Anna Endresen & Laura A. Janda

20.07.2015

CLEAR

Cognitive Linguistics: Empirical Approaches to Russian



A joint project



Anna Endresen
UiT



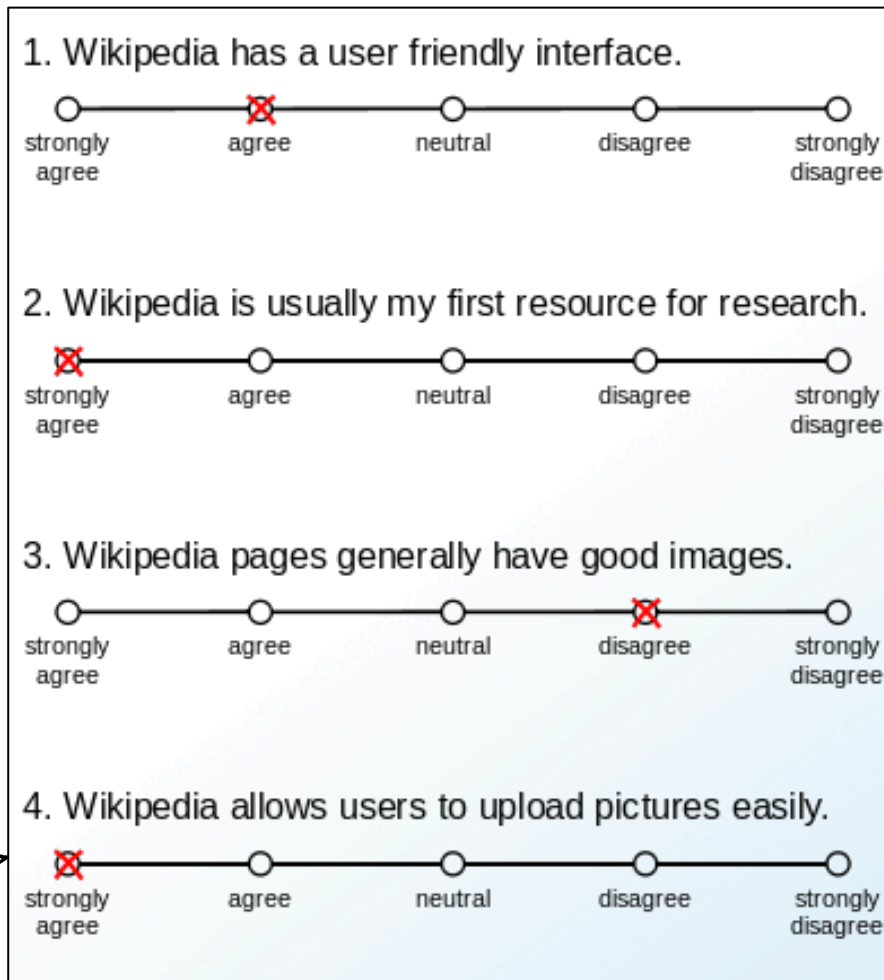
Laura A. Janda
UiT

Structure of the talk

- **Intro**
 - What is experimental Likert-type scale data?
 - What statistical tests are appropriate: Parametric vs. Non-parametric
- **Our study: marginal change-of-state verbs in Russian**
 - Experimental design and our research questions
 - 5 statistical models for collected data
 - ANOVA
 - Ordinal logistic regression
 - Regression mixed-effects model
 - Regression tree & Random forests
 - Classification tree & Random forests
- **Conclusions**
 - Are the outcomes of these models comparable?
 - Which model is the most appropriate, informative, user-friendly?

Levels of agreement / disagreement

Likert scale



Rensis Likert
(1903-1981)

“A Technique for the Measurement of Attitudes”. 1932. PhD dissertation. Columbia University.



A method of ascribing quantitative values to qualitative data in order to make it amenable to statistical analysis.

Likert-type / Likert-like scales (cf. Lavrakas 2008: 429)






How important are surveys to your startup's success?

Not at all Important	Slightly Important	Moderately Important	Very Important	Extremely Important
<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

- How often do you feel in control of your life?
 - (1) Never
 - (2) Seldom
 - (3) Often
 - (4) Almost always



How satisfied are you with our services?

 <input type="radio"/> Very Unsatisfied	 <input type="radio"/> Unsatisfied	 <input type="radio"/> Neutral	 <input type="radio"/> Satisfied	 <input checked="" type="radio"/> Very Satisfied
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Importance

Frequency

Quality

Satisfaction

Data measurement: 4 types

- **Nominal scales**

- Categorize: yes/no, genders, colors, races
- Convey no quantitative information and no ordering of items



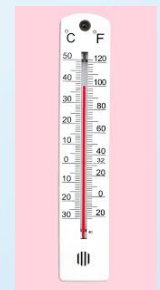
- **Ordinal scales**

- Order or rank things: movie ranking



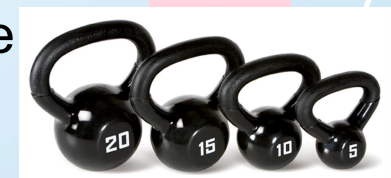
- **Interval scales**

- Order + equal intervals: centimeters, degrees Celsius



- **Ratio scales**

- Interpretable and natural zero: money, weight, age



Data measurement: 4 types

- **Nominal scales**
 - Categorize: yes/no,
 - Convey no quantitative information
- **Ordinal scales**
 - Order or rank things
- **Interval scales**
 - Order + equal intervals
- **Ratio scales**
 - Interpretable and non-zero

For nominal and ordinal scales only **non-parametric statistical tests** are appropriate (e.g. chi-squared test).

Interval and ratio scales **allow arithmetic calculations** that compare their sizes, averages, and variation.

Parametric statistical tests are appropriate (e.g. ANOVA)



“It is common to treat Likert scales as **interval** level data, it is more conservative to view such data as **ordinal**.”
(Lavrakas 2008)

There is a controversy about **Likert scale data**

Ordinal and ordinal scales only **non-parametric statistical tests** are appropriate (e.g. chi-squared test).

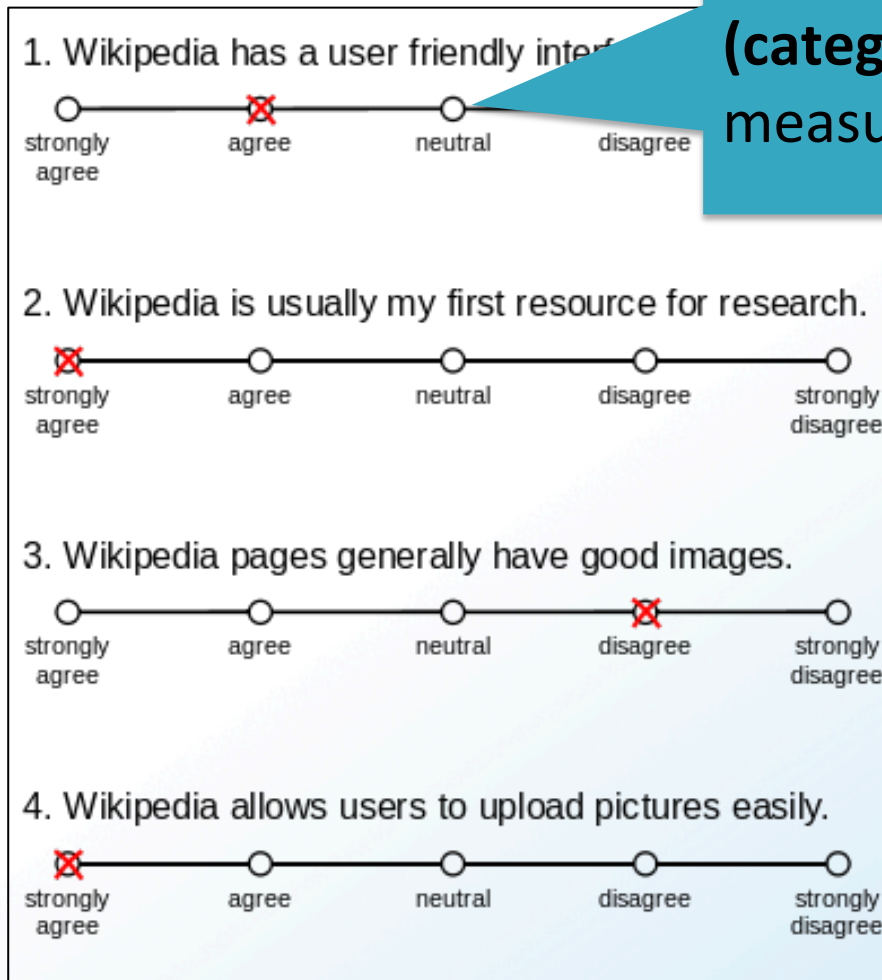
- **Ordinal scales**
 - Order or rank things
- **Interval scales**
 - Order + equal intervals
- **Ratio scales**
 - Interpretable and measurable

Interval and ratio scales **allow arithmetic calculations** that compare their sizes, averages, and variation.

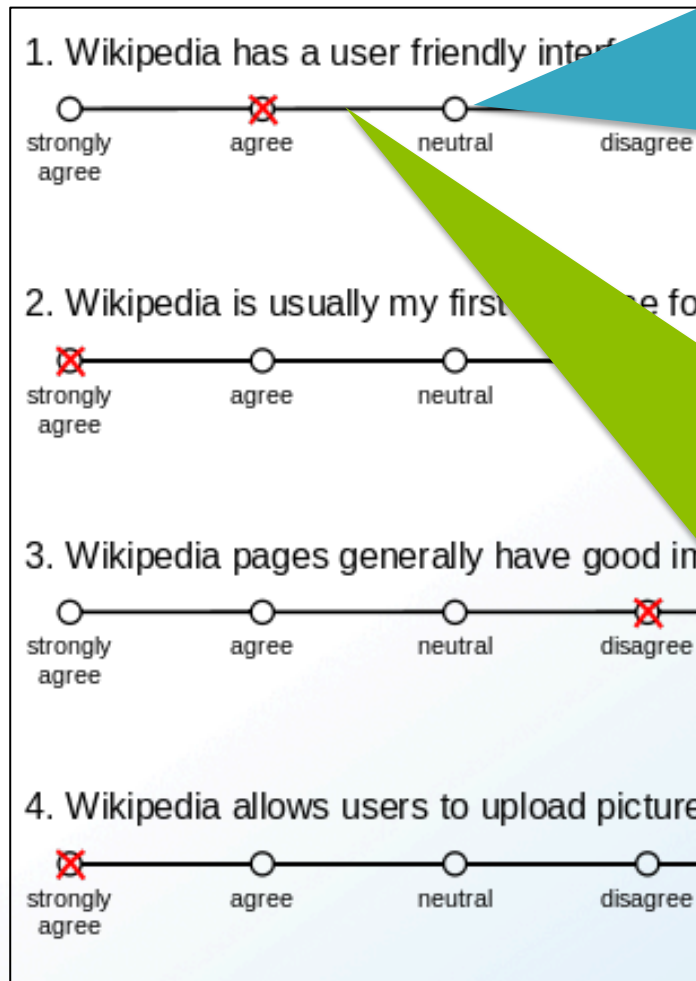
Parametric statistical tests are appropriate (e.g. ANOVA)

Likert scale

The response format (each item is a descriptive statement) is at the **ordinal (categorical)** level of measurement.



Likert scale



The response format (each item is a descriptive statement) is at the **ordinal (categorical)** level of measurement.

The key assumption is that the distances between every two adjacent points are of equal magnitude and justify the **interval** level of measurement.

(reinforced graphically or with a set of numbers 1,2,3,4...)

Objections

- Cohen et al (2000: 317) and Jamieson (2004) object against assuming an interval scale for Likert-type categories. >>
- They find it illegitimate to use parametric statistics for data obtained via Likert scales.

Likert scales: how to (ab)use them

Susan Jamieson

Dipping my toe into the water of educational research, I have recently used Likert-type rating scales to measure student views on various educational interventions. Likert scales are commonly used to measure attitude, providing 'a range of responses to a given question or statement'.¹ Typically, there are 5 categories of response, from (for example) 1 = strongly disagree to 5 = strongly agree, although there are arguments in favour of scales with 7 or with an even number of response categories.¹

between 'strongly disagree' and 'disagree' is equivalent to the intensity of feeling between consecutive categories on the Likert scale. The legitimacy of assuming an interval scale for Likert-type categories is an important issue, because the appropriate descriptive and inferential statistics differ for ordinal and interval scales^{1,5} and if the wrong technique is used, the researcher increases the chance of concluding the wrong conclusion about the significance (or otherwise) of research.

The response categories in Likert scales have a rank order, but the intervals between values cannot be presumed equal

The mean (and standard deviation) are inappropriate for ordinal data

There is more to it: Knapp (1990: 121)

- **The distinction between ordinal and interval scales of data measurement is often a challenge** when one has to categorize a specific data set.
- A particular scale can be “**ordinal, less than ordinal, or more than ordinal**”, and that there are **no agreed-upon rules** for determining this.
- The ordinal / interval scale-and-statistics controversy is a **long-standing and continuing debate** in the literature. For the history of conflicting views see Gardner 1975.

Possible solution: a different format

Please circle the number that represents how you feel about the computer software you have been using

I am satisfied with it

Strongly Disagree —1—2—3—4—5—6—7— Strongly Agree

It is simple to use

Strongly Disagree —1—2—3—4—5—6—7— Strongly Agree

It is fun to use

Strongly Disagree —1—2—3—4—5—6—7— Strongly Agree

It does everything I would expect it to do

Strongly Disagree —1—2—3—4—5—6—7— Strongly Agree

I don't notice any inconsistencies as I use it

Strongly Disagree —1—2—3—4—5—6—7— Strongly Agree

It is very user friendly

Strongly Disagree —1—2—3—4—5—6—7— Strongly Agree

Likert-type scales in linguistics: Elicitation of acceptability judgments

- In linguistic experiments, Likert-type scales are used as a technique for elicitation of acceptability judgments.
- The ambition is to capture the gradient nature of linguistic intuition.
- The subjects are presented with a ranked set of points (usually 5 or 7) where at least the top and the bottom ends are descriptively categorized (cf. Dąbrowska 2010; Bermel and Knittle 2012):

1

2

3

4

5

6

7

Unacceptable

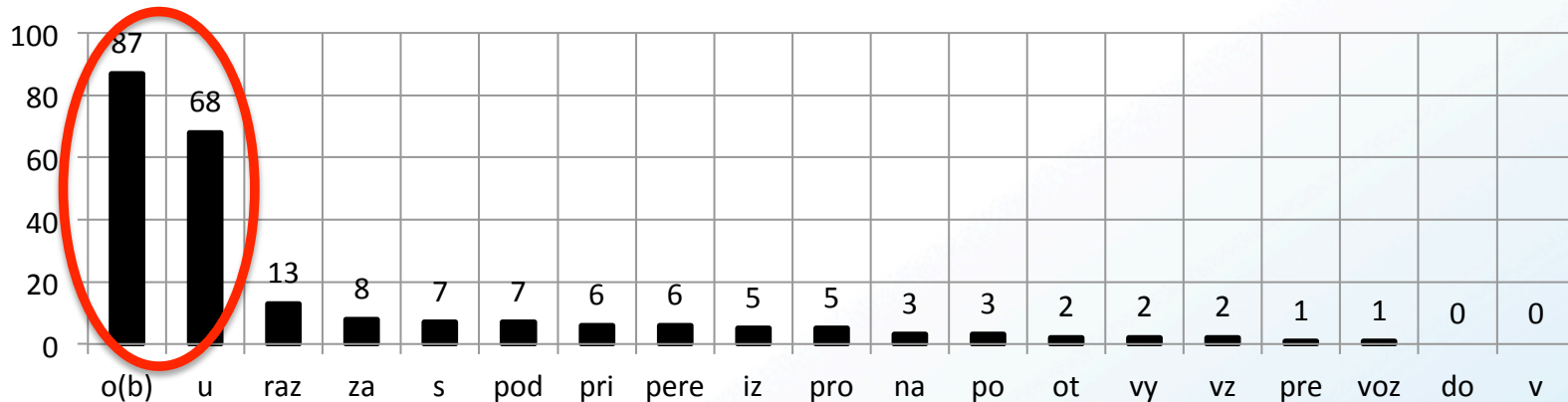
Perfectly normal

Discussion goes on in linguistic studies

- Dąbrowska (2010: 8) points out that a number of studies (Jaccard & Wan 1996; Labovits 1967, Kim 1975) have argued that “parametric tests are quite robust, so that **violations of the intervalness assumption have relatively little impact on the results of the test**”.
- Dąbrowska 2010 states that “the use of parametric tests with data obtained using Likert scales has now become standard” (cf. similar observations in Blaikie 2003, Pell 2005).
- Dąbrowska (2010) herself uses a Likert-type scale in elicitation experiments and analyzes the responses with ANOVA and t-tests.
- Similarly, Bermel and Knittle (2012a,b) conduct an experiment using a Likert scale and explore their results with ANOVA statistics.

Our study: marginal change-of-state verbs in Russian

- *Ob''jasnit'* 'clarify, make X be clear' < *jasnyj* 'clear_{ADJ}'
- **Two most productive patterns: o-...-it' and u-...-it'**



- We are interested in **new coinages** like
 - *omuzykalit'* 'musicalize' (< *muzykal'nyj* 'musical_{ADJ}')
 - *ukonkretit'* 'concretize' (< *konkretnyj* 'concrete_{ADJ}')
 - *ovnešnit'* 'externalize' (< *vnešnij* 'external_{ADJ}')

Our experiment: A score-assignment test

The task: Evaluate the marked word using one of the statements.

Давно пора как-то оприличить наше общение более мягкими выражениями.

'It's high time we made our interaction respectable by using kinder statements.'

- 5 points - Это совершенно нормальное слово русского языка.
'This is an absolutely normal Russian word'
- 4 points - Это слово нормальное, но его мало используют.
'This word is normal, but it is rarely used'
- 3 points - Это слово звучит странно, но, может быть, его кто-то использует.
'This word sounds strange, but someone might use it'
- 2 points - Это слово звучит странно, и его вряд ли кто-то использует.
'This word sounds strange and it is unlikely that anyone uses it'
- 1 point - Этого слова в русском языке нет.
'This word does not exist in the Russian language.'

The scale

- The experiment was designed as a score-assignment test.
- Subjects were presented with sixty sentences and a rating system. Each sentence contained a verb that we wanted them to evaluate.
- We used a numerical scale of 5 points combined with a categorical scale of evaluative statements.
- In doing so we wanted to ensure a uniform interpretation of scale points across all subjects.
- What is crucial here is that this 5 point scale is very culturally entrenched in Russia because it is commonly used in Russian school and university grades.
- Every Russian is familiar with the scale of 5 points where 5 points mean the best grade.

Our study: on-line questionnaire, one task per page

QuestionPro Survey – WordWorld

surveys.questionpro.com/a/TakeSurvey;jsessionid=baadrzGZpDsqO7YdeFW7t

Google

Лингвистический эксперимент

27%

Back Questions marked with an * are required Exit Survey

8. Проще всего увкуснить творог добавлением изюма, банана и сладких ягод. *

- 5 – Это совершенно нормальное слово русского языка.
- 4 – Это слово нормальное, но его мало используют.
- 3 – Это слово звучит странно, но, может быть, его кто-то использует.
- 2 – Это слово звучит странно, и его вряд ли кто-то использует.
- 1 – Этого слова в русском языке нет.

Continue

POWERED BY QuestionPro

Stimuli

STANDARD WORDS

Words that are standard and conventionalized, might be stored in memory rather than generated on the fly

e.g.: *undo*

MARGINAL WORDS

Words that are generated by some speakers and can be understood / accepted by some speakers

e.g.: *unworry*

NONCE WORDS

Words that cannot be generated and do not exist

e.g.: *unblick*

Stimuli:

60 prefixed change-of-state verbs with the meaning 'make X be Y'

STANDARD WORDS

10 o + 10 u
(control group 1)

obogatit' 'enrich'
uprostit' 'simplify'

MARGINAL WORDS

10 o + 10 u
(experimental
group)

ovnešnit' 'externalize'
uvkusnit' 'make tastier'

NONCE WORDS

ex
co
an
pr
10 o + 10 u
(control group 2)
ot
vs
on
al

očavit'
učopit'

60 change-of-state verbs as stimuli

- All verbs used in the experiment are **deadjectival**. This decision is made in order to reduce the number of valuables.
- All standard and marginal verbs chosen for experiment are **morphologically transparent** and **analyzable** and have a clear existing adjectival base.
- All stimuli verbs are given as **perfective infinitives**.
- Verbs are presented **in contexts**.
 - For standard and marginal change-of-state verbs we use real contexts from the corpus, often shortened.
 - The contexts of nonce verbs are based on corpus contexts of real verbs with meanings similar to those that are assumed for nonce verbs.

3 research questions

PREDICTOR 1: PREFIX

Does the more productive prefix O- form more acceptable novel marginal verbs than the less productive prefix U-?

PREDICTOR 2: AGE OF SPEAKER

Does the speakers' leniency regarding marginal verbs correlate with age? Do adults (25-62 year old, N=51) have more conservative judgements than children (14-17 year old, N=70)?

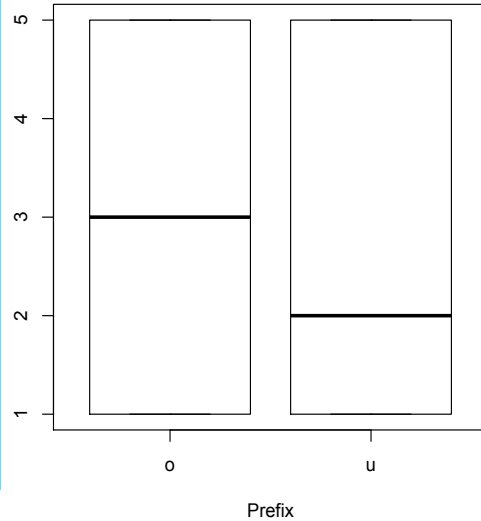
PREDICTOR 3: WORD CLASS

Are MARGINAL verbs of the two rival patterns (O- and U-) perceived more like STANDARD or more like NONCE verbs?

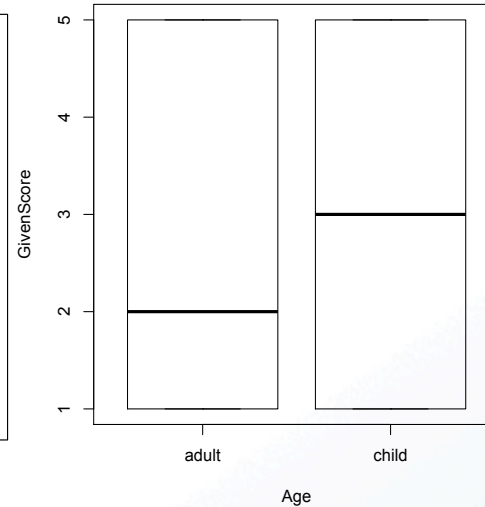
Central tendencies in data distribution

Verbs prefixed in O- overall tend to receive higher acceptability scores compared to U-verbs.

Distribution of scores across prefixes



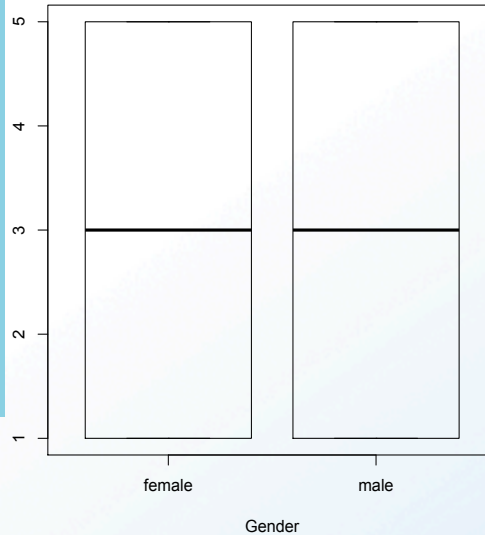
Distribution of scores across age groups



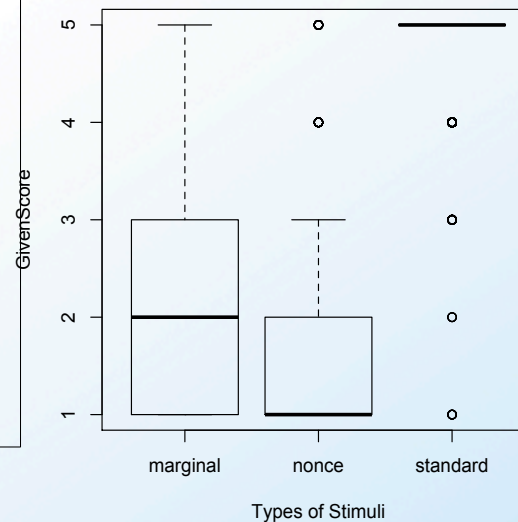
Children assign higher acceptability ratings than adults.

Gender does not make any difference.

Distribution of scores across genders



Distribution of scores across word categories



Marginal verbs received surprisingly low acceptability scores.

Overview: 5 statistical models

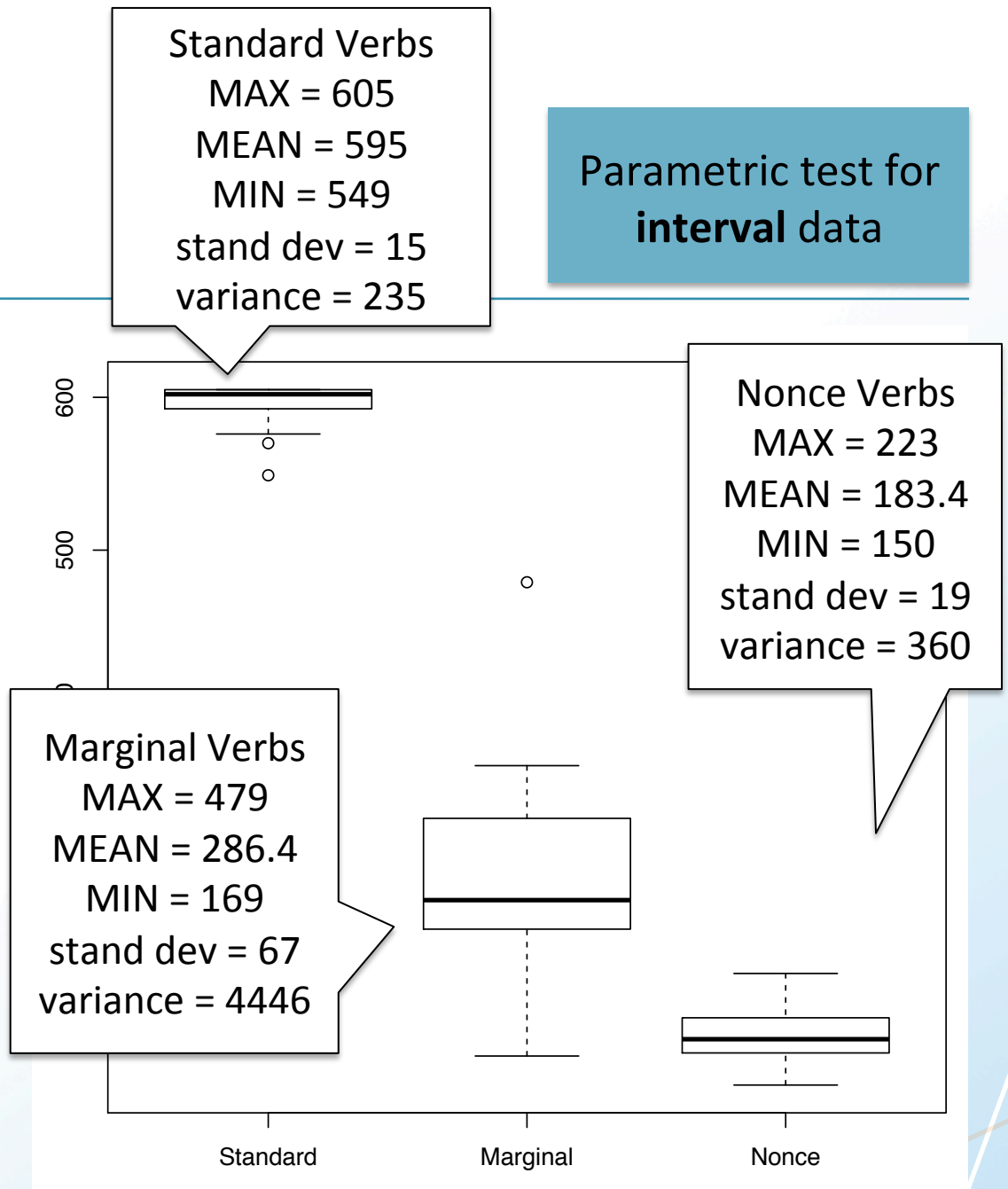
Type of test	Name	Type of data	Significant factors
Parametric	ANOVA	For interval data	WordType
	Ordinal logistic regression	For ordinal data	WordType >>> AgeGroup > Prefix
	Regression mixed-effects model	For ordinal data	WordType >>> AgeGroup
Non-parametric	Regression tree & Random forests	For numerical ordinal data	WordType >>> AgeGroup > Prefix
	Classification tree & Random forests	For categorical data	WordType >>> Prefix > AgeGroup

Do parametric and non-parametric tests provide different insights?

Which model is the most informative regarding marginal words?

Model 1. ANOVA

- The impact of **age** and **prefix** is non-significant.
- The impact of **word type** (standard vs. marginal vs. nonce) is significant:
- $F = 546$, $df = 2$, $p\text{-value} < 2.2e-16$



Model 1. ANOVA

T-test RESULTS for **standard vs. marginal** words:

$t = 20$, $df = 21$, $p\text{-value} = 3.173e-15$, 95% confidence interval is 277
340

T-test RESULTS for **marginal vs. nonce** words:

$t = 7$, $df = 22$, $p\text{-value} = 1.098e-06$, 95% confidence interval is 71
135

- Marginal verbs are evaluated by speakers more like nonce verbs than standard verbs.
- This suggests that speakers are more sensitive to frequency than to semantic transparency.

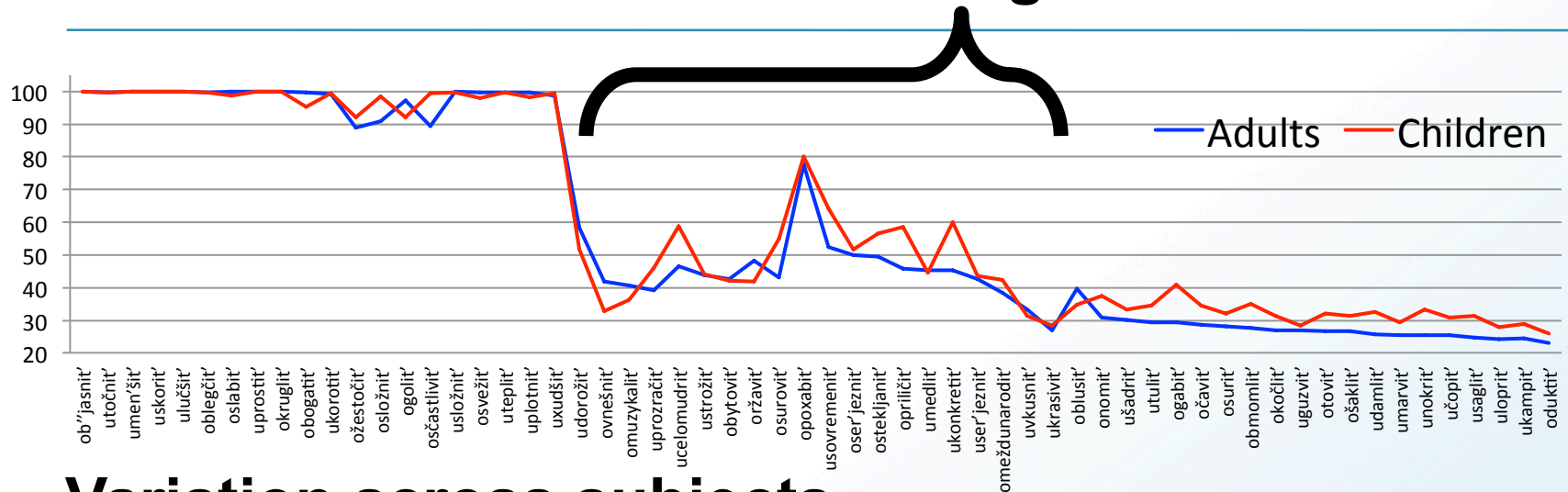
2. Ordinal logistic regression

Factor	Chi-Square	Degrees of freedom	<i>p</i> -value	
AgeGroup	59.28	1	< .0001	***
Prefix	5.45	1	0.0195	*
WordType	3415.95	2	< .0001	***
TOTAL	3425.06	4	< .0001	***

- Three factors are statistically significant predictors of acceptability scores – **WordType** and **AgeGroup** and **Prefix**.
- The impact of Gender was found insignificant: Chi-Square= 0.33, df = 1, p-value = 0.56.
- The impact of **WordType** accounts for most of data, while the other two factors are very minor.

Random-effects factors

Variation across individual marginal stimuli



Variation across subjects

Marginal verb	Gloss	Number of subjects who gave				
		5 points ("normal word")	4 points	3 points	2 points	1 point ("does not exist")
<i>usovremenit'</i>	'modernize'	22	26	27	18	28
<i>opriličit'</i>	'make decent'	9	25	33	22	31

3. Regression mixed-effects model for ordinal data

Parametric test for ordinal data

Random-effects factor	Name	Variance	Standard Deviation
SubjectCode	(Intercept)	1.091	1.045
Stimulus	(Intercept)	1.043	1.021

Fixed-effects factor	Estimate	Std.error	z value	Pr(> z)	
AgeGroup-child	0.5803	0.2013	2.883	0.00394	**
WordType-nonce	-1.7791	0.3292	-5.405	6.48e-08	***
WordType-standard	7.4203	0.3712	19.991	< 2e-16	***

- The impact of **Gender** and **Prefix** is found insignificant.
- The most optimal fitted model indicated the significant effects of **WordType** and **AgeGroup**.
- The effect of WordType is more significant than that of AgeGroup.

4 and 5. Regression and Classification trees & Random Forests (CART)

Non-parametric
test for **ordinal** data

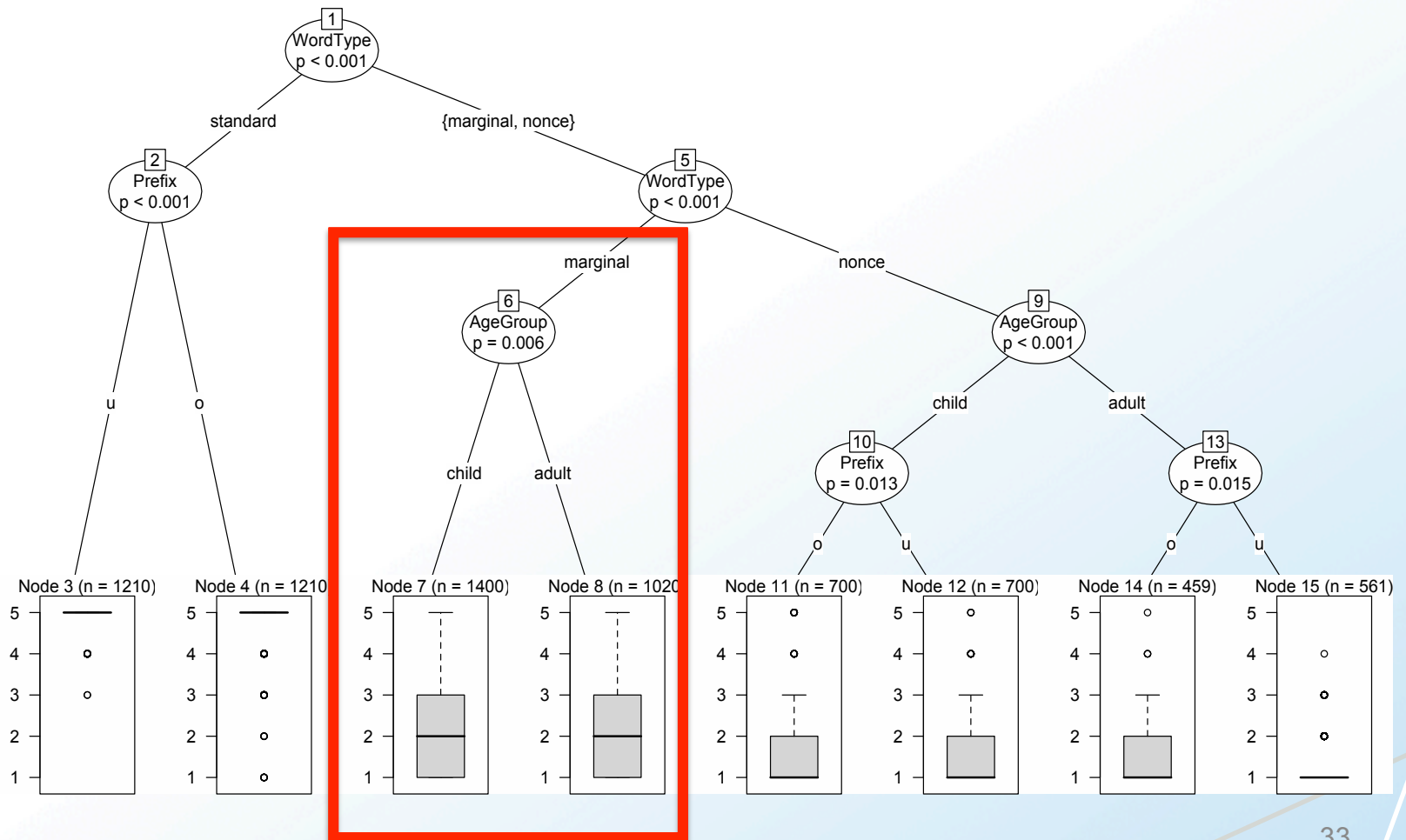
- Classification and Regression Trees is a new method that is quickly gaining popularity in genetics, medicine (Strobl et al. 2009: 324), social sciences, and linguistics (Tagliamonte & Baayen 2012 and Baayen et al. 2013).
- Classification and Regression Trees is a non-parametric statistical technique which is appropriate for non-interval data.
- More flexible in modeling combinations of predictors than Logistic Regression (Faraway 2006: v).
- Trees do not hold any assumptions about the normal distribution of the response variable (as opposed to the logistic regression model)
- Can cope with any data structure and type.
- Highly recommended for unbalanced datasets.

How exactly does CART work?

- CART is an algorithm-based method.
- The outcome of the CART analysis is a graphically plotted “tree” created via a recursive partitioning of data.
- The Tree represents an algorithm of data partitioning which consists of recursive binary splits, each based on one variable.
- The Tree outlines a decision procedure of predicting the values of the dependent variable.
- As a result, recursive splits subdivide the entire data set into several non-overlapping subsets of data.

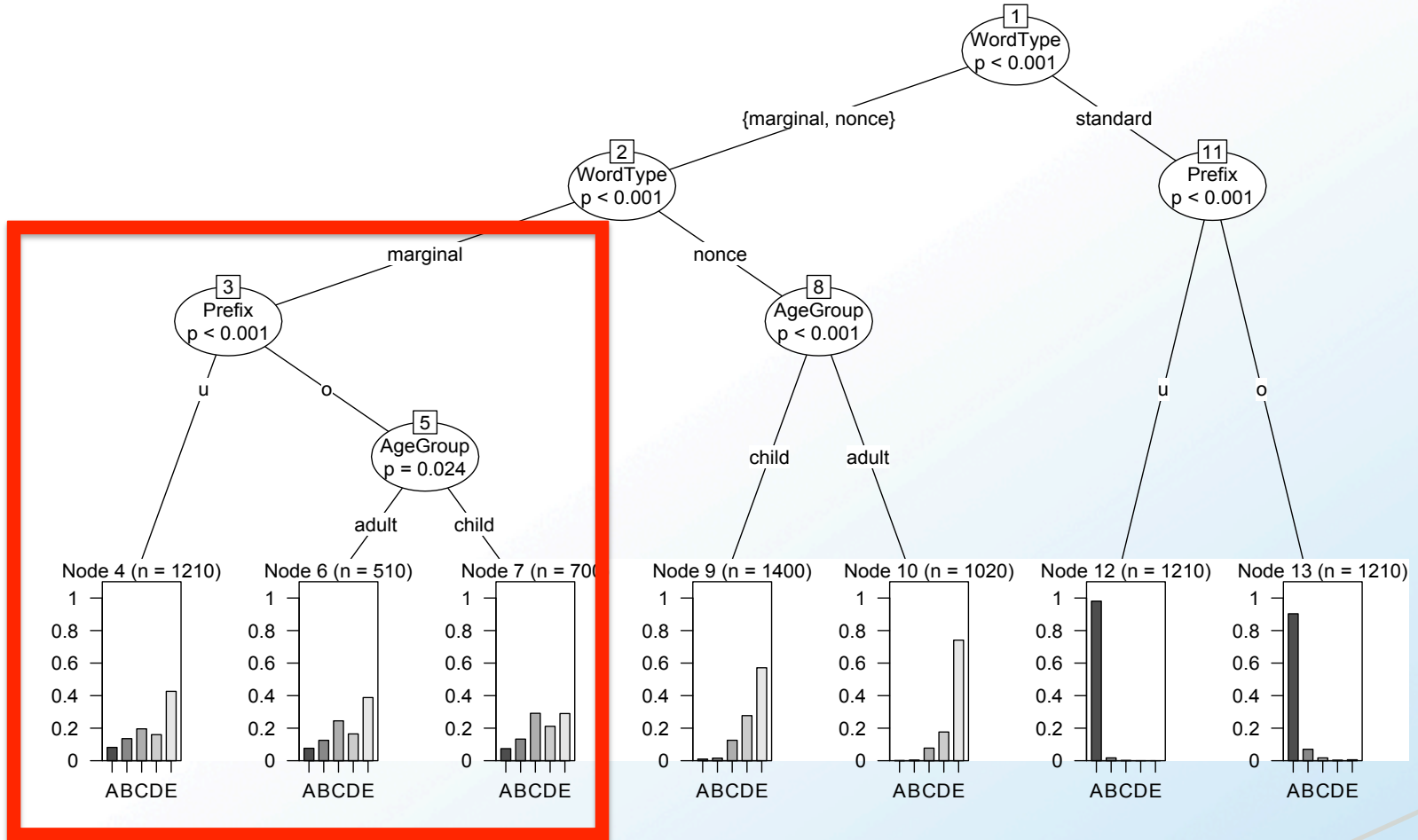
4. Regression tree & Random forests

Non-parametric test for **ordinal** data



5. Classification tree & Random forests

Non-parametric test for categorical data



Classification tree & Random forests model

This model demonstrates that the importance of a factor can belong to different “levels”: what is crucial at the level of a local split (AgeGroup and Prefix) might have very small overall predicting power considering the entire dataset, while other factors (like WordType) can determine the major trend of data distribution, as we saw in the major split of the Trees and the highest bar in the Random Forest plots.

The outcome of Random Forest analyses indicates that AgeGroup and Prefix do have some importance but their effect is very small. This effect is revealed in high level interactions of the factors.

Random Forests

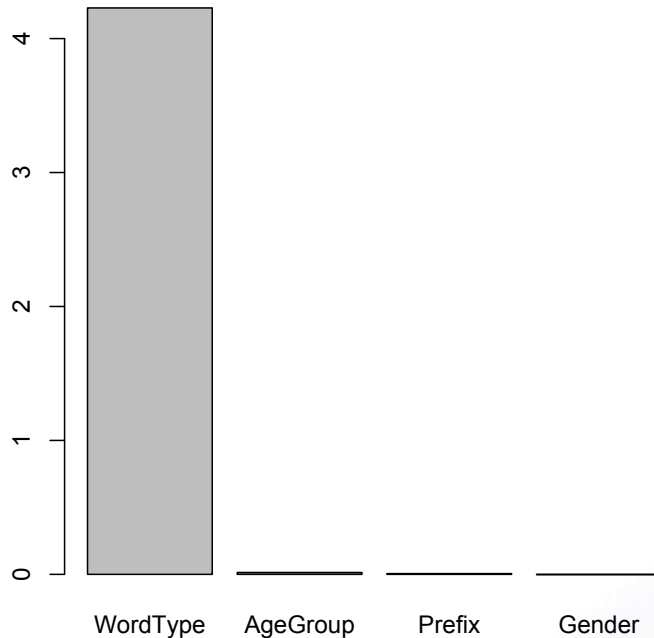


Figure 1: Variable importance scale for ordinal data (A>B>C>D>E).

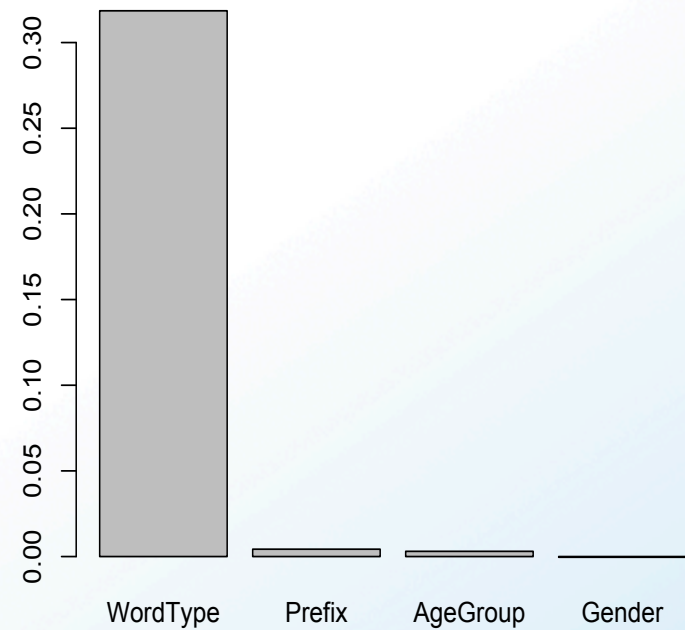


Figure 2: Variable importance scale for categorical data (A, B, C, D, E).

AgeGroup and Prefix do have some importance but their impact on the overall distribution of data is very small.

Summing up

Type of test	Name	Type of data	Significant factors
Parametric	ANOVA	For interval data	WordType
	Ordinal logistic regression	For ordinal data	WordType >>> AgeGroup > Prefix
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Do parametric and non-parametric tests provide different insights?

Which model is the most informative regarding marginal words?

Conclusions

Do parametric and non-parametric tests provide different insights?

- Parametric tests provide outcomes comparable with non-parametric models:
 - All models identify WordType as the major predictor.
 - The differences concern the factors AgeGroup and Prefix that have very small impact.

Which model is the most informative regarding marginal words?

- Classification Tree & Random Forest model
 - Safest and most appropriate for this data set
 - Most informative
 - Very detailed
 - User-friendly 😊

Anything else?

- The use of culturally entrenched grading scale is an advantage.

Now it's

CLEAR

Cognitive Linguistics: Empirical Approaches to Russian

Thank you!
Спасибо!
Tusen takk!

Contact us at anna.endresen@uit.no, laura.janda@uit.no

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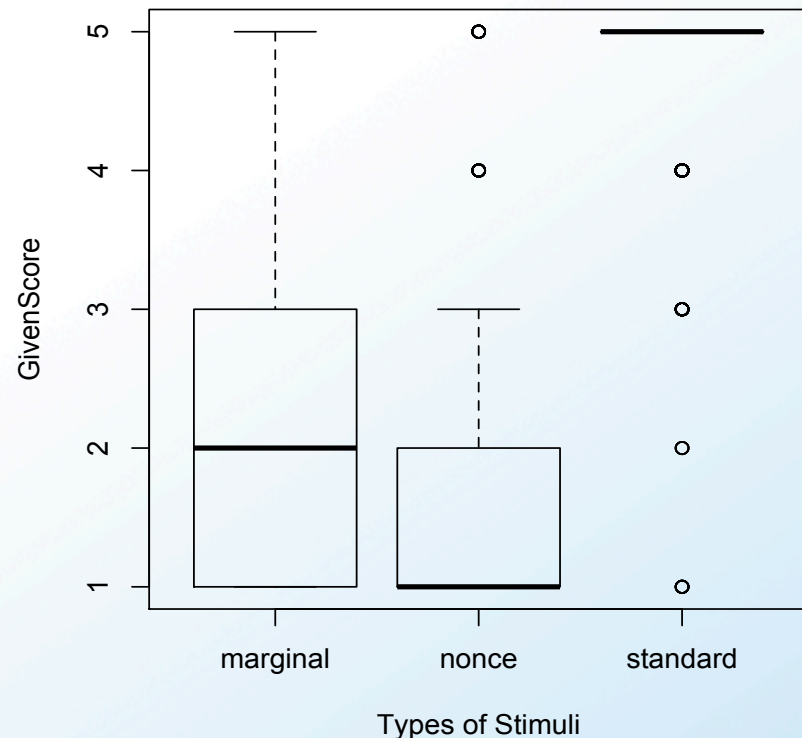
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Additional slides

Impact of Word type

- Types of stimuli (Word type) constitute three distinct patterns in terms of their ratings and MEDIANS.
- Marginal verbs have the MEDIAN score “2” and in this sense they are much closer to nonce verbs (MEDIAN score “1”) than standard verbs.
- Standard verbs, by contrast, receive the MEDIAN score “5” and form the most homogeneous group in terms of ratings.

Distribution of scores across word categories

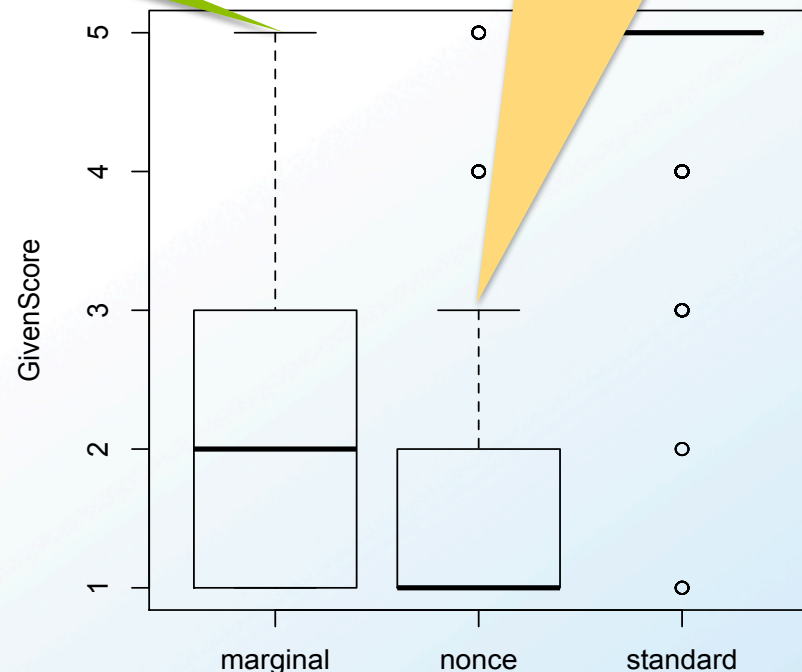


Whiskers indicate that the ratings of marginal verbs can be as high as score “5” (= “This is an absolutely normal Russian word”)

Whiskers of the nonce words reach only the score “3” (= “This word sounds strange, but someone might use it”).

- Types of stimuli (Word type) constitute three distinct patterns in terms of their ratings and MEDIANS.
- Marginal verbs have the MEDIAN score “2” and in this sense they are much closer to nonce verbs (MEDIAN score “1”) than standard verbs.
- Standard verbs, by contrast, receive the MEDIAN score “5”.

Distribution of scores across categories



Overall marginal verbs received from subjects surprisingly low acceptability scores: half of marginal stimuli received the lowest scores of 1 and 2.

What do these results mean?

- Each type of word has a different behavior
- Marginal words are semantically transparent, but nonce words are not
- **Marginal words** are rated **more like nonce words** than like standard words
- Speakers are **more sensitive to frequency than to semantic transparency**
- **Frequency**, which is related to **performance**, is a **stronger factor than competence** (ability to unpack morphological patterns)
- **Memory** may be a **stronger factor than use of productive rules**